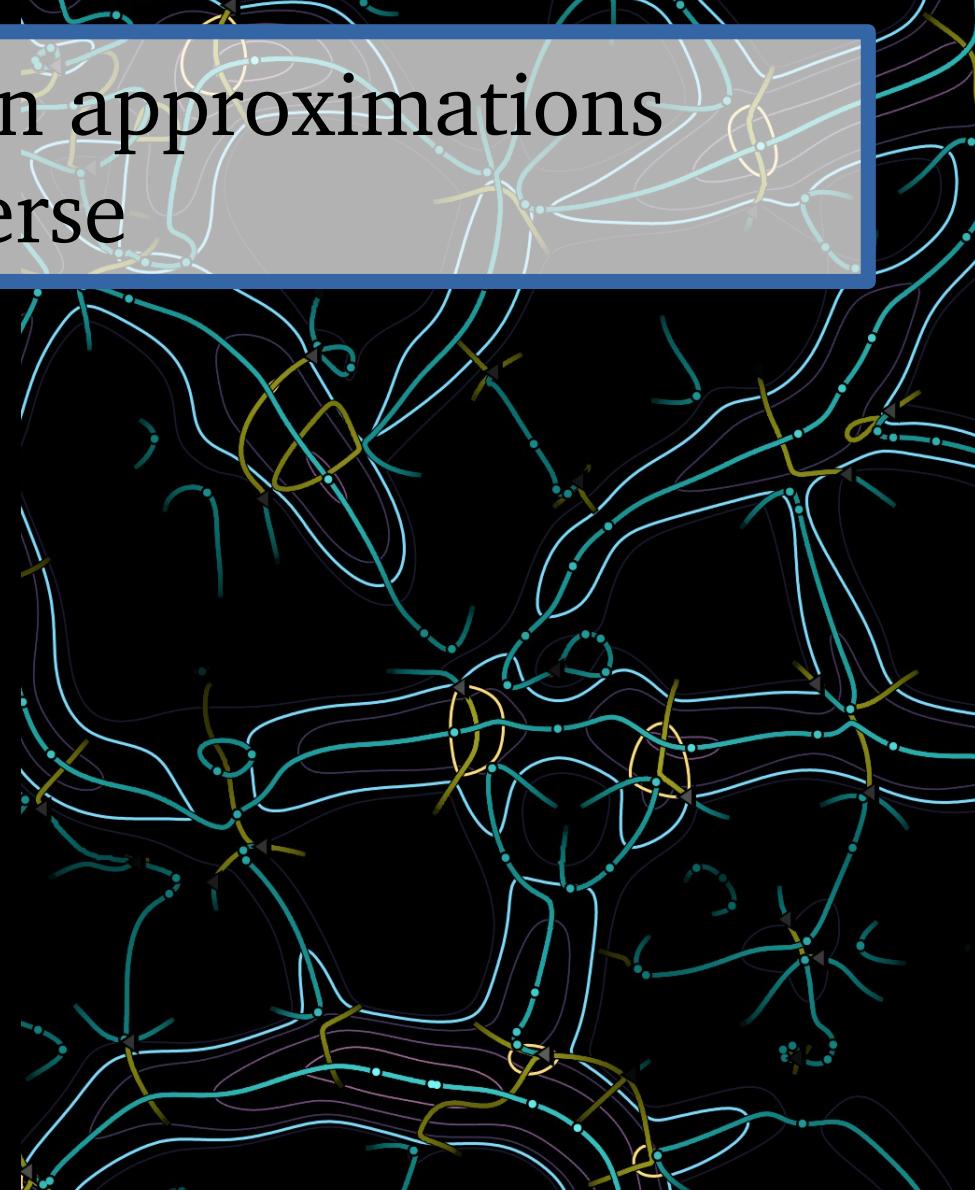


# Zeldovich and Adhesion approximations and the *real* Universe

IAU S308 “the Zeldovich Universe”  
23/06/2014

Johan Hidding  
Kapteyn Astronomical Institute

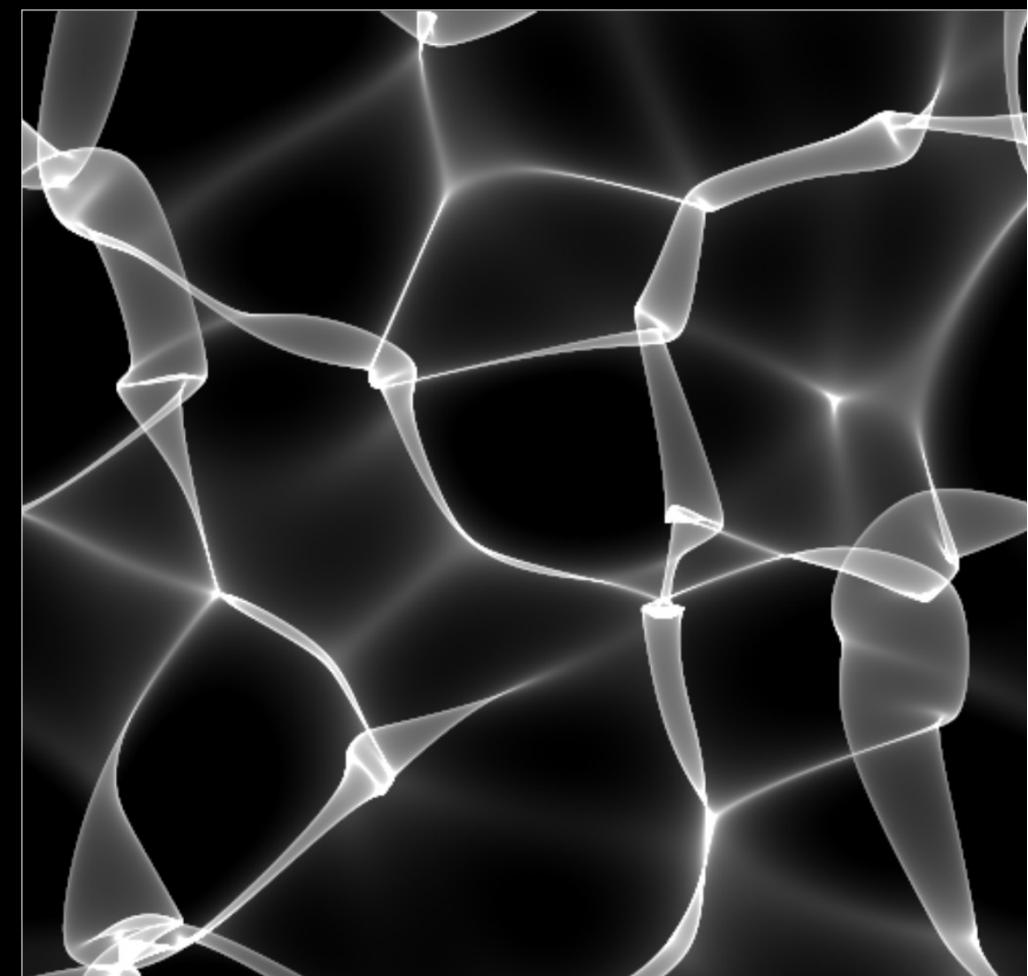
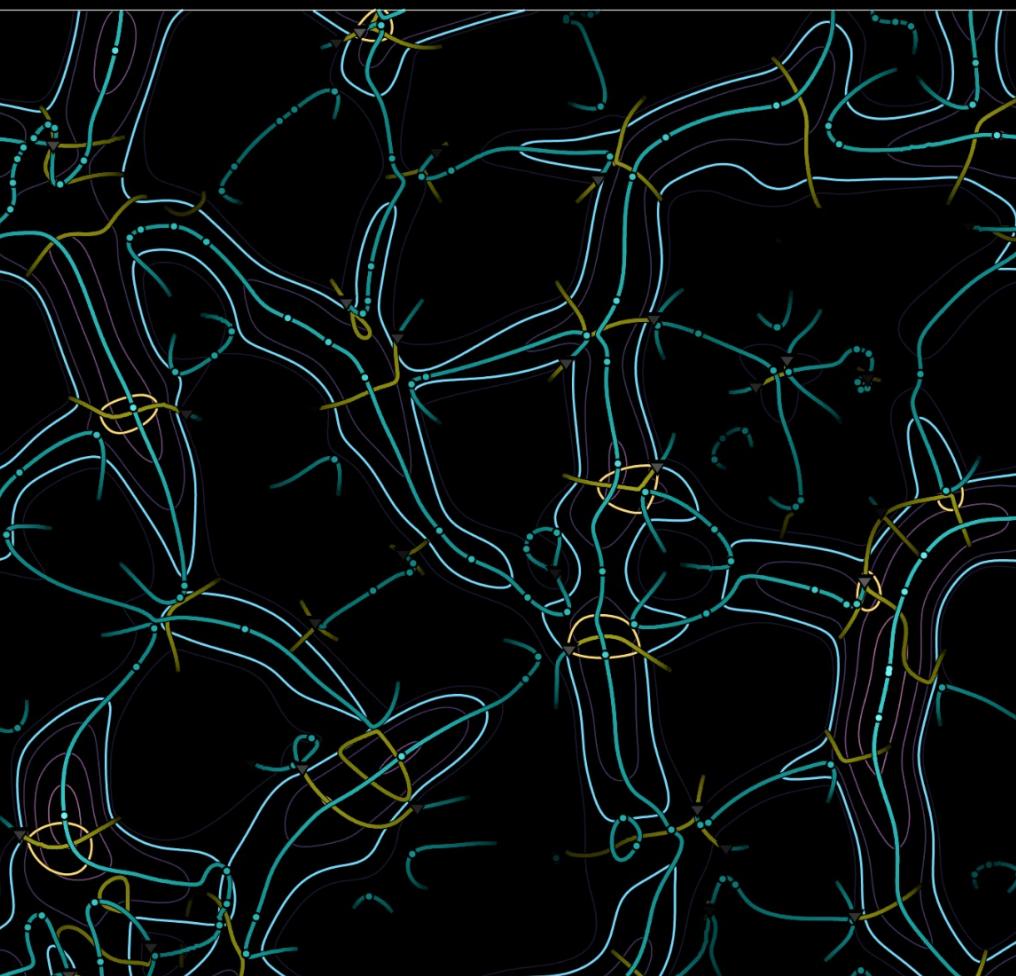
Rien van de Weijgaert  
Sergei Shandarin  
Gert Vegter  
Bernard Jones



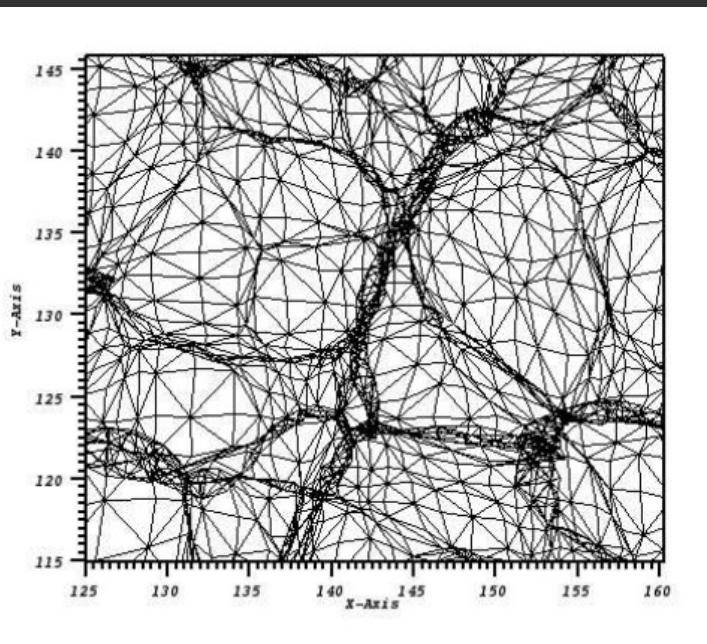
Lagrangian space

# $A_3$ -lines

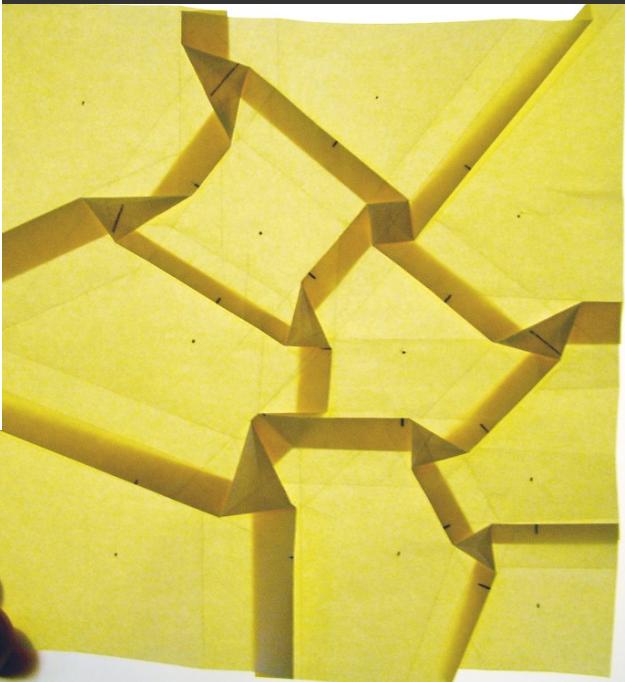
Eulerian space



# Phase-space

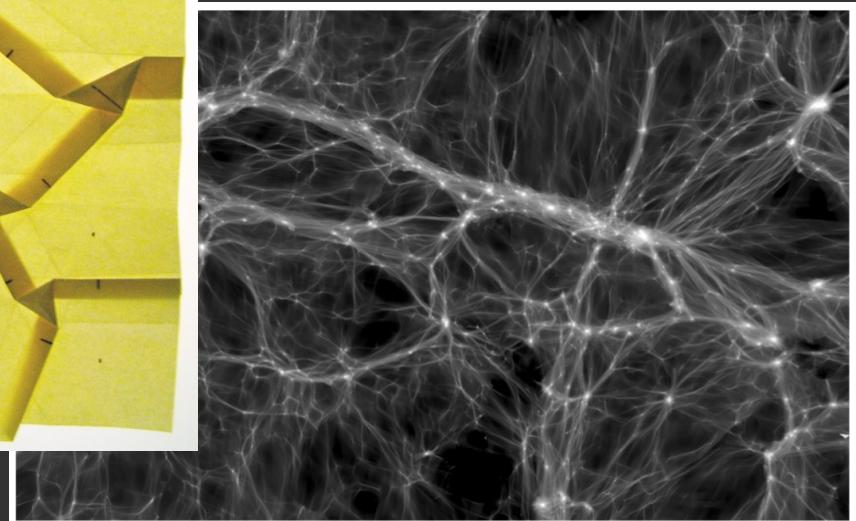


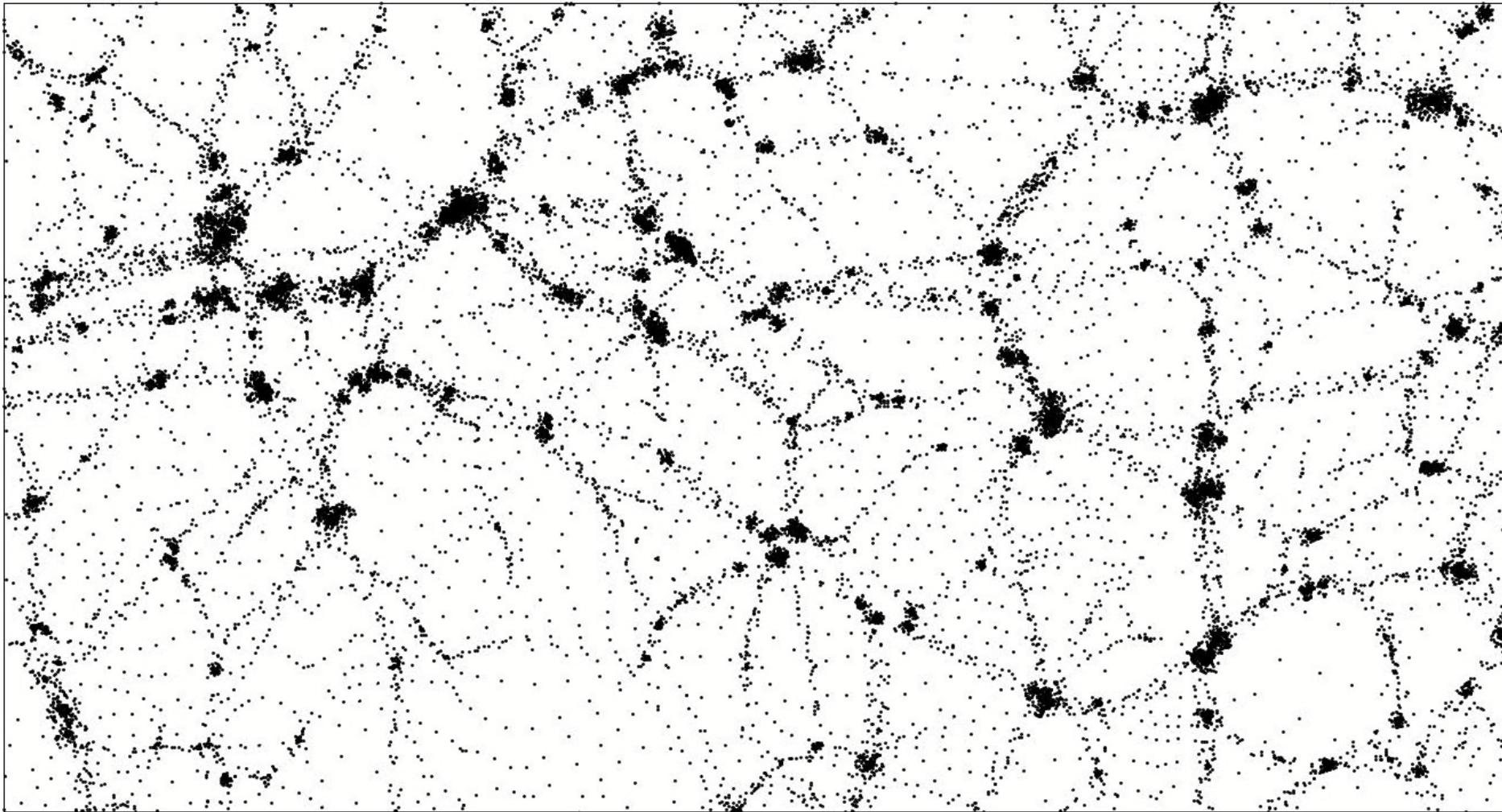
Shandarin et al. (2012)

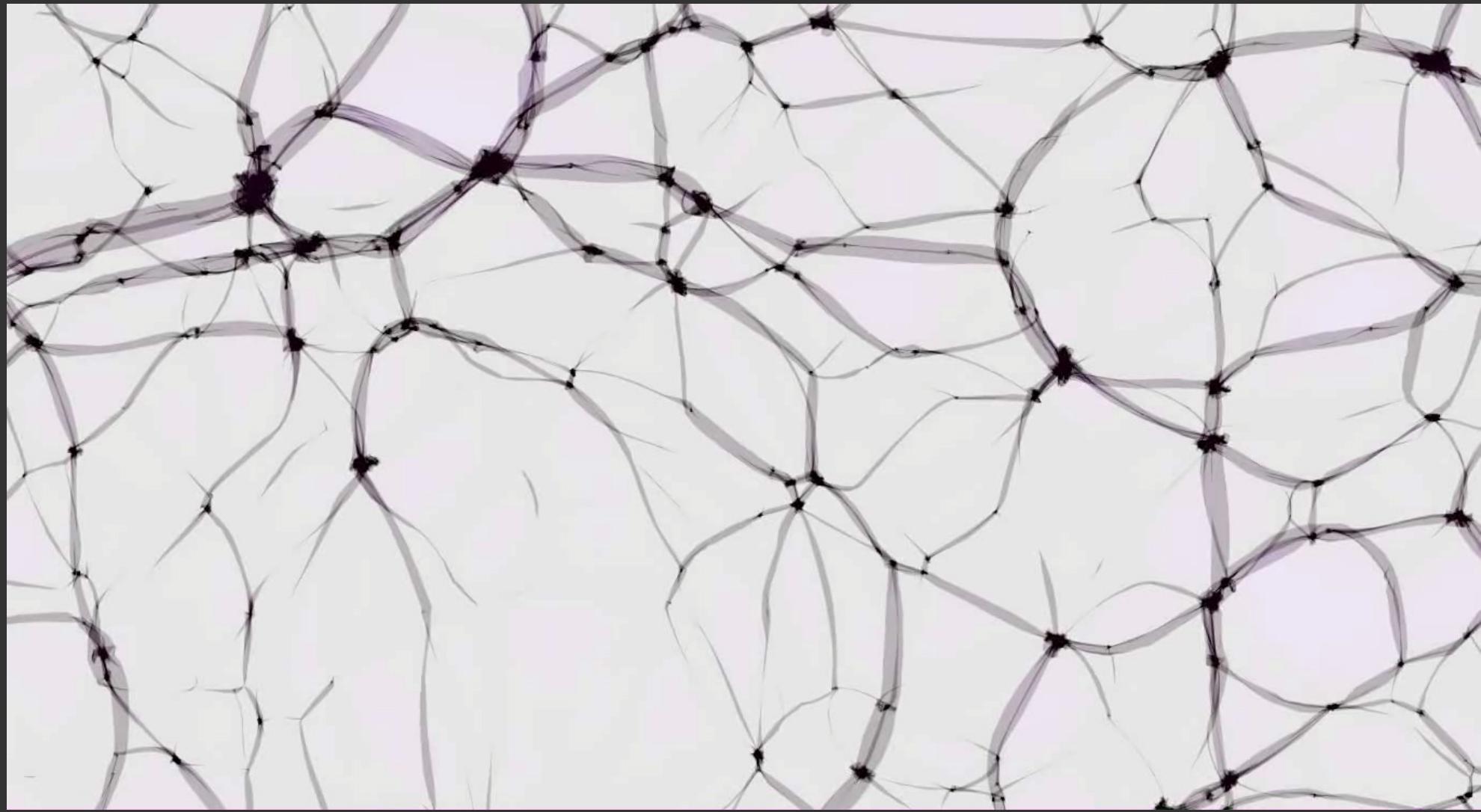


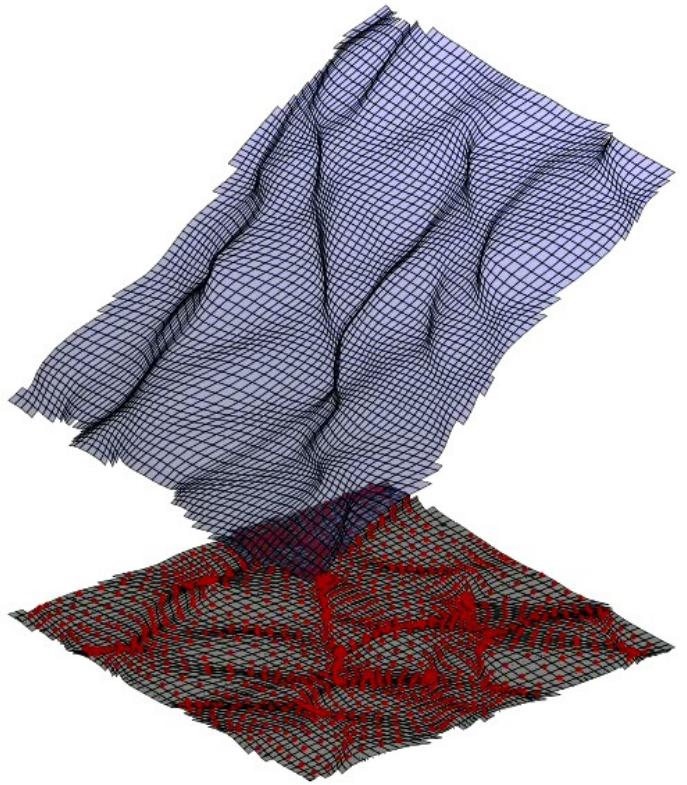
Neyrinck et al. (2012)

Abel et al. (2012)





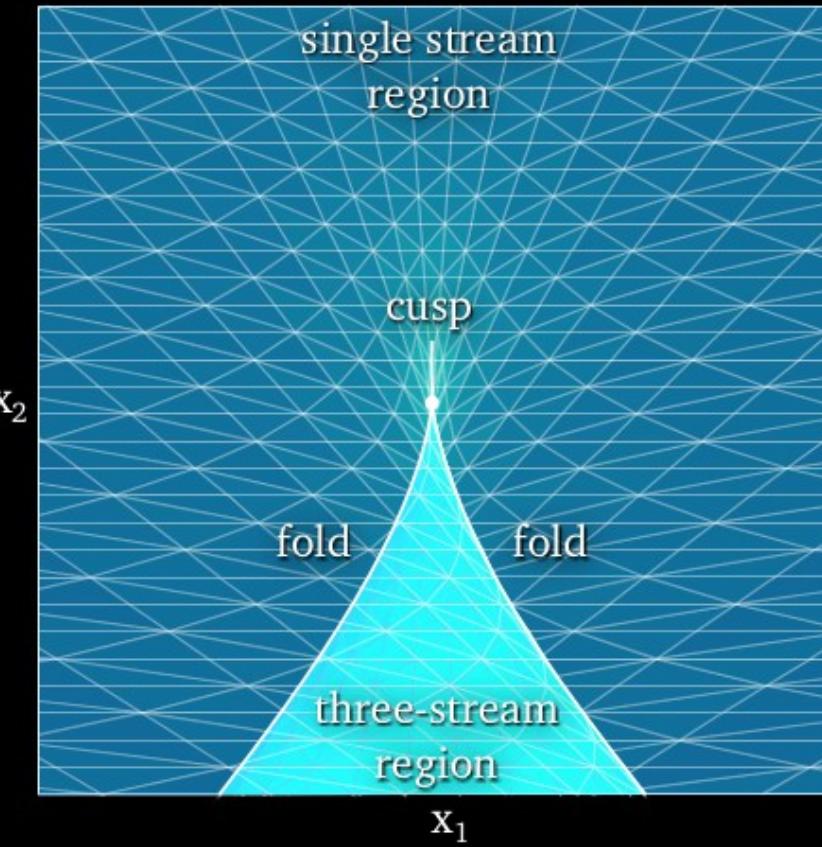
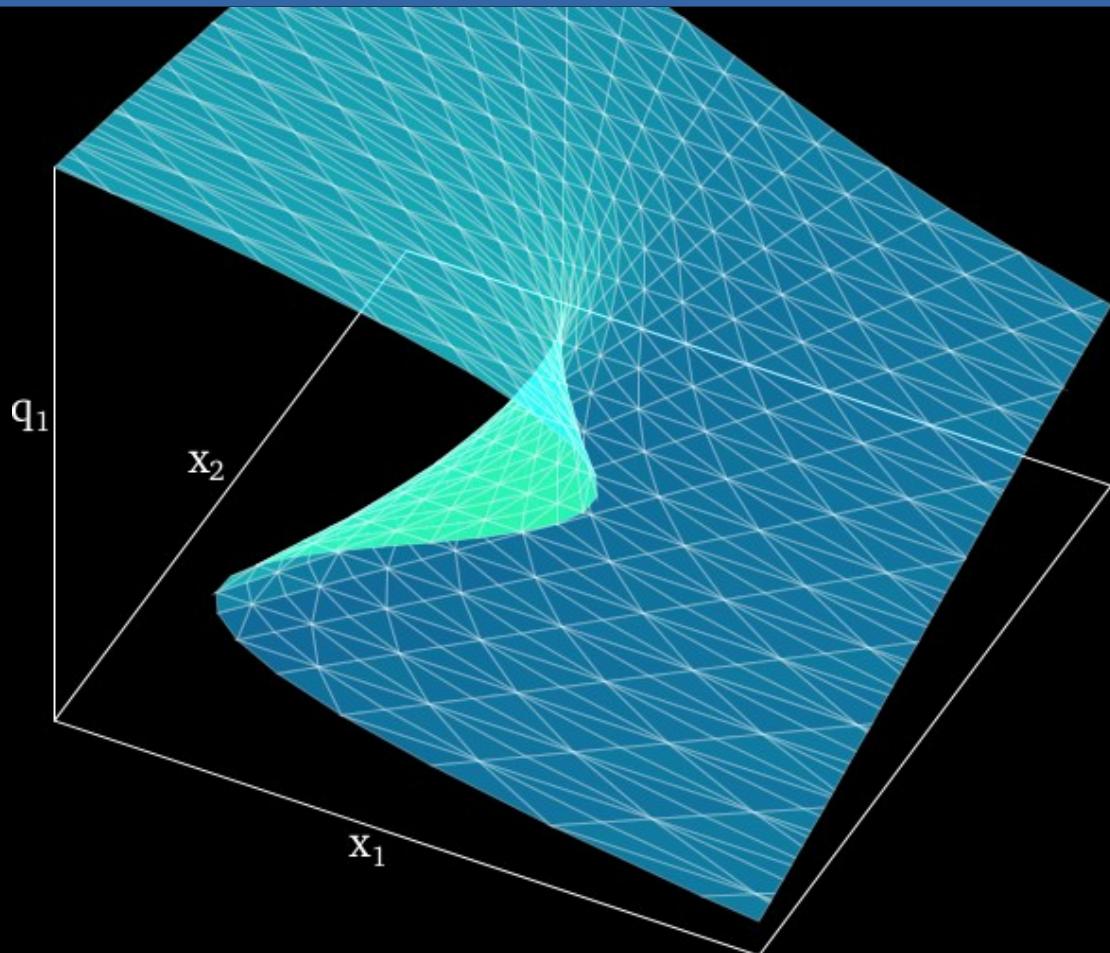




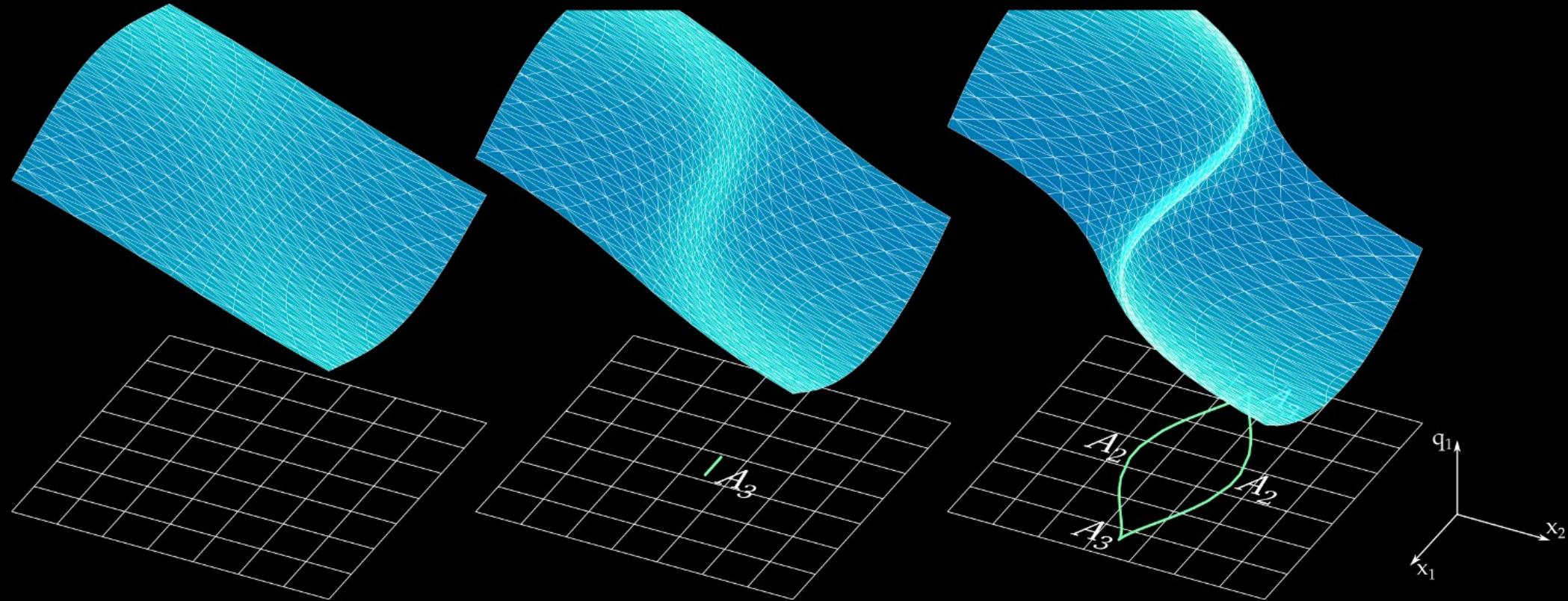
- Use Lagrangian continuity to trace the folds in phase-space
- Classify different types of potential *flow*

$$x = q - D \nabla \Phi$$

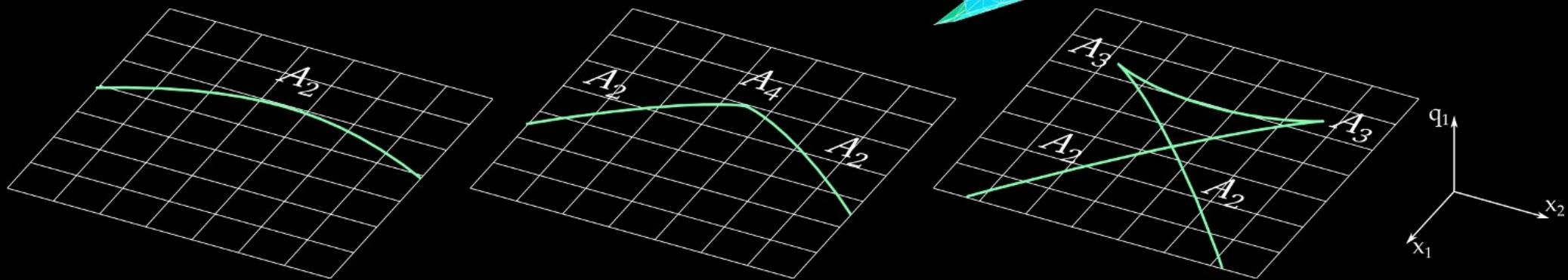
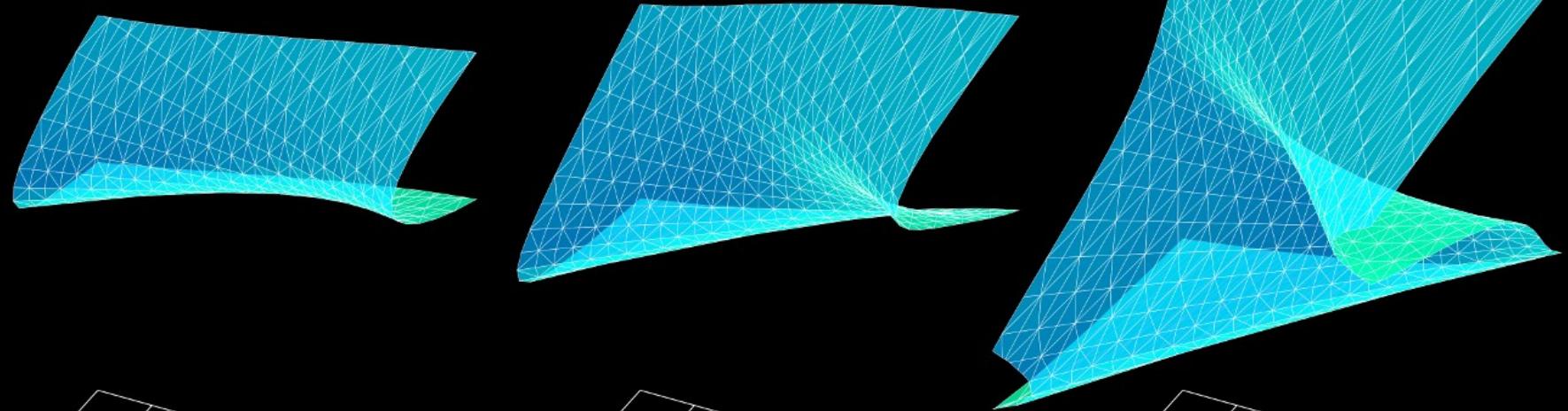
# Mathematics of folds in phase-space



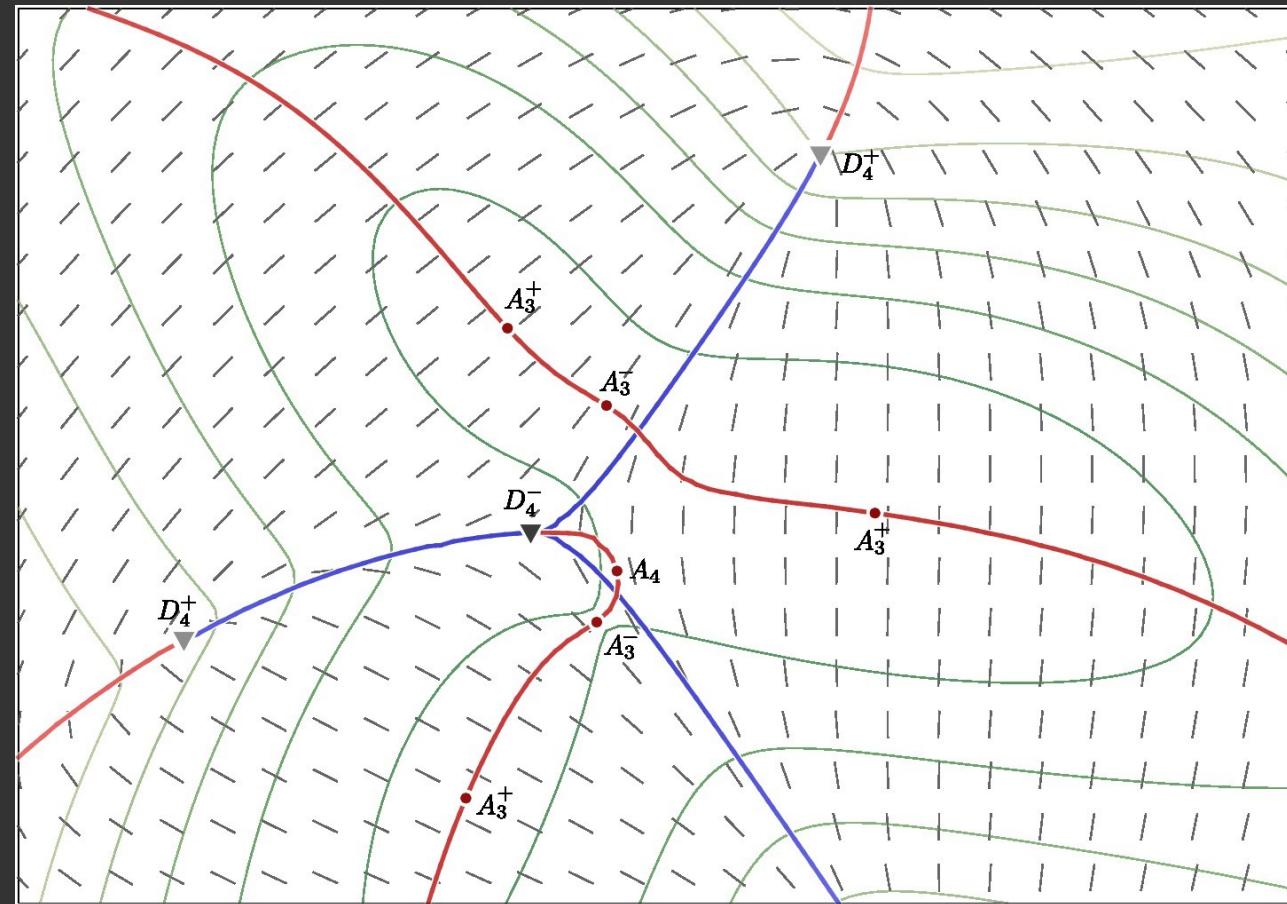
# Mathematics of folds in phase-space



# Mathematics of folds in phase-space



# Catastrophe Theory



- Identify critical lines in tensor field
- $A_3$  – lines

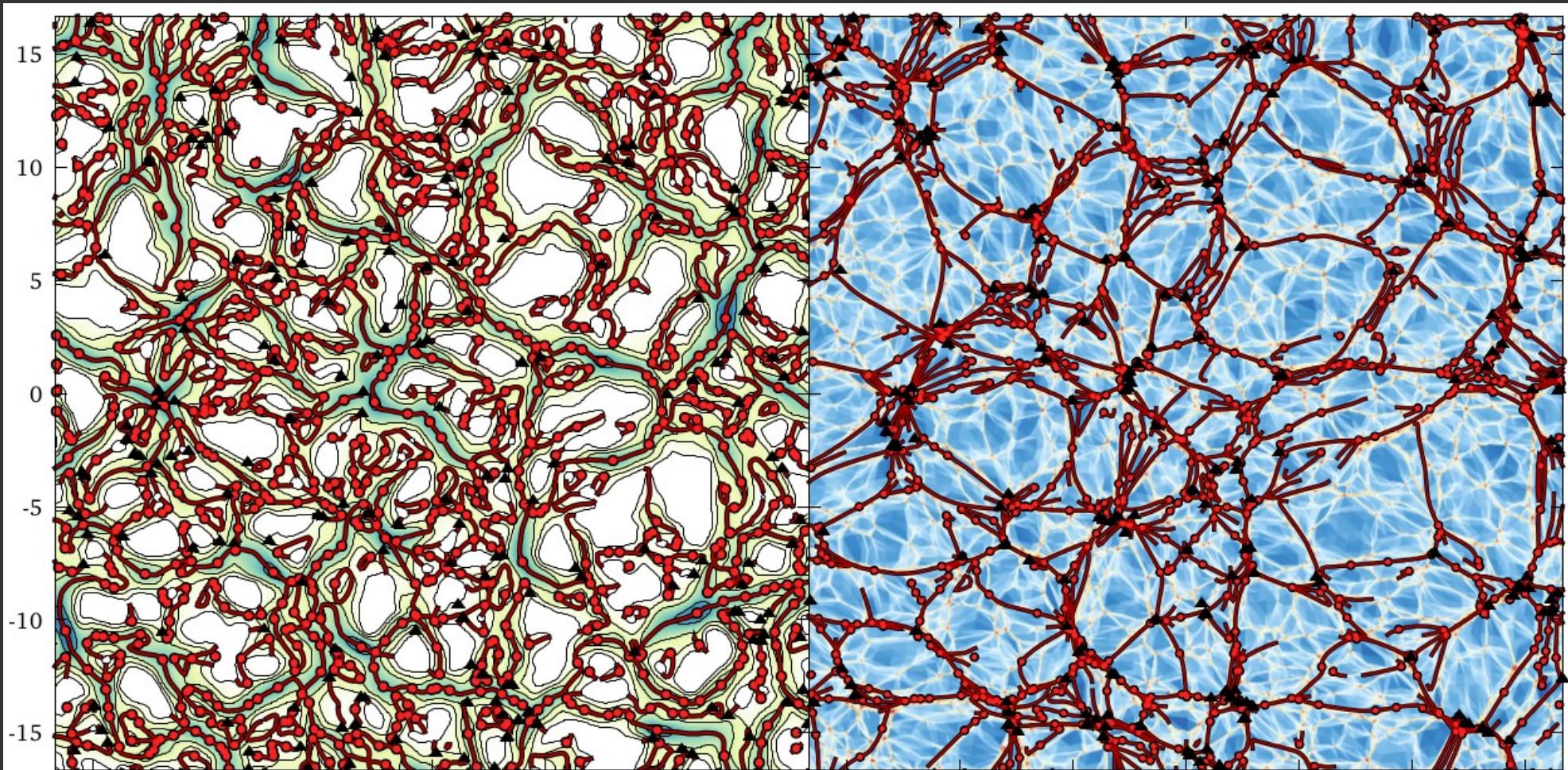
$$\nabla \lambda \cdot e_\lambda = 0$$

Arnold, Zeldovich & Shandarin (1982)

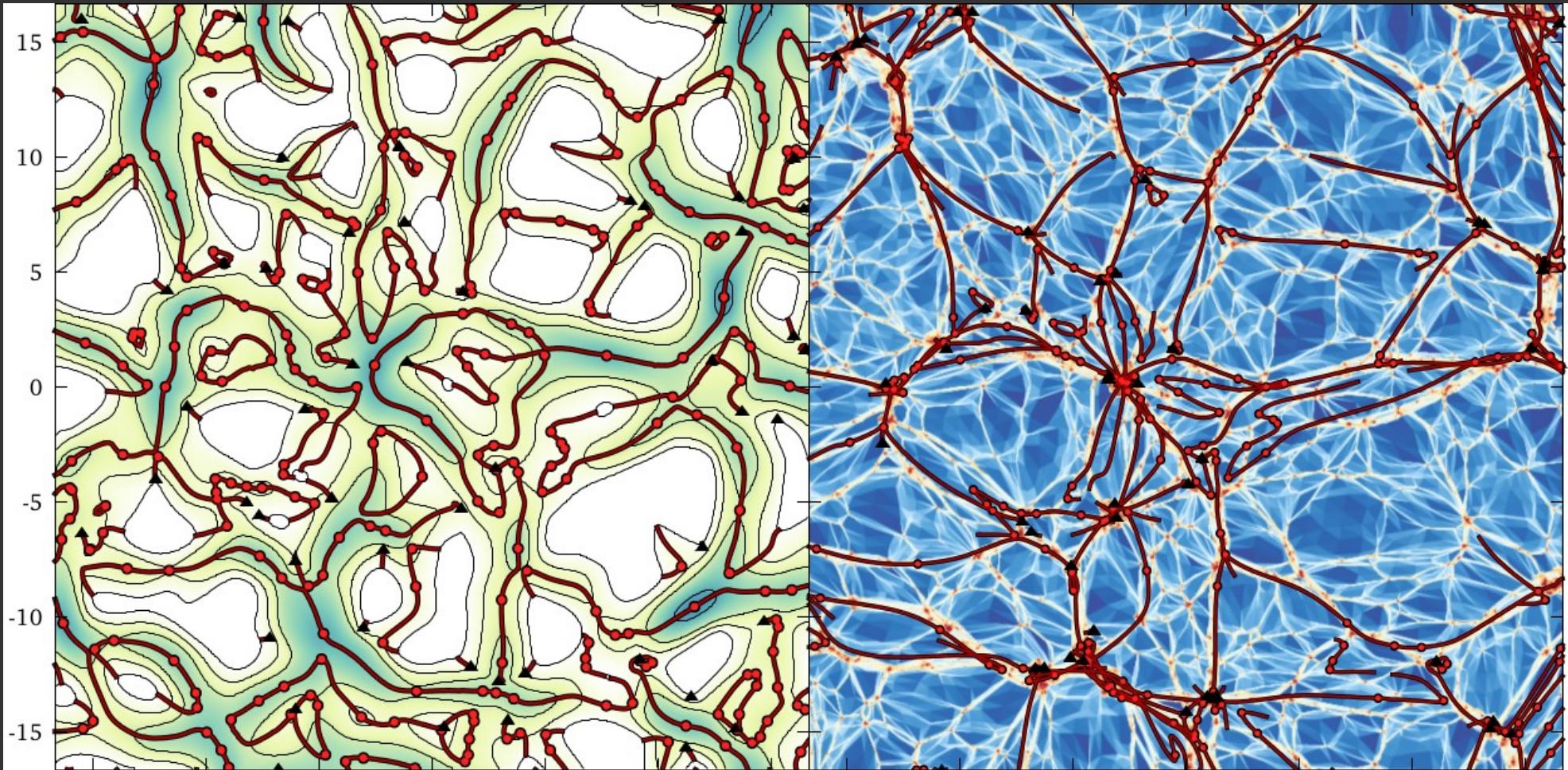
Arnold (1986)

Hidding, Shandarin & van de Weygaert (2014)

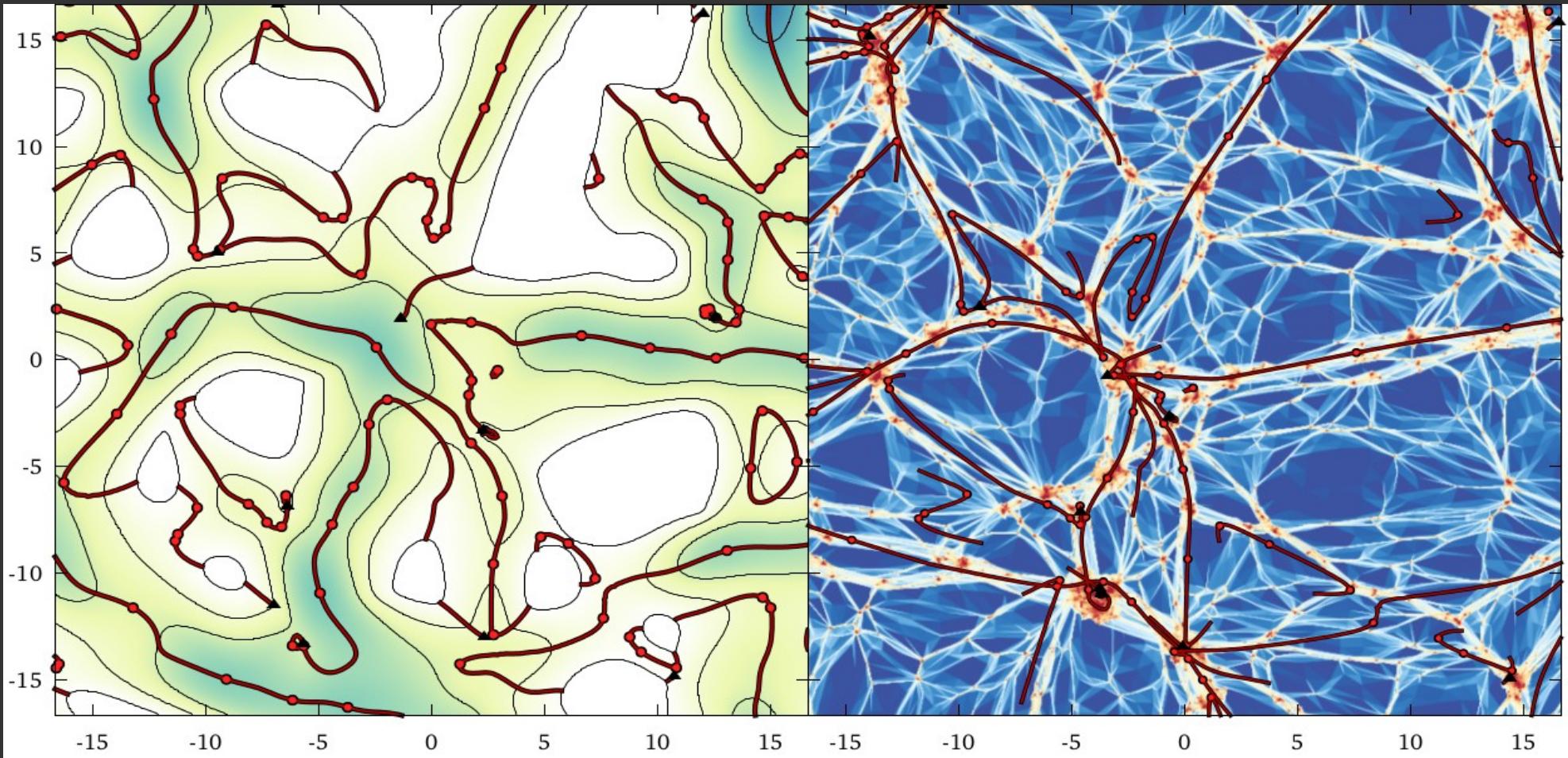
# $A_3$ -lines and N-body simulation

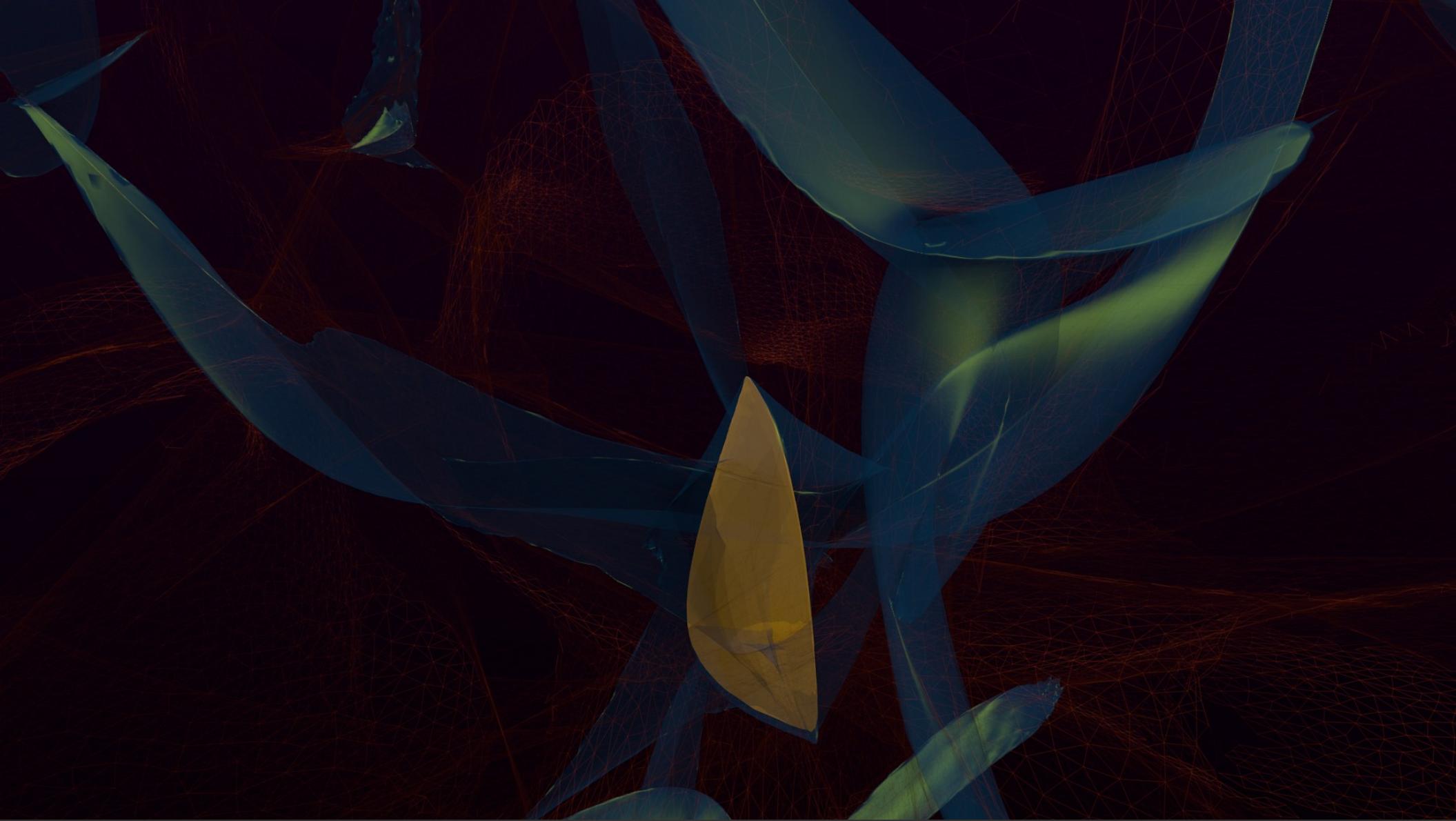


# $A_3$ -lines and N-body simulation



# $A_3$ -lines and N-body simulation





- Zeldovich

## Adhesion

$$\partial_t u + (u \cdot \nabla) u = 0$$

- Adhesion

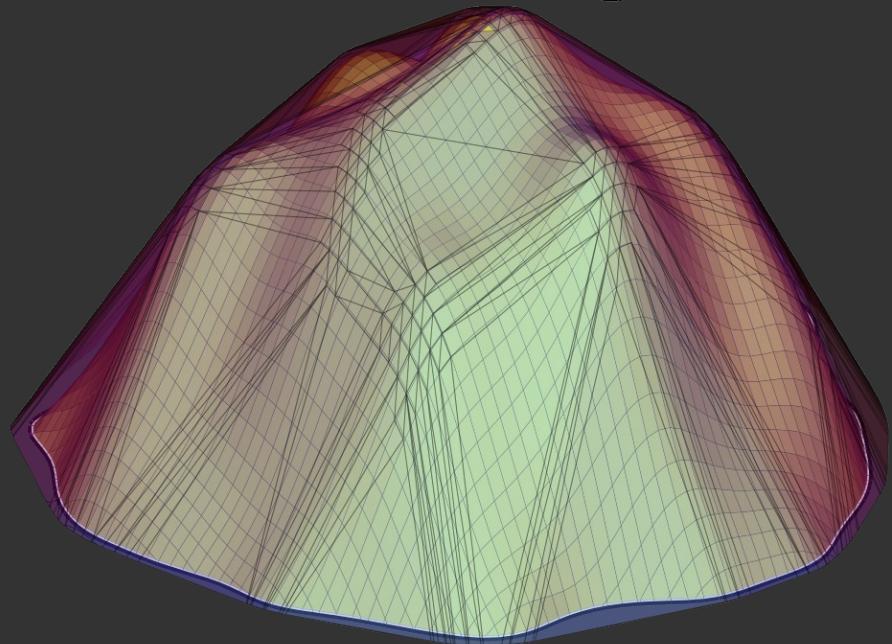
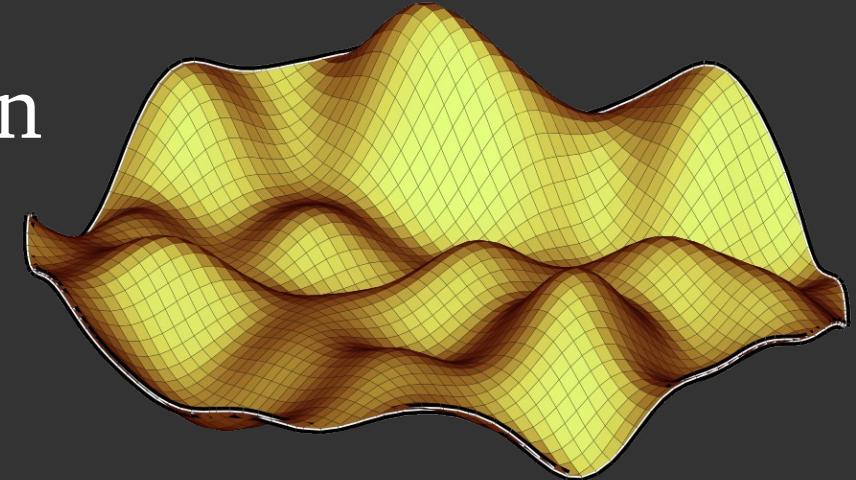
$$\partial_t u + (u \cdot \nabla) u = \nu \nabla^2 u$$

Saichev & Gurbatov (1984)

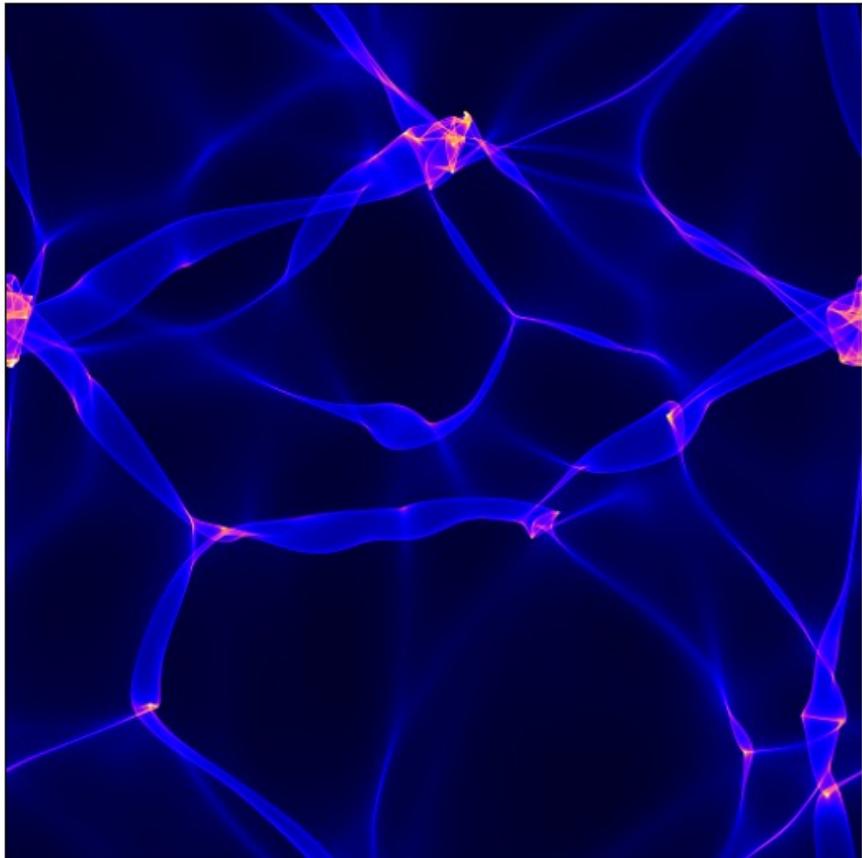
Shandarin & Zeldovich (1989)

...

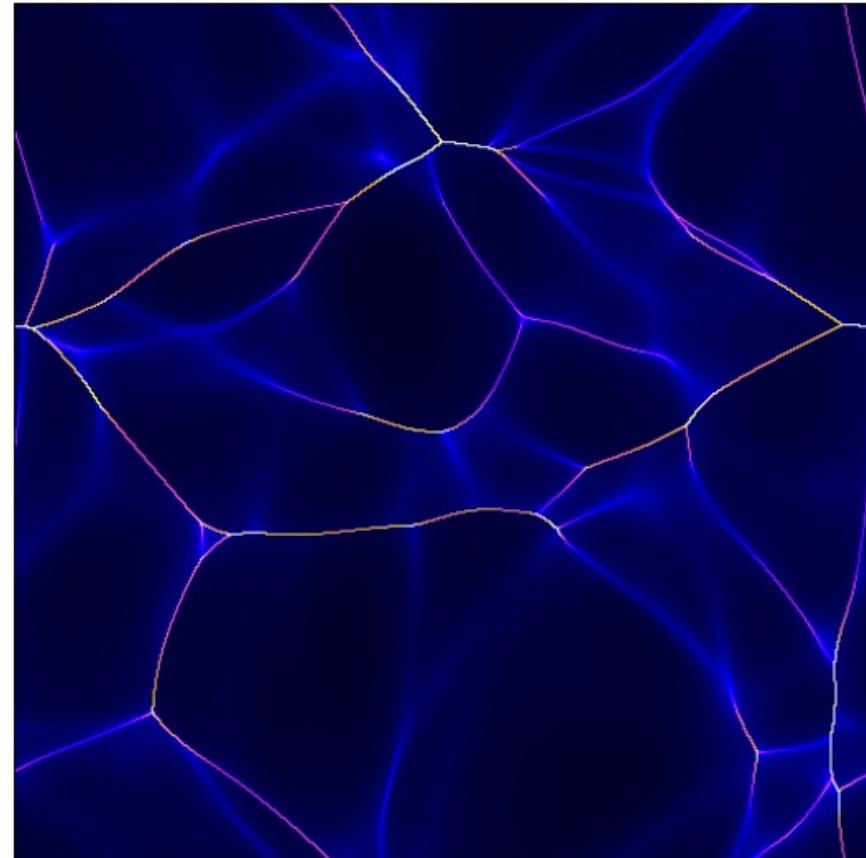
Hidding et al. (2014) in prep.



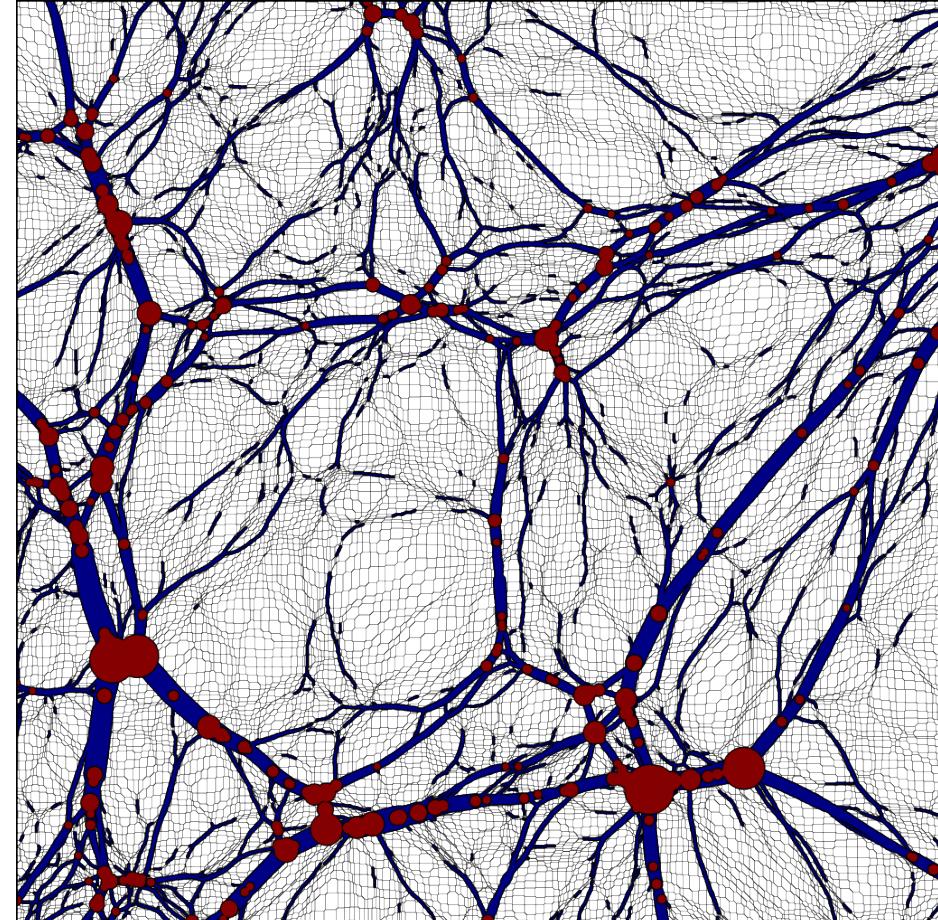
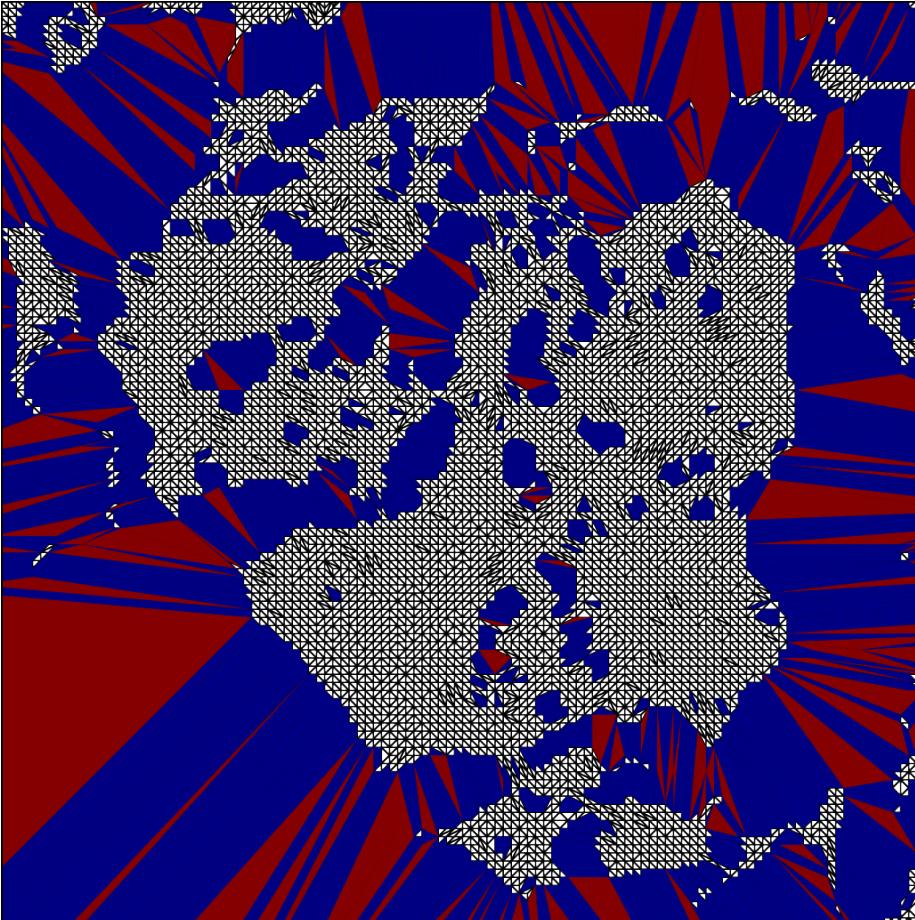
Zeldovich



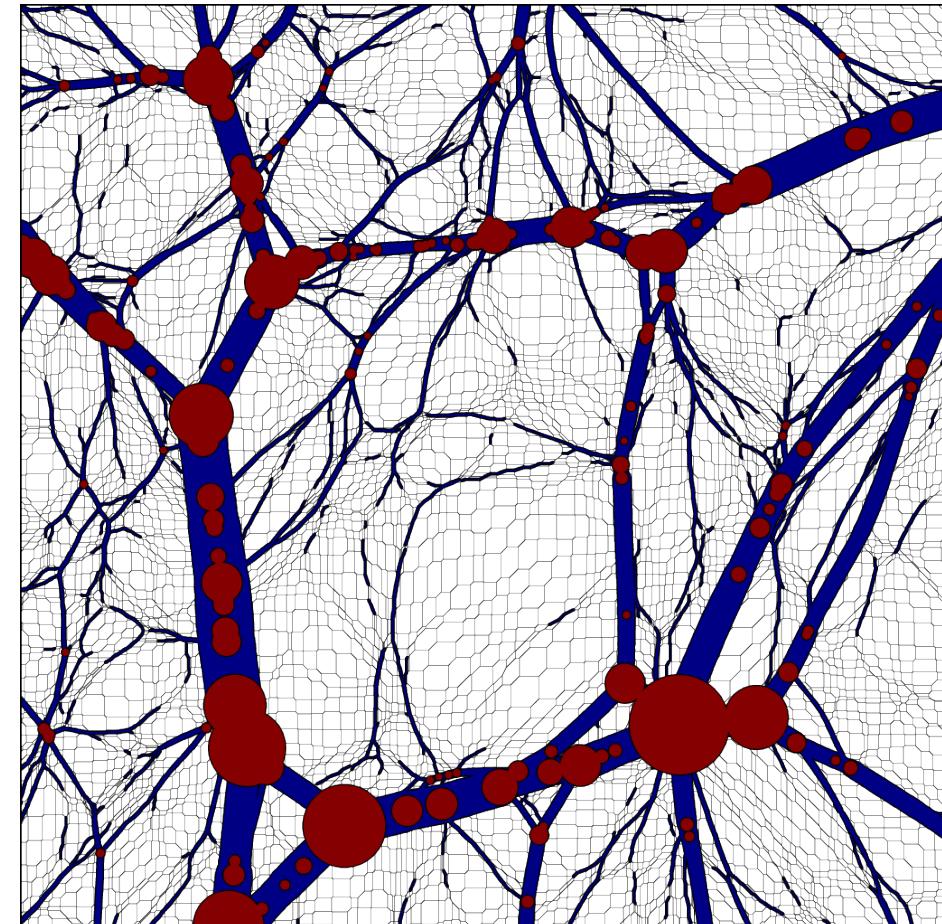
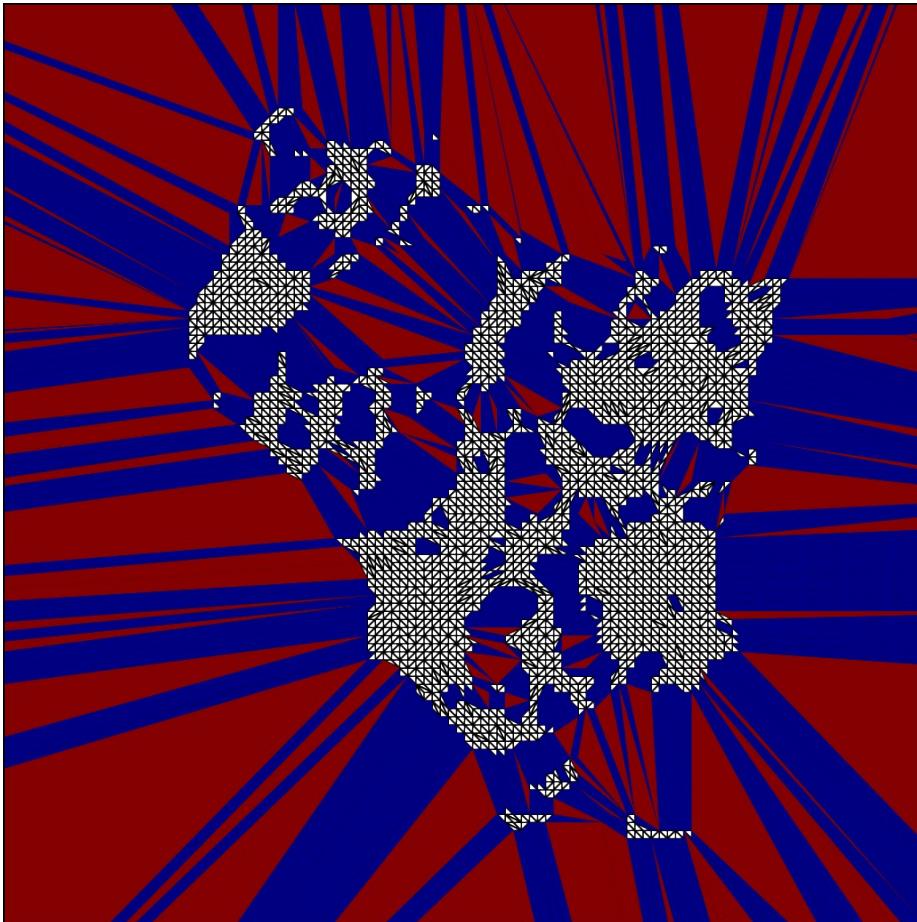
Adhesion



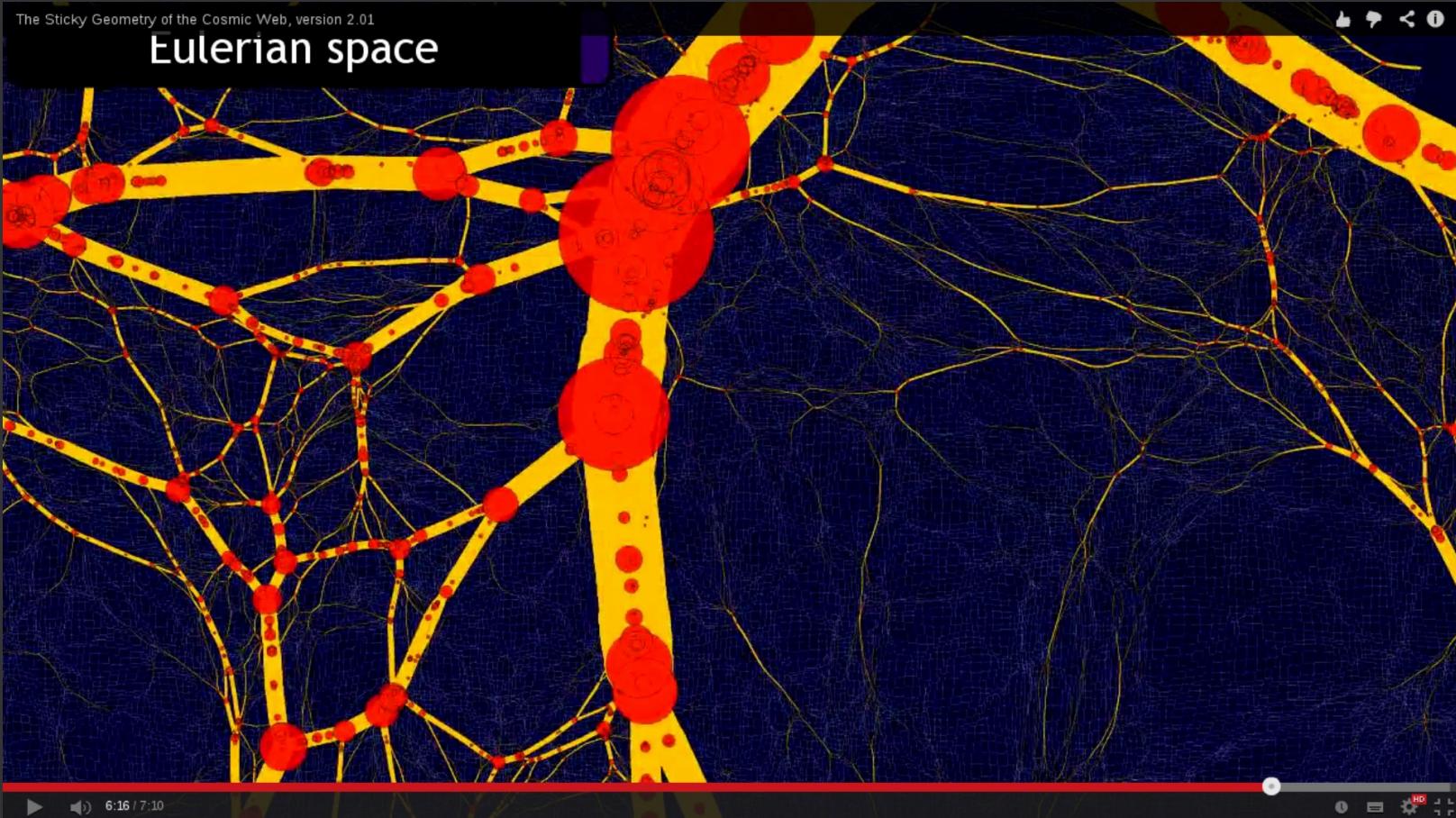
# Duality between Lagrangian and Eulerian space



# Duality between Lagrangian and Eulerian space

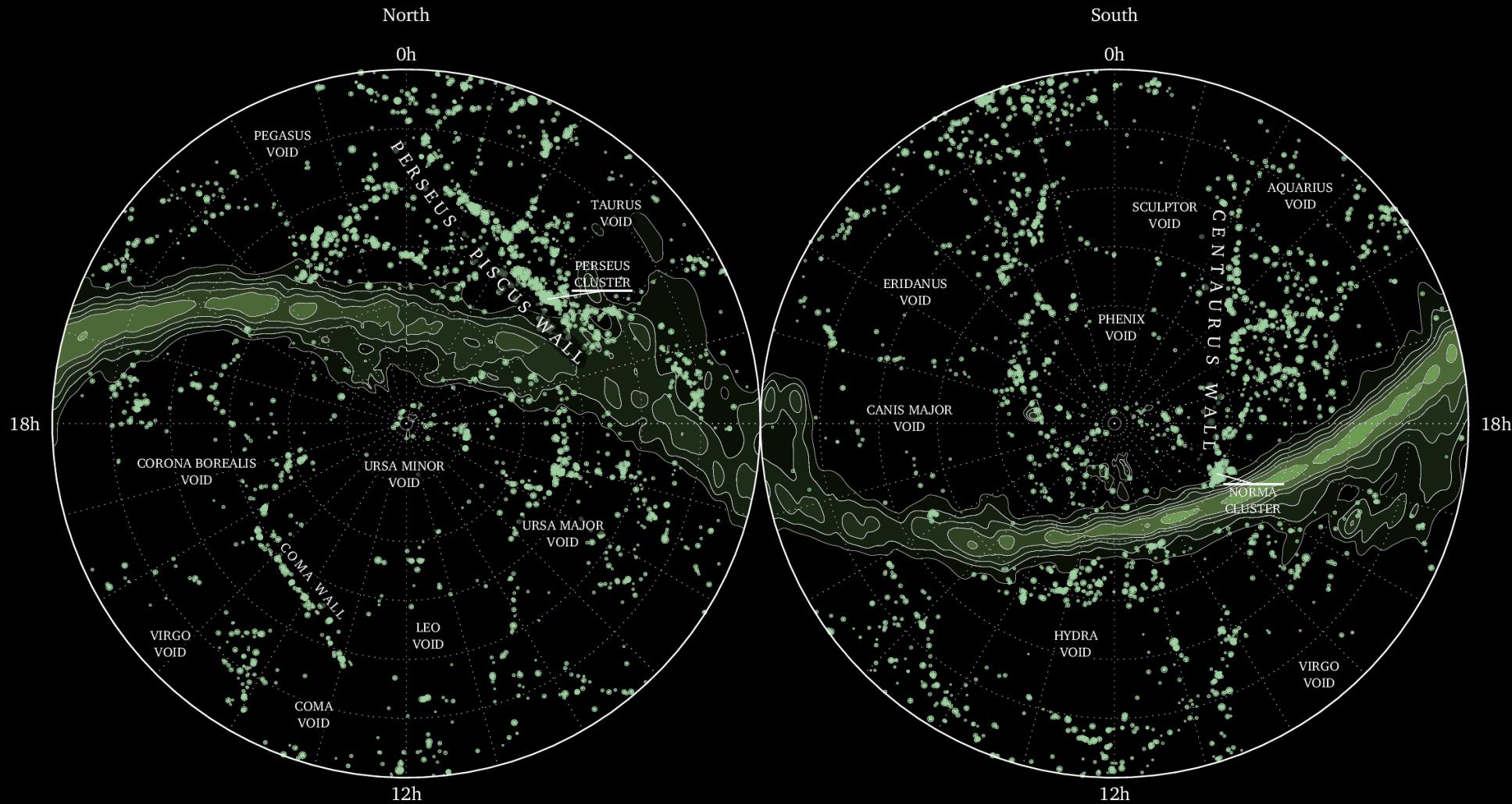


## Eulerian space



<http://youtu.be/wI12X2zcqI>  
(or search: Geometry of Cosmic Web)

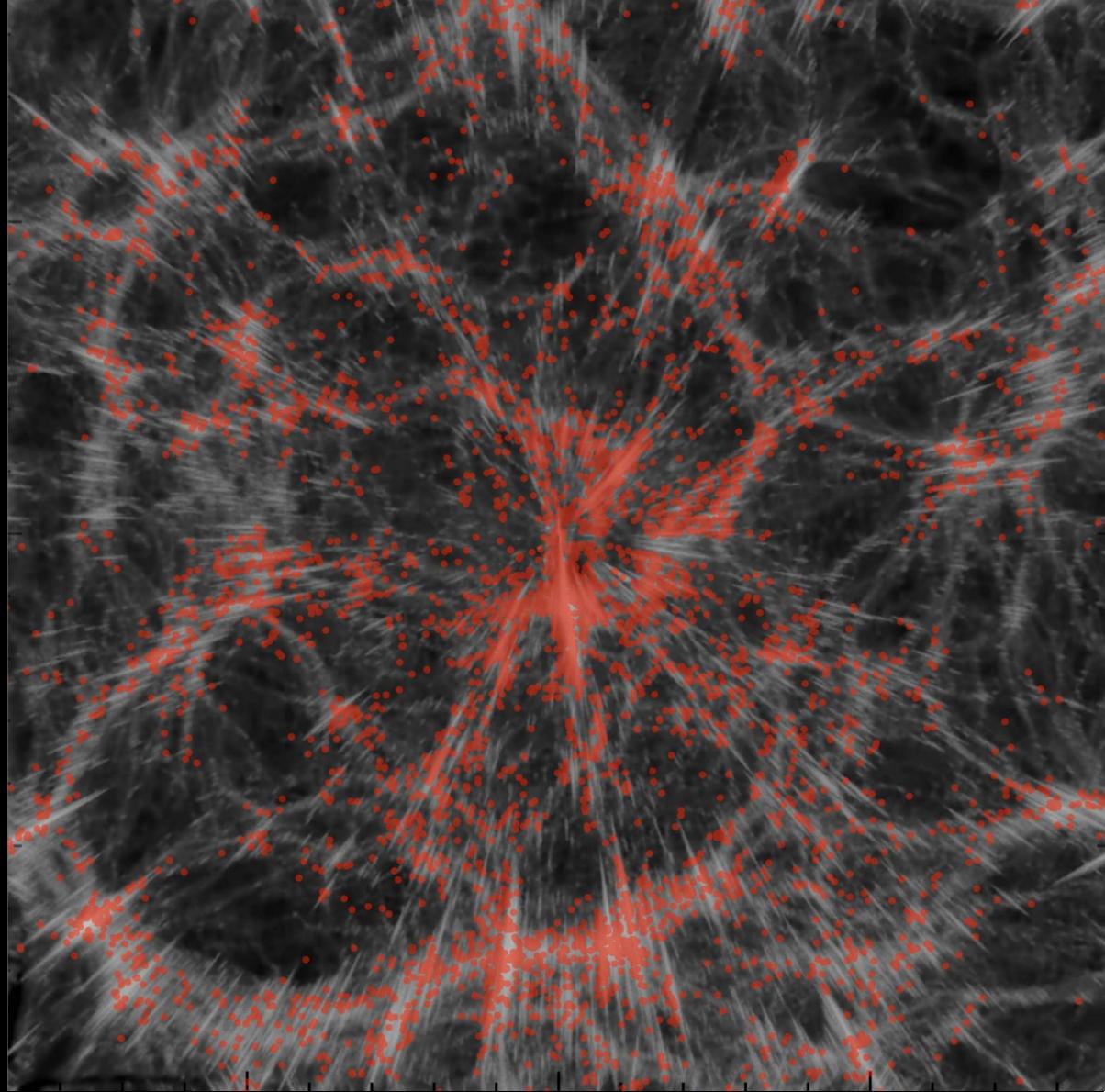
# 2MRS – Huchra et al. (2012)

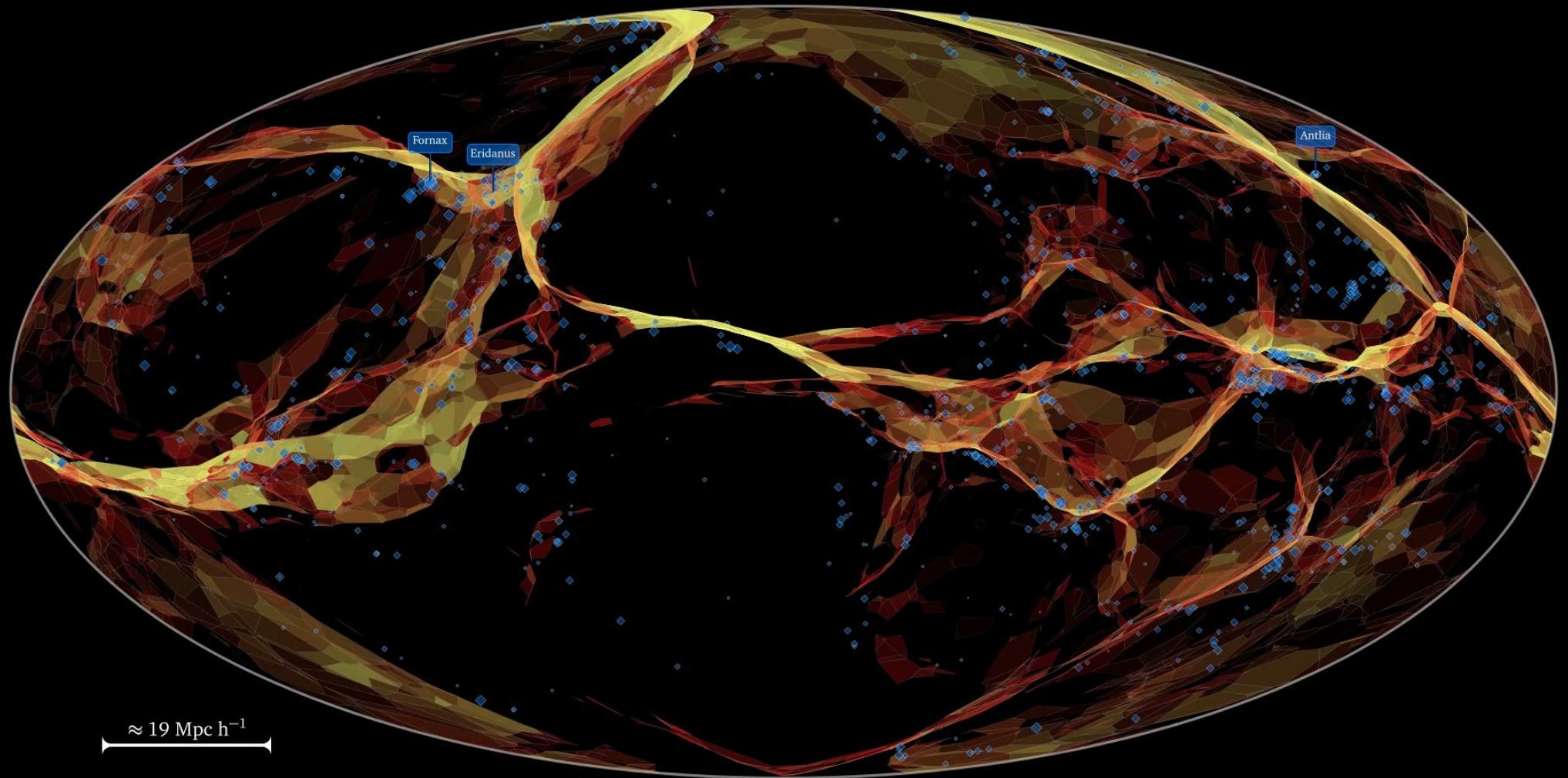


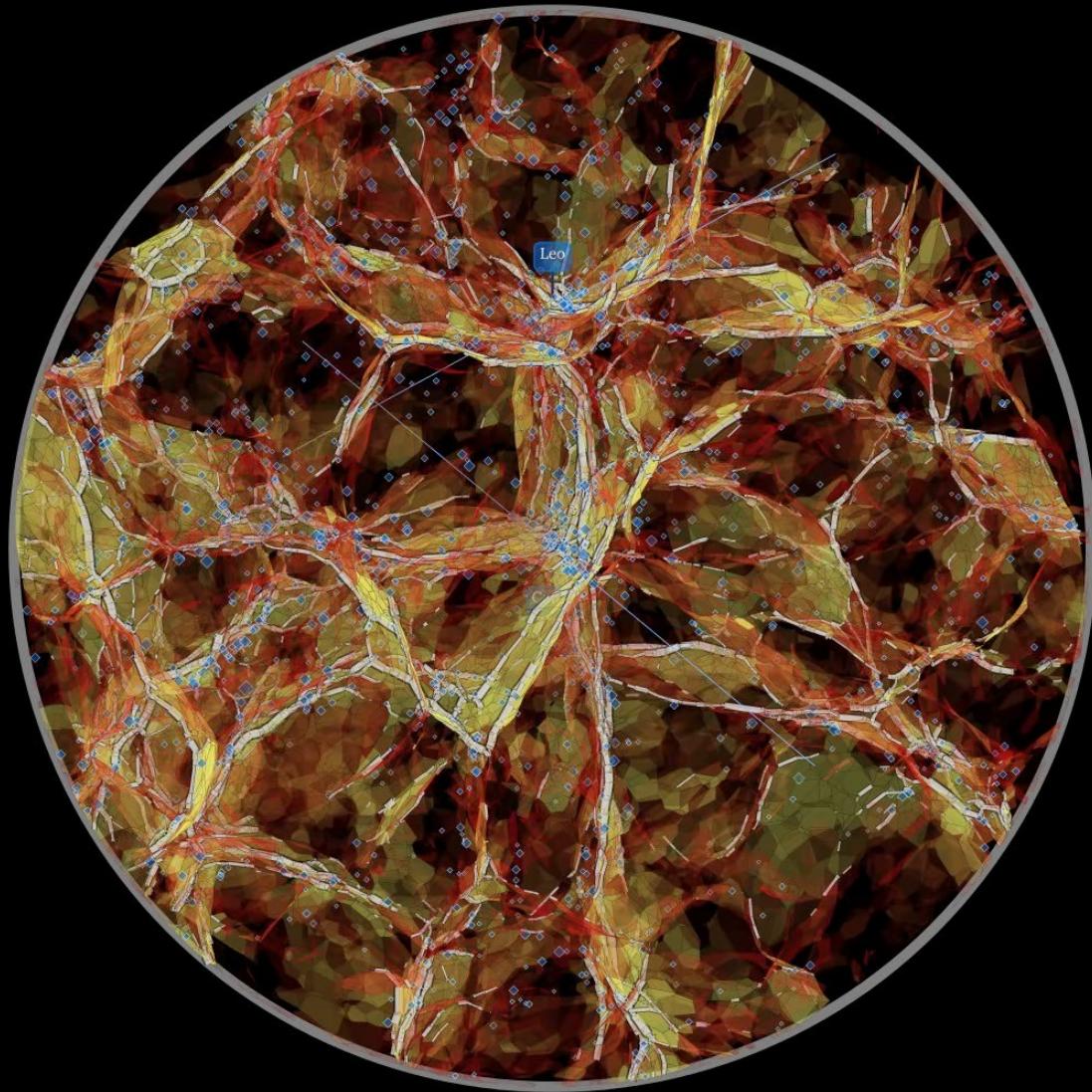
# Reconstruction

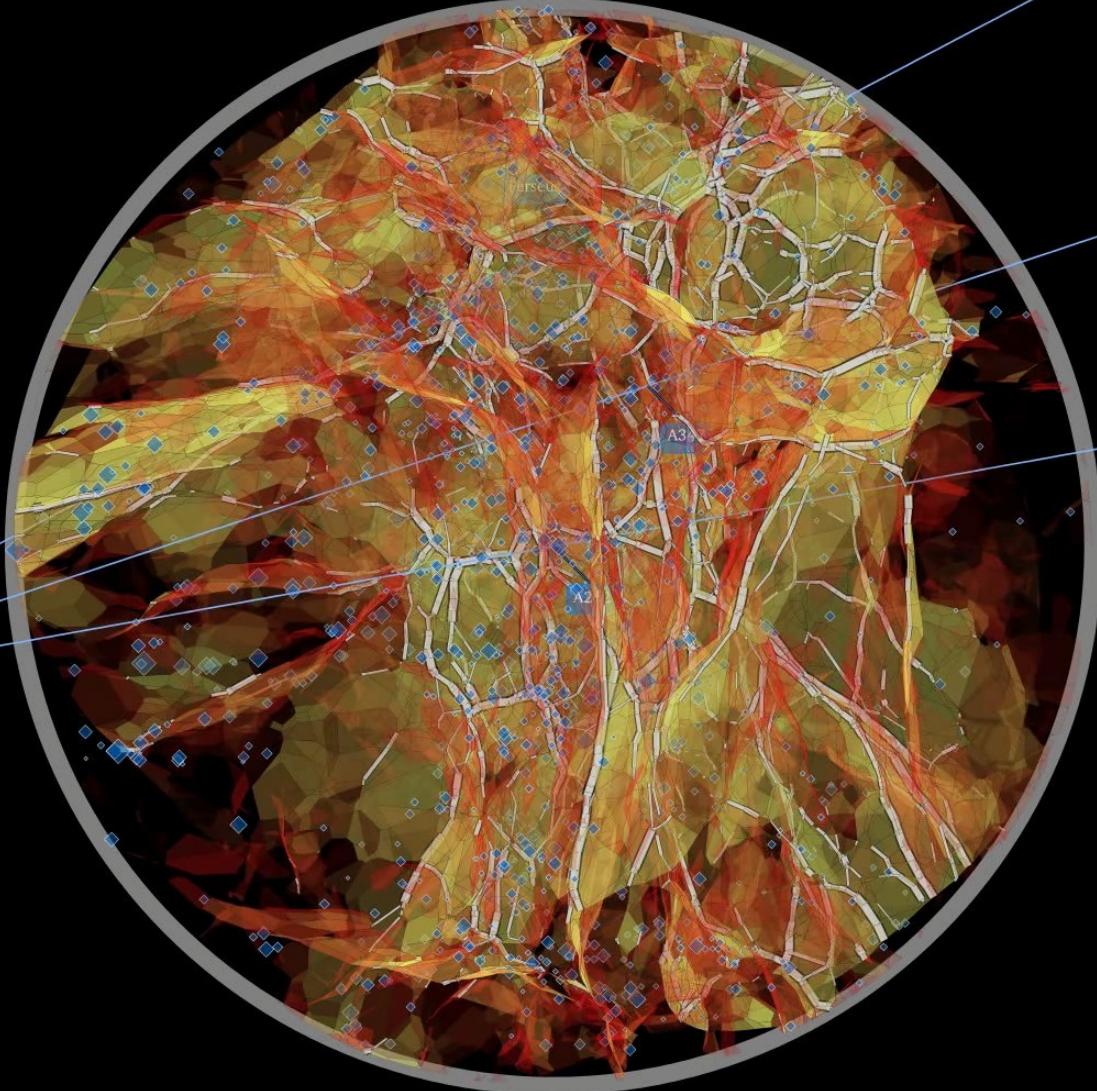
Kitaura & Enßlin (2008)

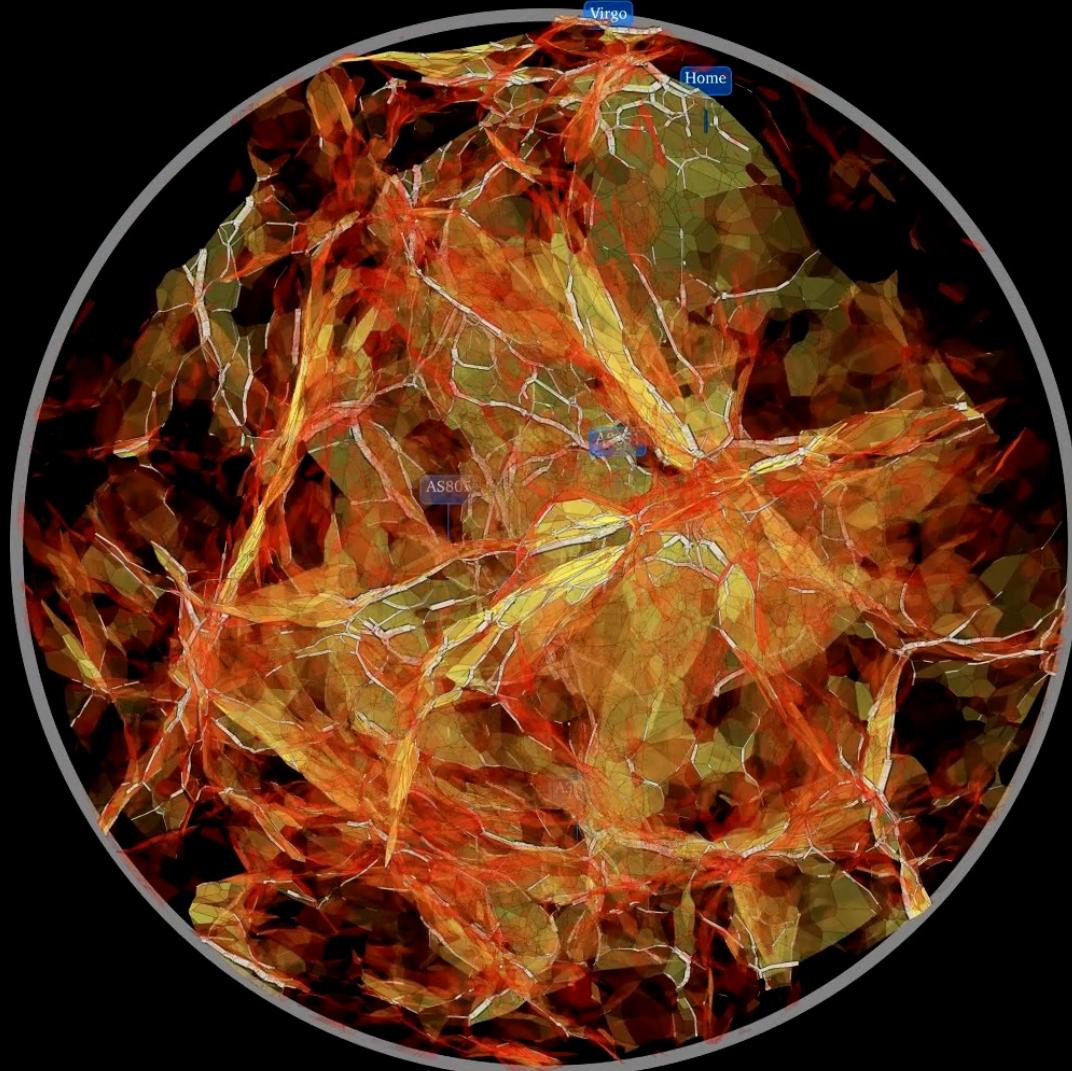
Heß, Kitaura & Gottloeber  
(arXiv:1304.6565)











Thanks!