



Yakob Zel'dovich (1914 – 1987)





Simulations of the cosmic web

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Ann. Phys. (Berlin) 524, No. 9–10, 507–534 (2012) / DOI 10.1002/andp.201200212

annalen
der **physik**

Dark matter and cosmic structure

Carlos S. Frenk^{1,*} and Simon D. M. White²

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The current standard model for the evolution of cosmic structure is reviewed, tracing its development over the last forty years and focussing specifically on the role played by numerical simulations and on aspects related to the nature of dark matter.

Attention is to provide an account of the main ideas and advances that have shaped the subject. We begin by presenting in Table 1 a chronological listing of the landmark developments that have driven this remarkable story.

2 Prehistory

In 1933 Zwicky published unambiguous evidence for dark matter in the Coma galaxy cluster [1]; in 1939 Bab-

1 Preamble

Review Article

Dark Matter

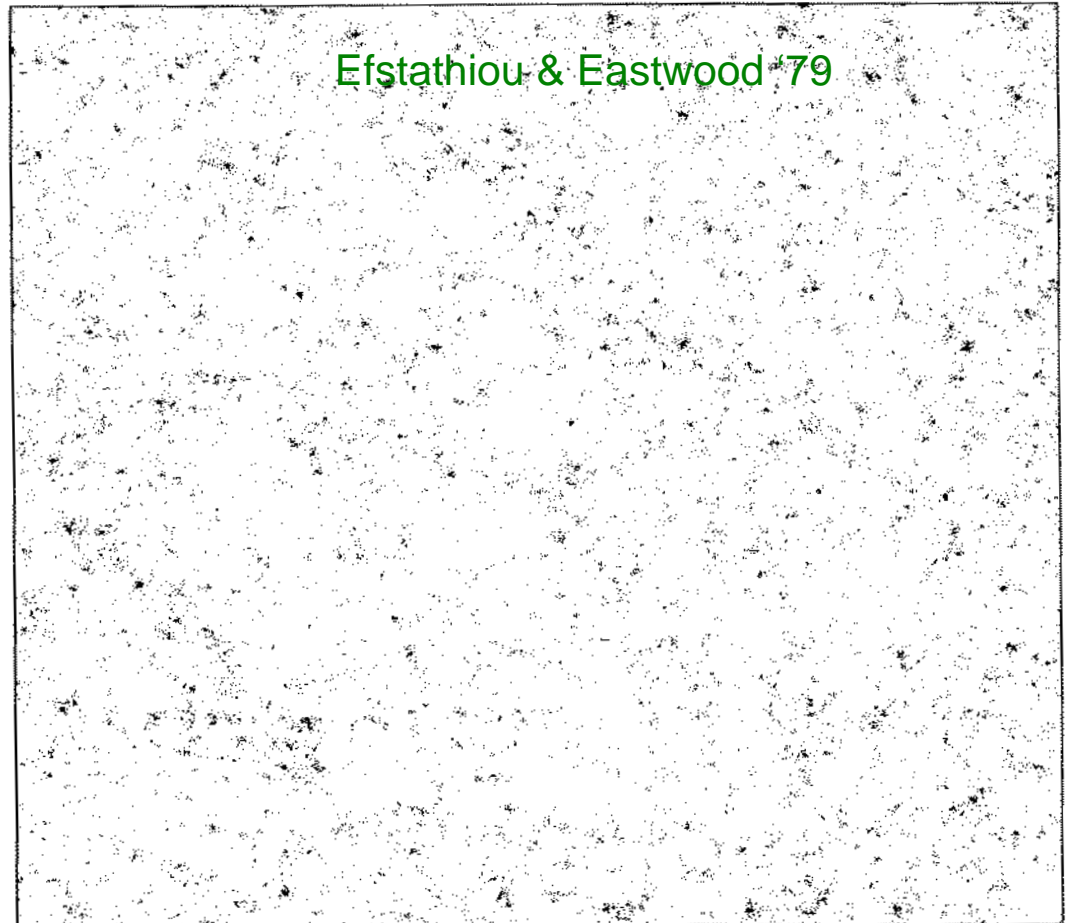
Edited by Matthias Bartel
and Volker Springel

$$|\delta_k|^2 \propto k^n \quad \Omega = 1$$

- Press & Schechter 1974 –
- Peebles & Groth 1976 –
- White 1976 – Coma cluster –
- Aarseth, Gott & Turner 1979 –
- Efstathiou & Eastwood 1979 –

Clustering of particles in an expanding Universe

51



The big Bang

Dark matter

Two revolutionary ideas were proposed in 1980

Cosmic inflation
→ initial conditions

- radiation
- particles
- heavy particles carrying the weak force
- quark
- anti-quark
- electron
- positron (anti-electron)
- proton
- neutron
- meson
- hydrogen
- deuterium
- helium
- lithium

15 thousand million years

1 thousand million years

300 thousand years

3 minutes

10^{-5} seconds

10^{-34} seconds

10^{-43} seconds

10^{32} degrees

degrees

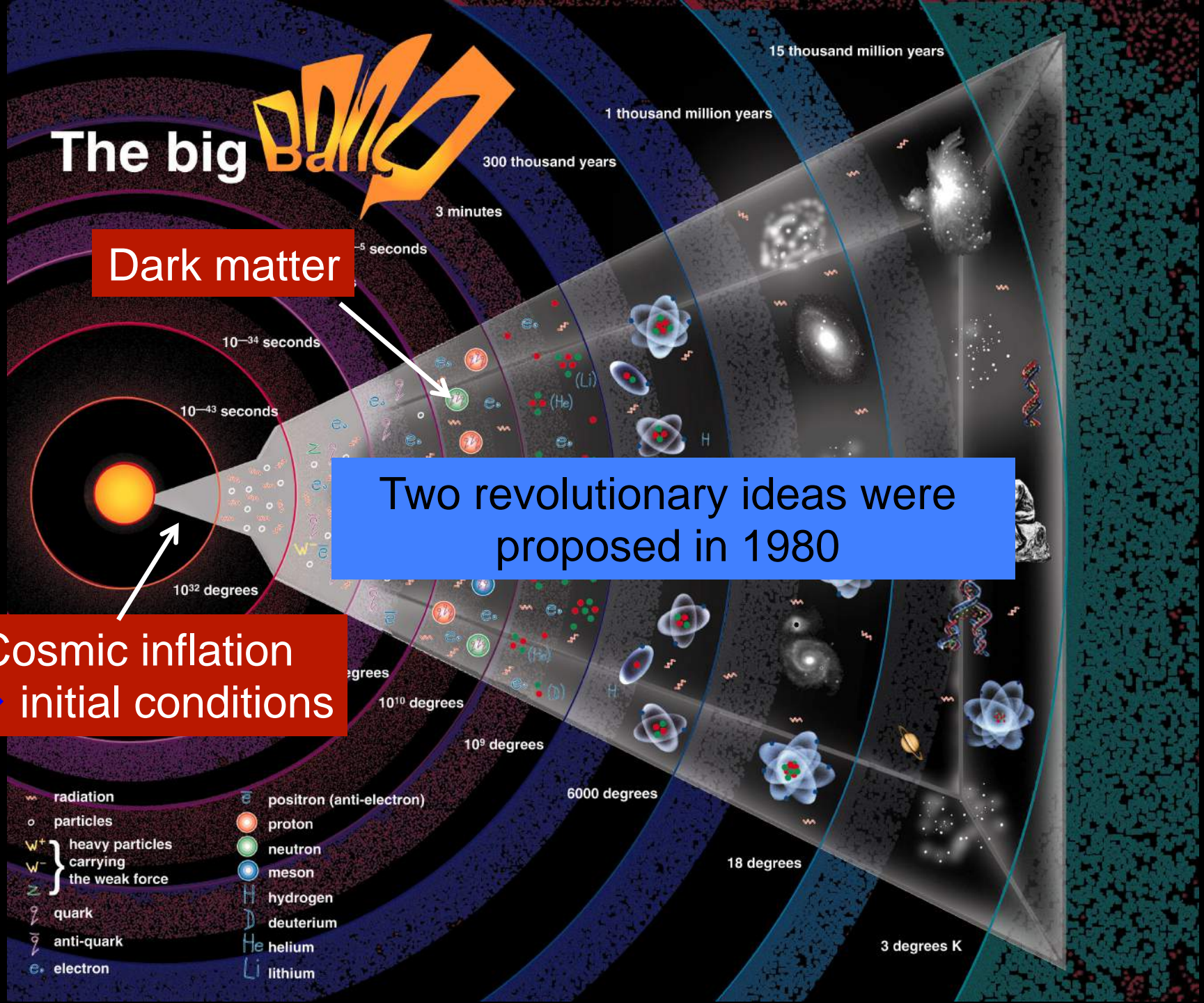
10^{10} degrees

10^9 degrees

6000 degrees

18 degrees

3 degrees K





For the first time in Cosmology → a well-defined theory of the initial conditions for the formation of cosmic structure

The dark matter power spectrum

$k^3 P(k)$

The linear power spectrum (“power per octave”)

Free streaming \rightarrow

$$\lambda_{\text{cut}} \propto m_x^{-1}$$

for thermal relic

$$m_{\text{CDM}} \sim 100 \text{ GeV}$$

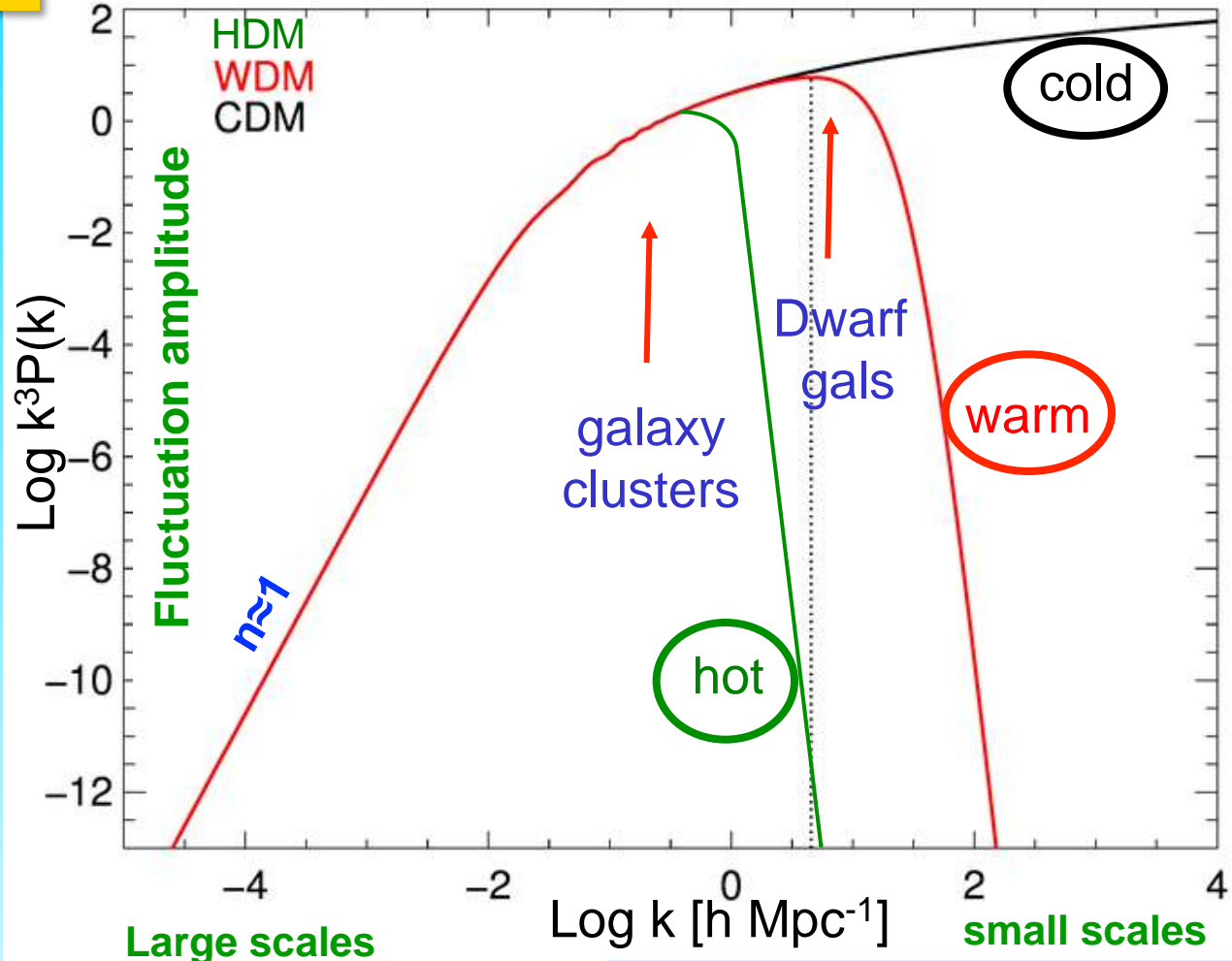
$$\text{susy}; M_{\text{cut}} \sim 10^{-6} M_{\odot}$$

$$m_{\text{WDM}} \sim \text{few keV}$$

$$\text{sterile } \nu; M_{\text{cut}} \sim 10^9 M_{\odot}$$

$$m_{\text{HDM}} \sim \text{few eV}$$

$$\text{light } \nu; M_{\text{cut}} \sim 10^{15} M_{\odot}$$



1981

HAS THE NEUTRINO A NON-ZERO REST MASS? (Tritium β -Spectrum Measurement)

V. Lubimov, E. Novikov, V. Nozik, E. Tretyakov
Institute for Theoretical and Experimental Physics, Moscow, U.S.S.R.

V. Kosik
Institute of Molecular Genetics, Moscow, U.S.S.R.

ABSTRACT

The high energy part of the β -spectrum of tritium in the molecule was measured with high precision by a toroidal β -spectrometer. The results give evidence for a non-zero electron anti-neutrino mass.

Fifty years ago Pauli introduced the neutrino to explain the β -spectrum shape. Pauli made the first estimate of the neutrino mass ($E_3 \text{ max} \approx \text{nuclei mass defect}$): it should be very small or maybe zero. Up to now the study of the β -spectrum shape is the most sensitive, direct method of neutrino mass measurement.

For allowed β -transitions, if $M_\nu = 0$, then $S = (E - E_0)^2$. The Kurie plot is then a straight line with the only kinematic parameter being $E_k = E_0$ (total β -transition energy). If $M_\nu \neq 0$, then $S = (E_0 - E) \sqrt{(E_0 - E)^2 - M_\nu^2}$. The Kurie plot is then distorted, especially near the endpoint.

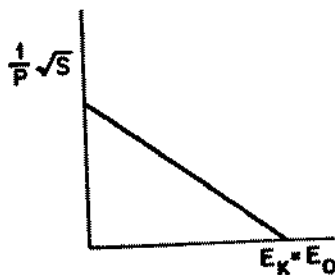


Fig. 1. Kurie plot for $M_\nu = 0$.

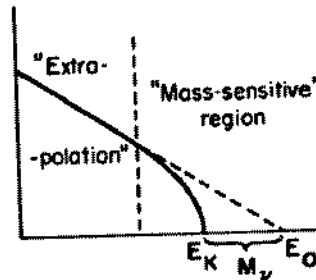


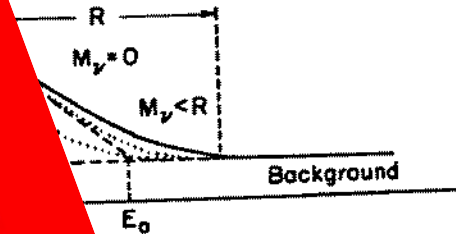
Fig. 2. Kurie plot for $M_\nu \neq 0$.

The method for the neutrino mass measurement is to obtain E_0 from the extrapolation and obtain E_k from the spectrum intercept. Then $M_\nu = E_0 - E_k$. Qualitatively, $M_\nu = 0$ if the β -spectrum near the endpoint runs below the extrapolated curve.

* Paper presented by Oleg Egorov.



things are more complicated. The apparatus resolution strongly affects the spectrum endpoint and rather the spectrum slope.



Realistic Kurie plot.

extrapolation. However, we are unable to determine M_ν , then once again the lack of counts near the endpoint indicate that $M_\nu \neq 0$. If $M_\nu \leq R$, the changes due to M_ν and the influence of R are indistinguishable. For $M_\nu > R$, the determination of the knowledge of R is compulsory. The background determines the statistical accuracy near the endpoint, i.e., in the region of the highest sensitivity to the ν mass. So: 1) R should be $\sim M_\nu$, 2) the smaller M_ν is, the smaller the background ($\sim M_\nu^2$) must be and the higher the statistics ($\sim M_\nu^3$) must be. For example, suppose that for $M_\nu = 100$ eV we need resolution R , background Q , and statistics N . If $M_\nu = 30$ eV, to achieve the same $\Delta M/M$ they should be $R/3$, $Q/10$, and $N \times 30$, respectively.

The shorter the β -spectrum, the less it is spread due to R (as $R \sim \Delta p/p = \text{const.}$). A classical example is ^3H β -decay, which has 1) the smallest $E_0 \sim 18.6$ keV, 2) an allowed β -transition, simple nucleus, and simple theoretical interpretation, 3) highly reduced radioactivity. The first experiments with ^3H were by S. Curran et al. (1948) and G. Hanna, B. Pontecorvo (1949). Using ^3H gas in a proportional counter, they obtained $M_\nu \leq 1$ keV. Further progress required magnetic spectrometer development. This allowed the resolution to be improved considerably, and L. Langer and R. Moffat (1952) obtained $M_\nu \leq 250$ eV. The best value was obtained by K. Bergkvist (1972): $R \sim 50$ eV and $M_\nu \leq 55$ eV.

The ITEP spectrometer is of a new type: ironless, with toroidal magnetic field (E. Tretyakov, 1973). The principle of the toroidal magnetic field focusing systems was proposed by V. Vladimirovsky et al. (An example is a "Horn" of ν -beams.) It turns out that a rectilinear conductor (current) has a focusing ability for particles emitted perpendicular to the rotation axis. This system has infinite periodical focusing structure. The ITEP spectrometer is based on this principle.

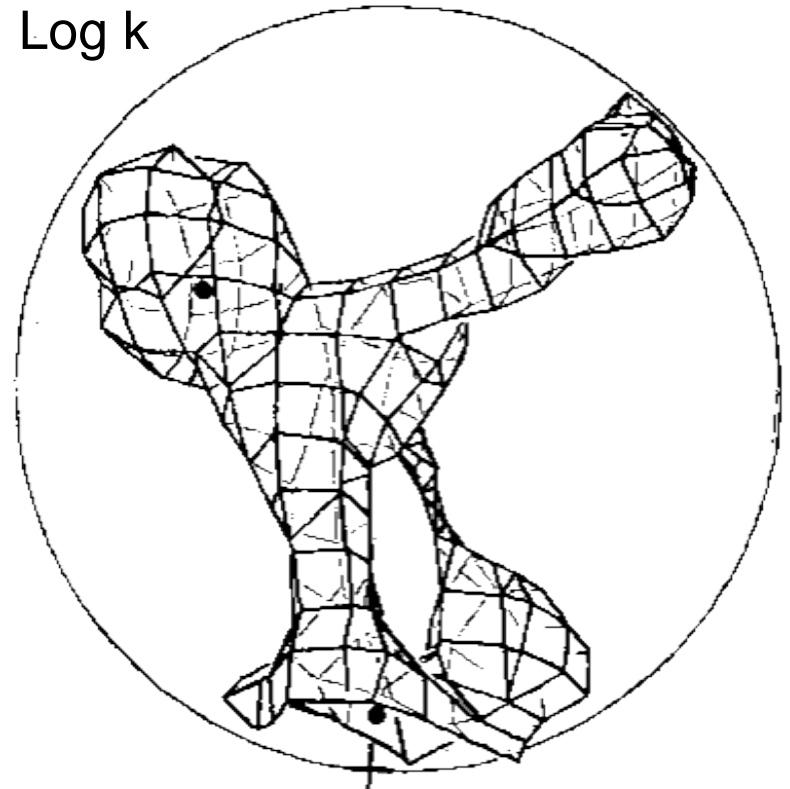
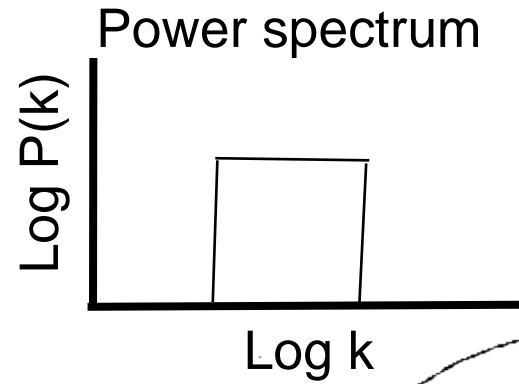
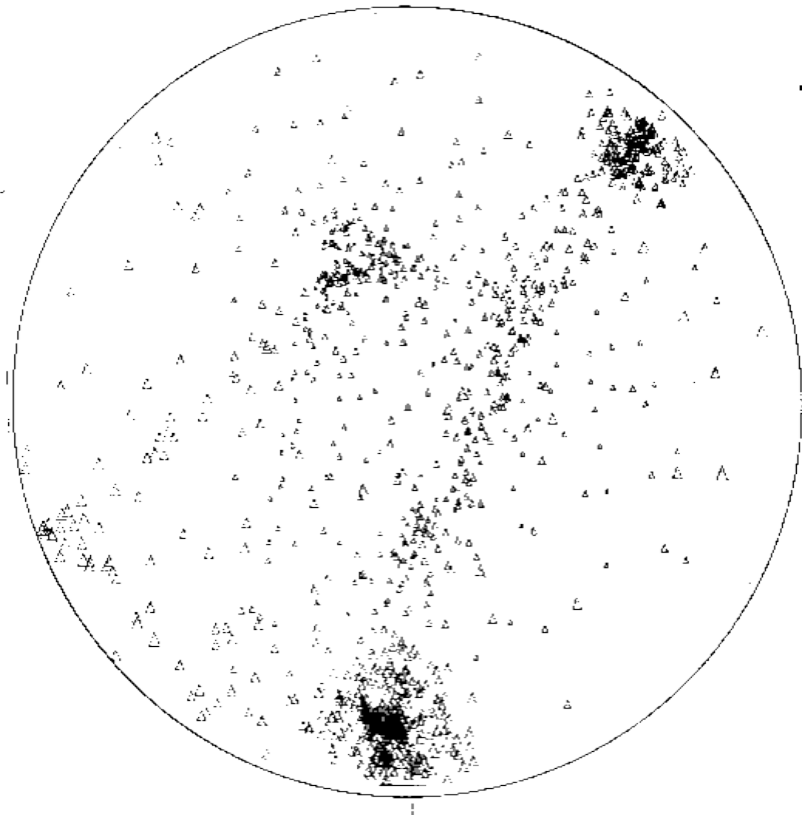
Mon. Not. R. astr. Soc. (1983) **204**, 891--907

Three-dimensional numerical model of the formation of large-scale structure in the Universe

A. A. Klypin and S. F. Shandarin *The Keldysh Institute of Applied Mathematics, Academy of Sciences of USSR, Miusskaja Sq. 4, Moscow 125047, USSR*

Received 1982 November 15; in original form 1982 April 28

“Pancake” model



Klypin & Shandarin 1983

THE ASTROPHYSICAL JOURNAL, 271:417–430, 1983 August 15

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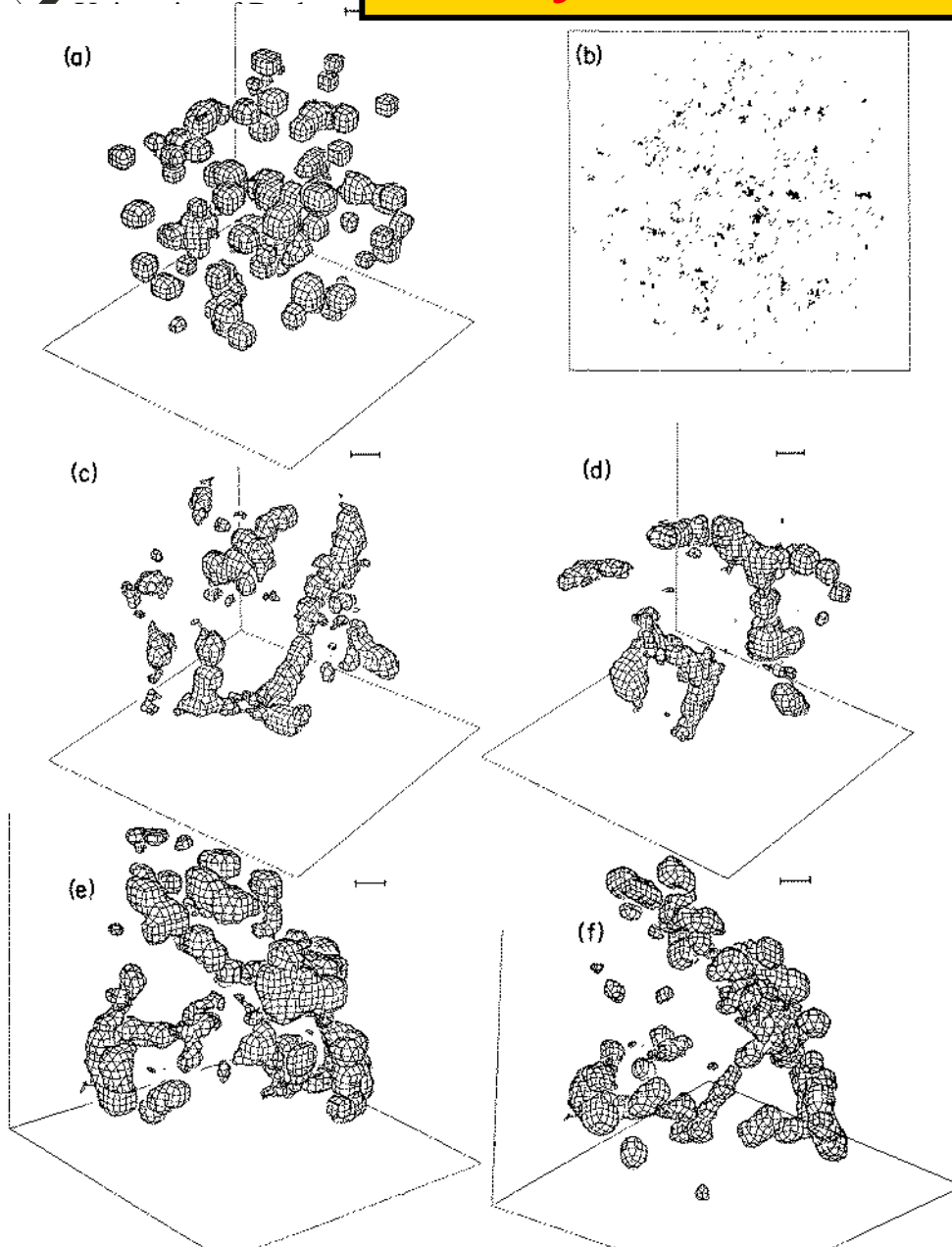
NONLINEAR EVOLUTION OF LARGE-SCALE STRUCTURE IN THE UNIVERSE

CARLOS S. FRENK,¹ SIMON D. M. WHITE,^{1,2} AND MARC DAVIS^{1,3}

University of California, Berkeley

Received 1982 November 4; accepted 1983 January 27

Early cosmological simulations



“Poisson” models ($n=0$)

“Pancake” models (neutrinos)

CfA redshift survey

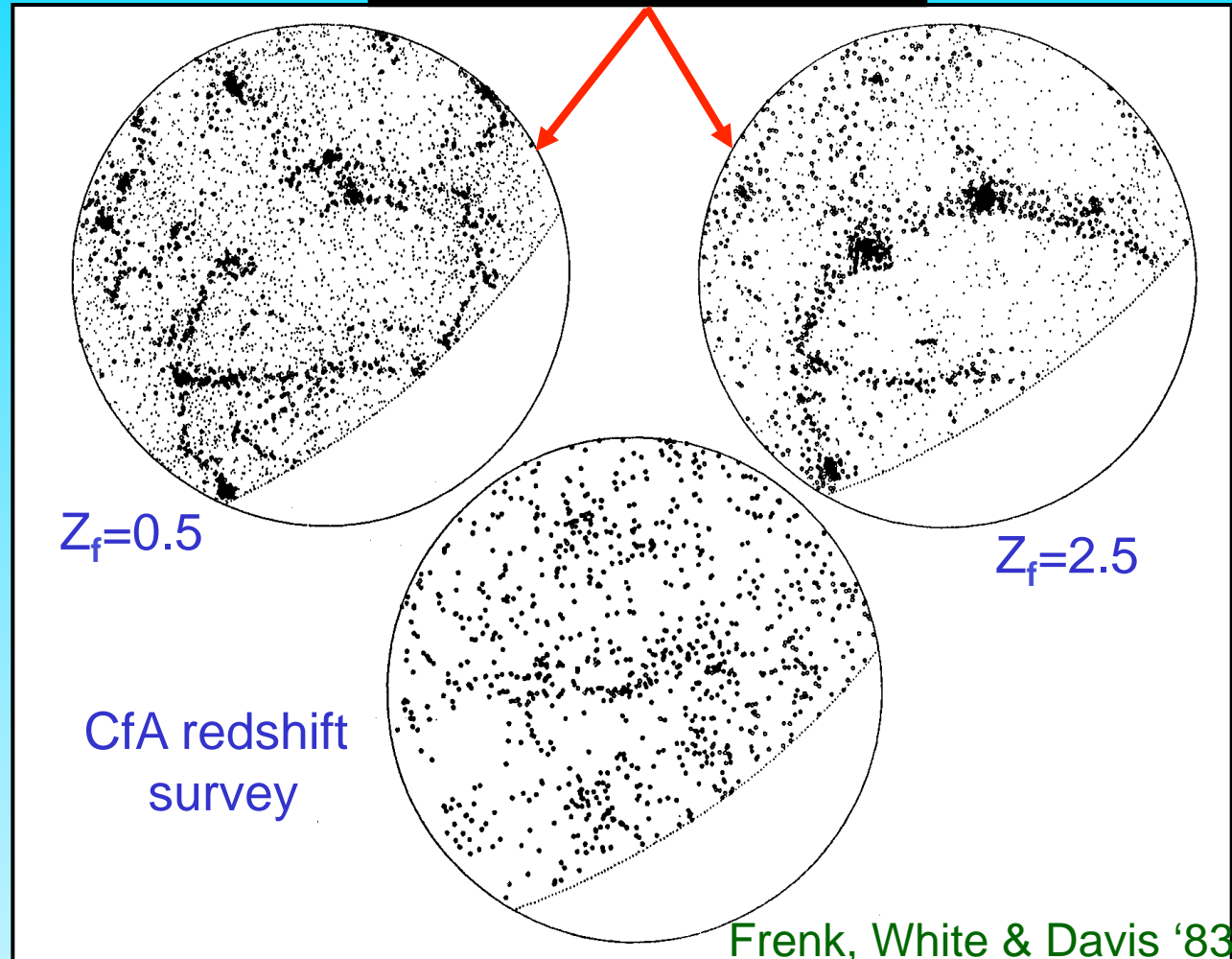
Neutrino (hot) dark matter

$$\Omega_{\nu}=1 \quad (m_{\nu} = 30 \text{ eV})$$

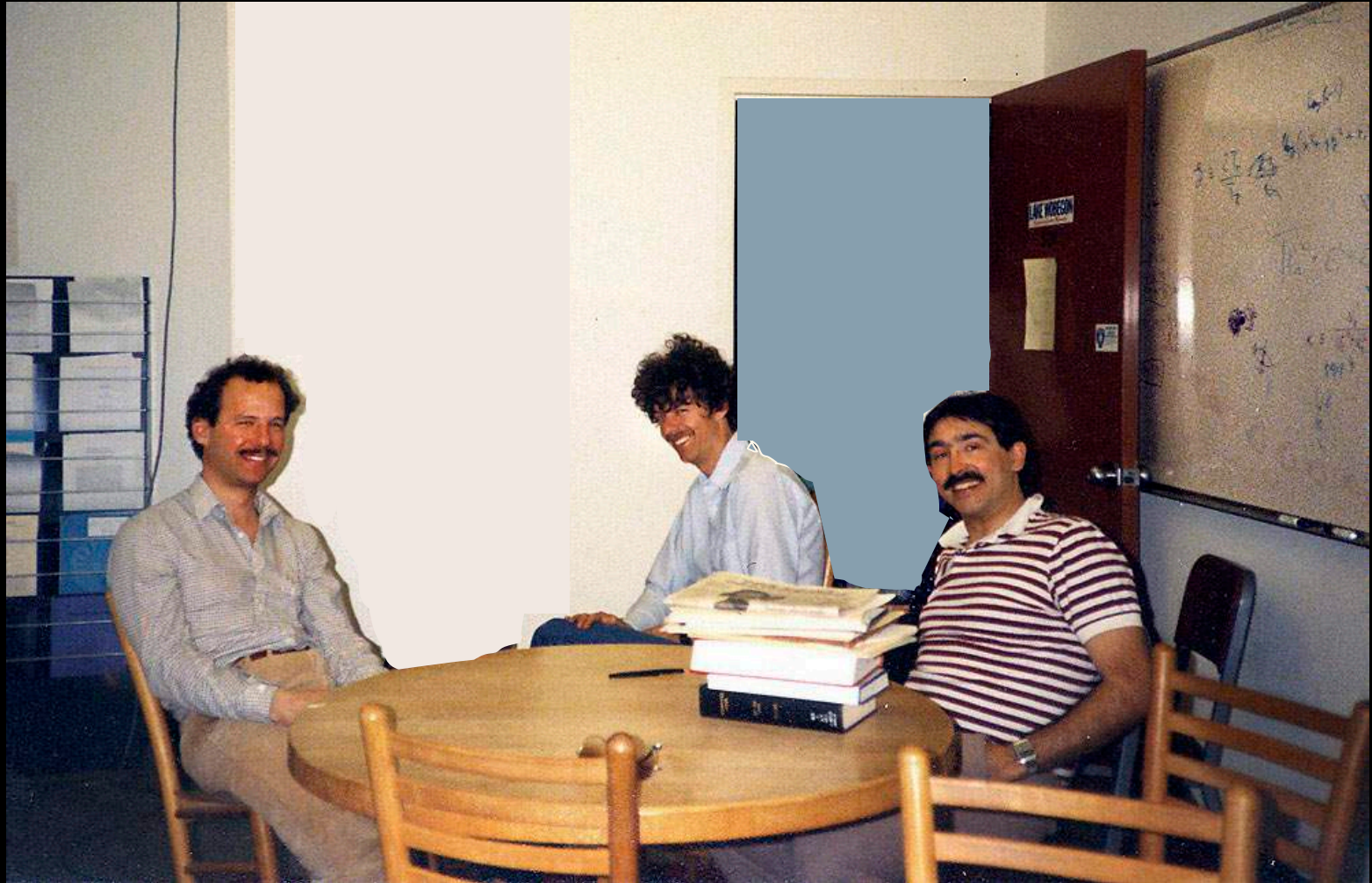
Free-streaming length so large that superclusters form first and galaxies are too young



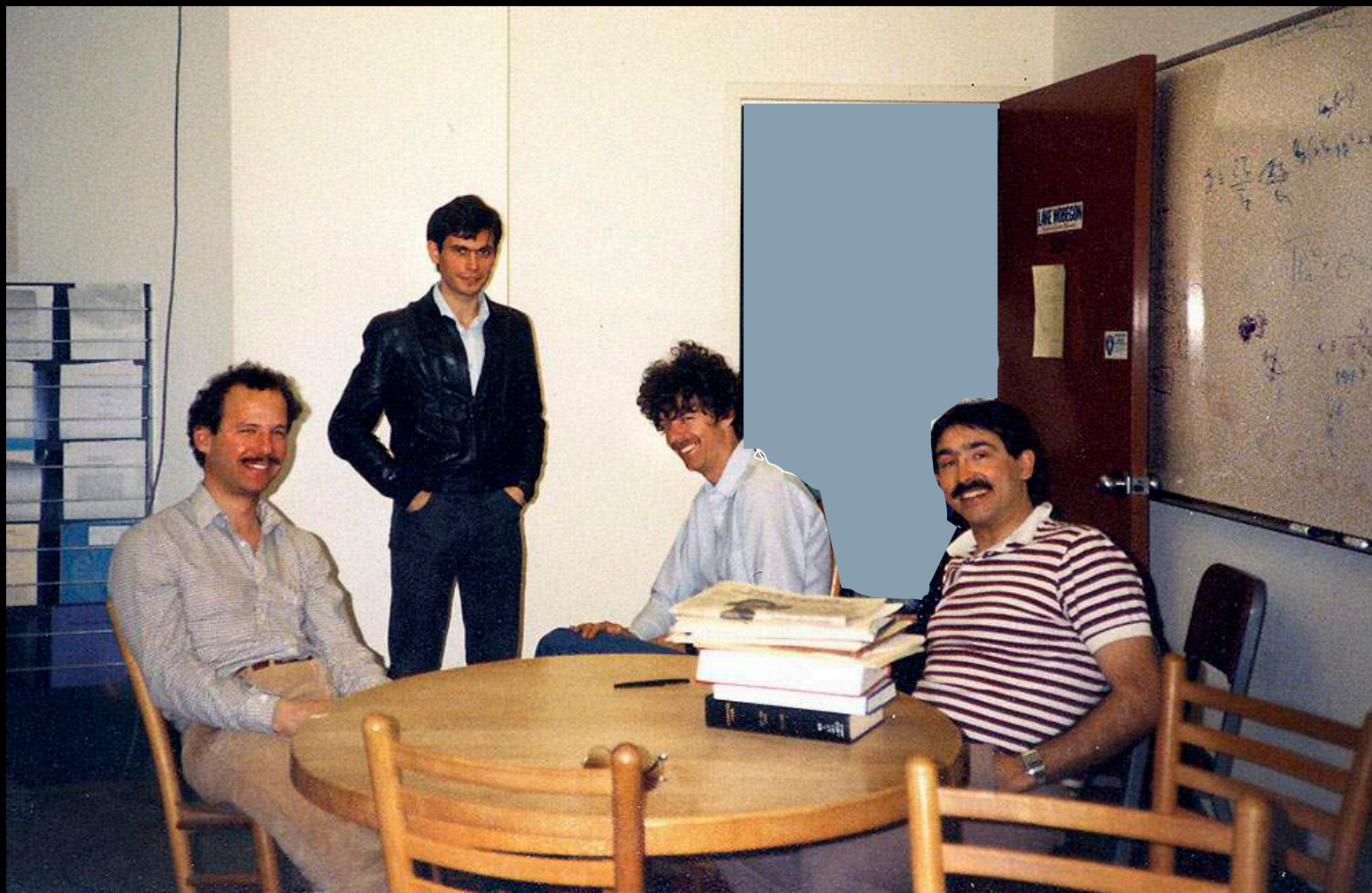
Neutrinos cannot make an appreciable contribution to Ω and $m_{\nu} \ll 10 \text{ eV}$



Frenk, White & Davis '83



The 'Gang of Four' - 1983



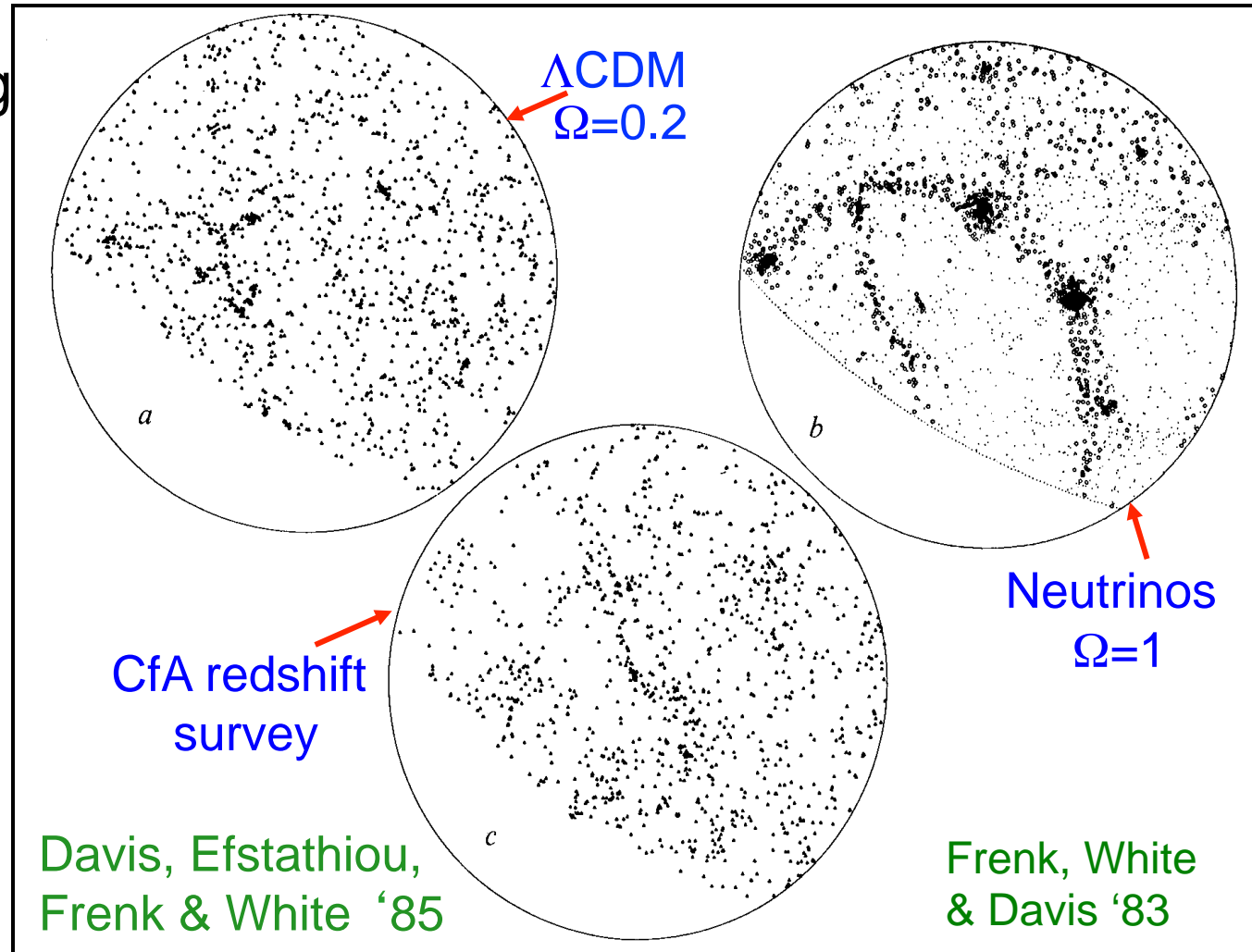
Non-baryonic dark matter cosmologies

Neutrino DM \rightarrow
unrealistic clust'ing

Neutrinos cannot
make appreciable
contribution to Ω
 $\rightarrow m_\nu \ll 10$ eV

Early CDM N-body
simulations gave
promising results

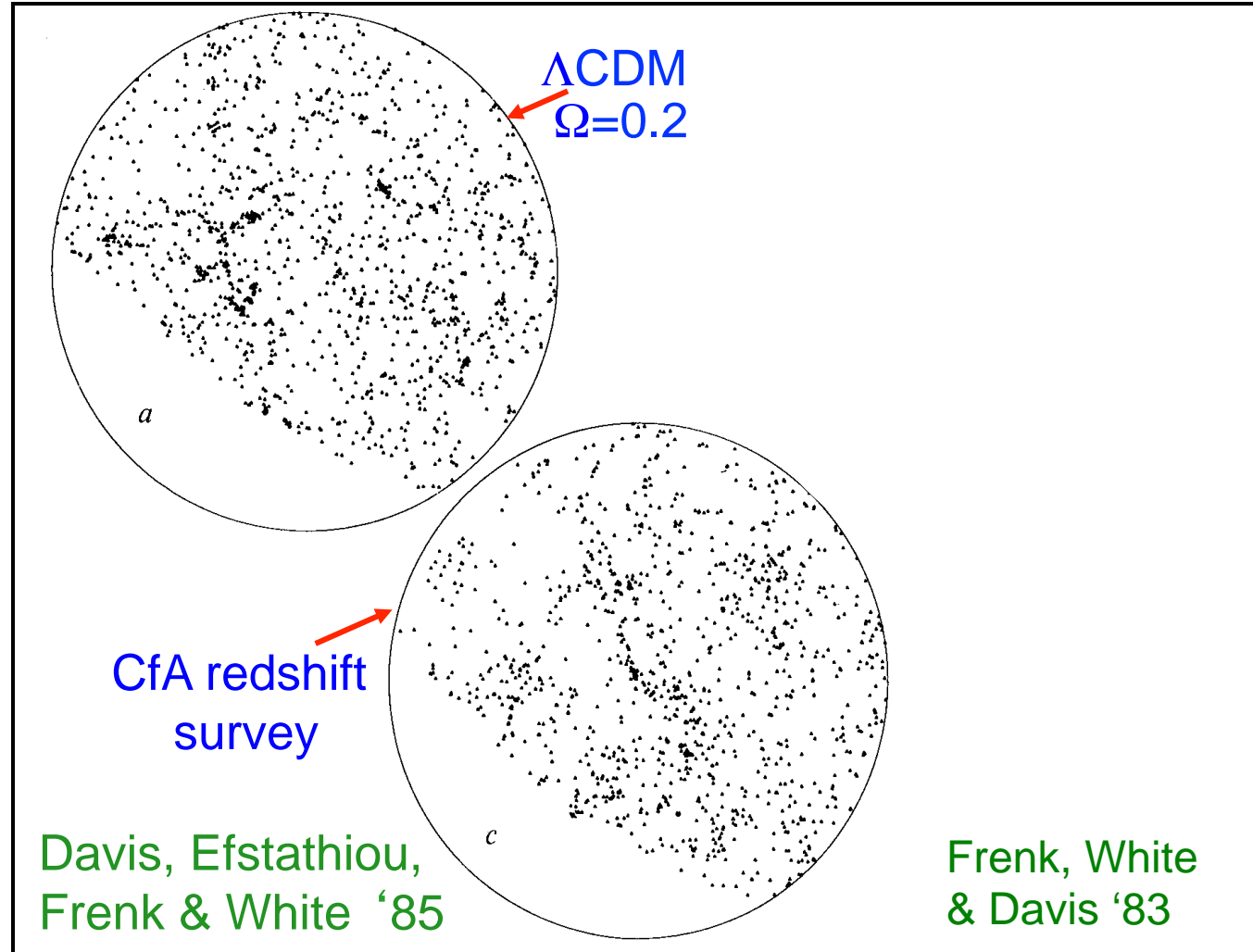
In CDM structure
forms hierarchically



Non-baryonic dark matter cosmologies

Λ was
inconceivable in
1985

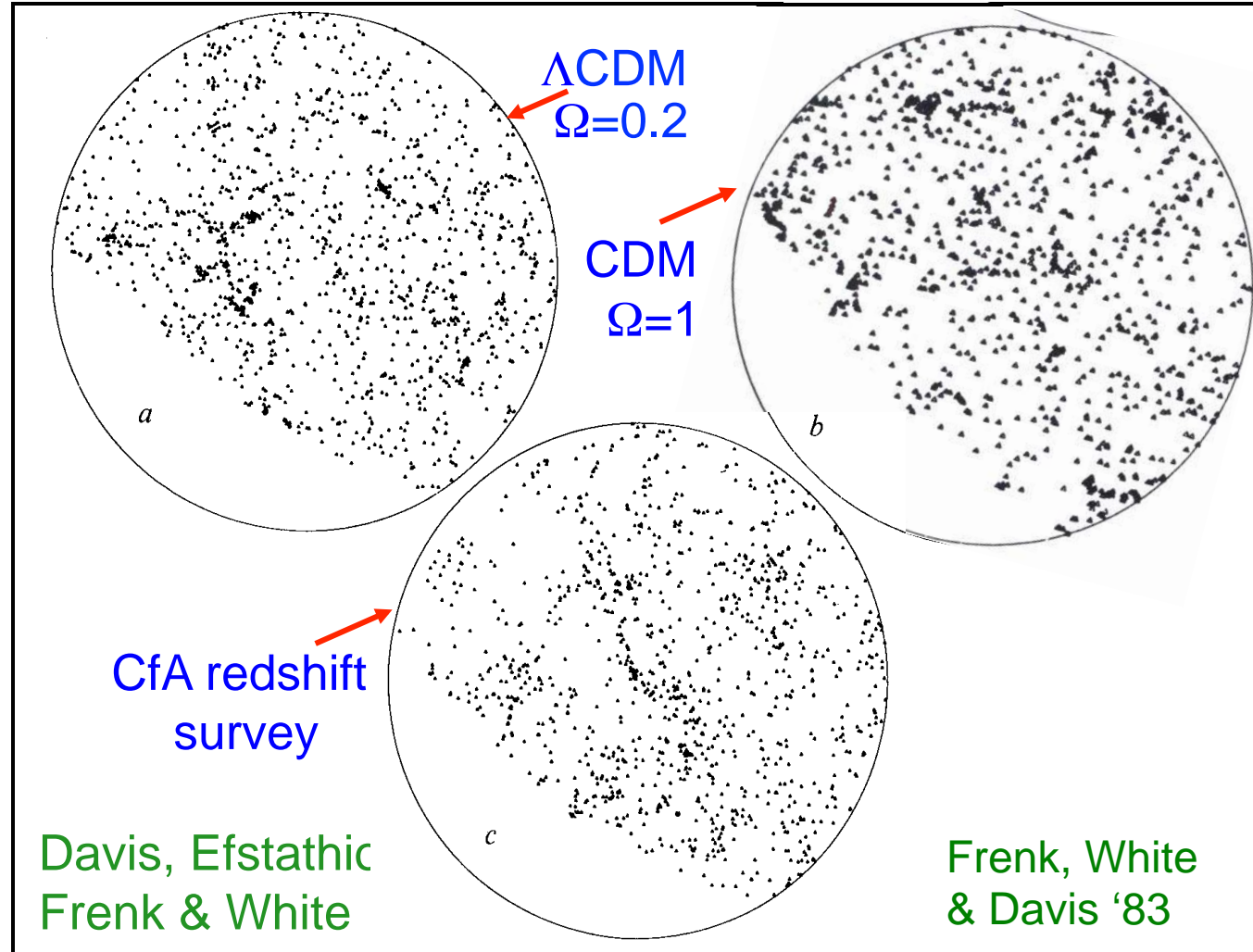
How can we make
 $\Omega=1$ give
acceptable
clustering?



Non-baryonic dark matter cosmologies

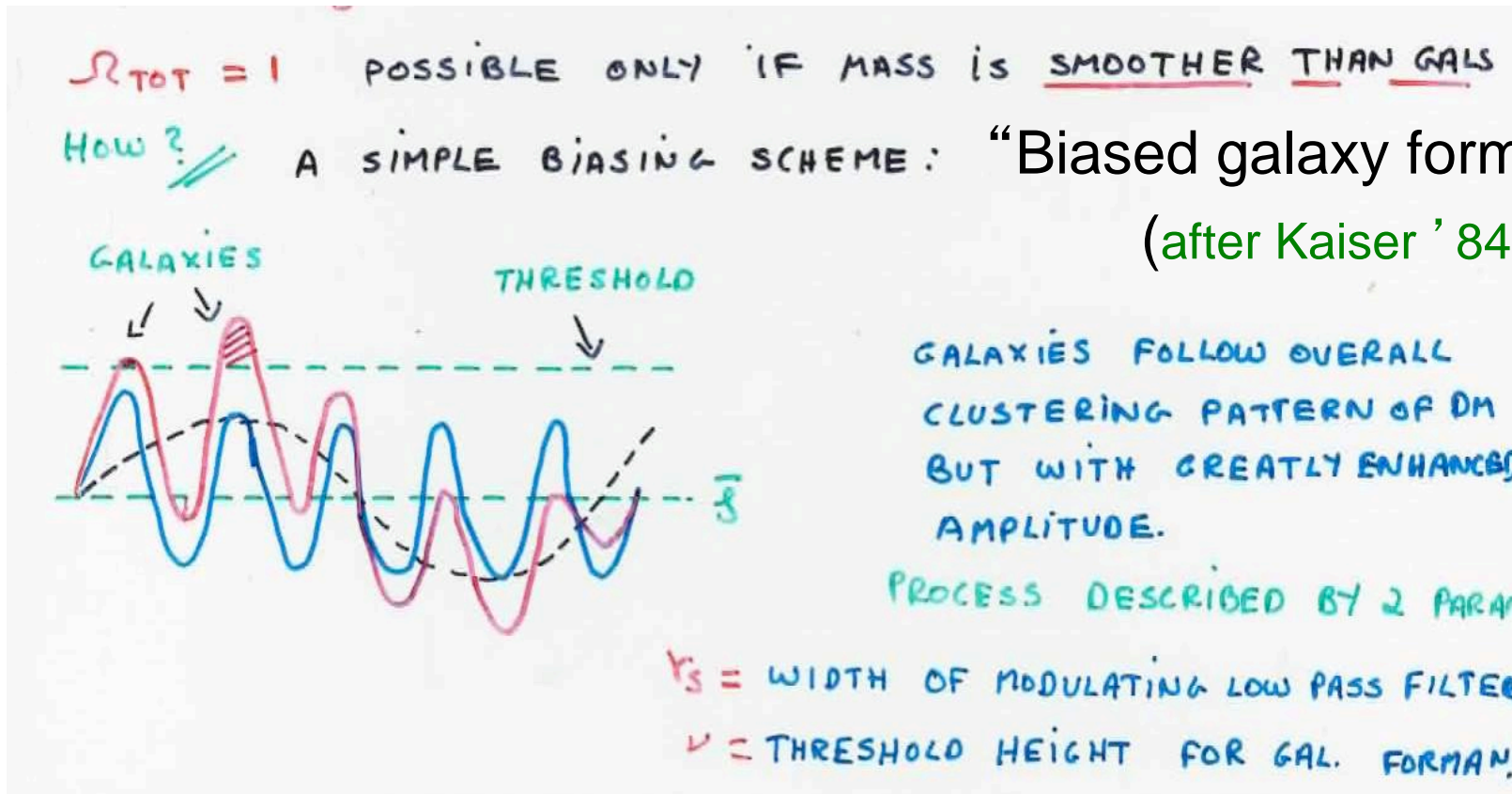
Λ was
inconceivable in
1985

How can we make
 $\Omega=1$ give
acceptable
clustering?



If galaxies trace mass, right clustering \rightarrow too large pec. velocities!

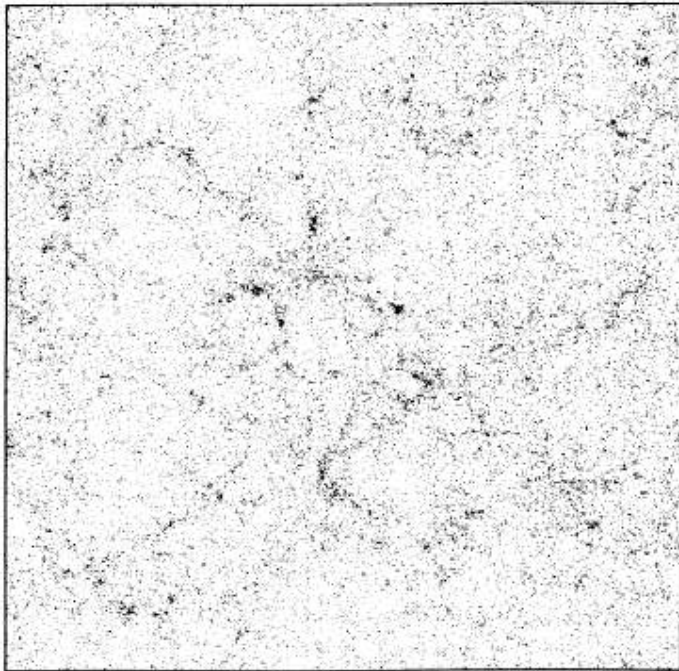
Dark matter



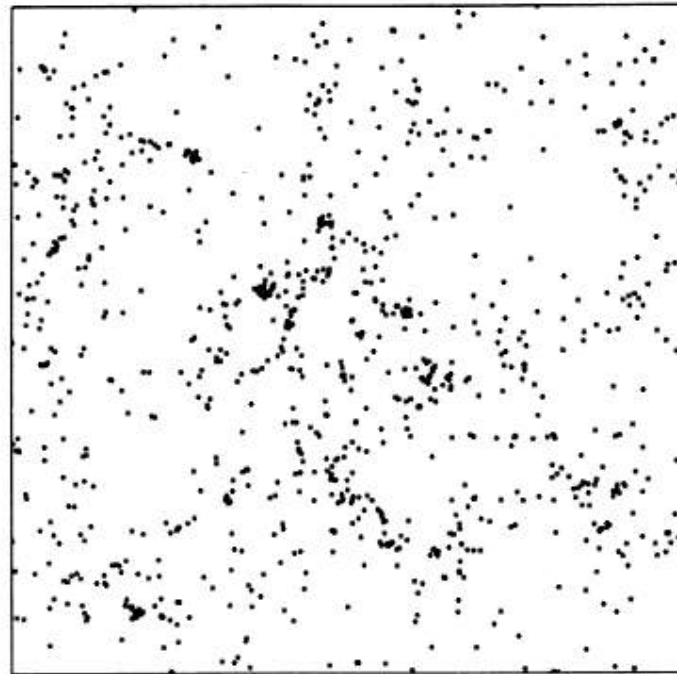
Biased galaxy formation

... or how to rescue $\Omega=1$! DEFW '85

Dark matter



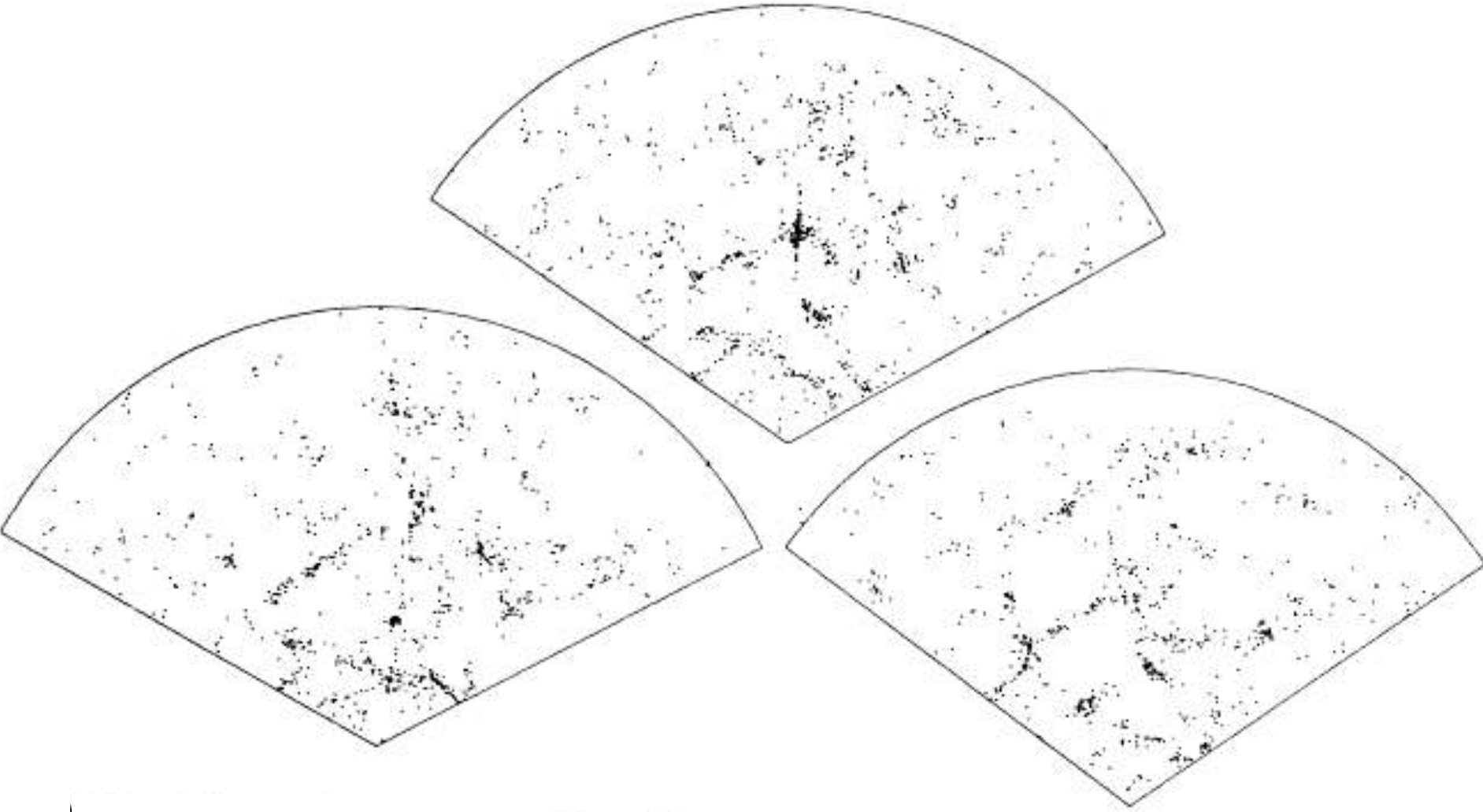
Galaxies



Gals \rightarrow peaks
of density
field

FIG. 16.—The projected distribution of all particles (*left*) and of the “galaxies” (*right*) in EdS1 at $a = 1.4$. The side of the box is $32.5h^{-1}$ Mpc. “Galaxies” are assumed to form only at the 2.5σ peaks of the linear density distribution.

SCDM compared to CfA-2 z-survey

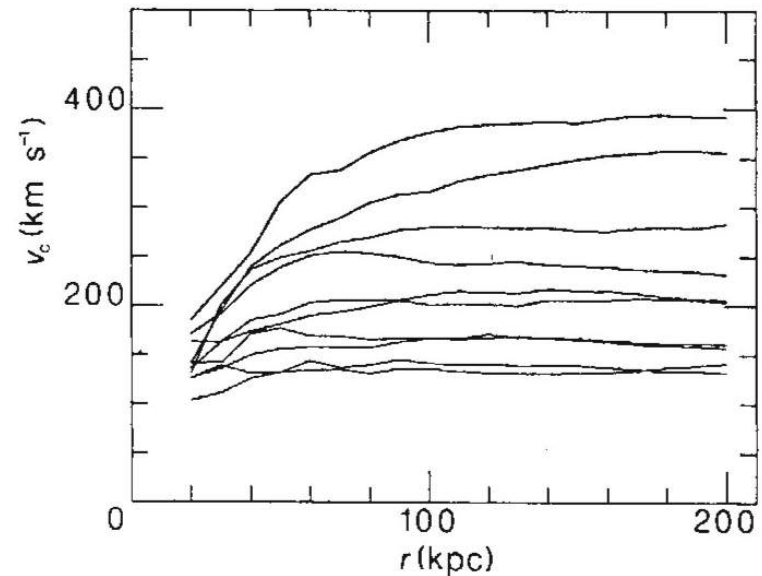


White, Frenk, Davis, Efstathiou '87

Cold dark matter, the structure of galactic haloes and the origin of the Hubble sequence

Carlos S. Frenk*, Simon D. M. White†, George Efstathiou‡ & Marc Davis§

A popular theory for galaxy formation holds that the Universe is dominated by exotic particles such as axions, photinos or gravitinos (collectively known as cold dark matter, CDM)¹⁻³. This hypothesis can reconcile the aesthetically pleasing idea of a flat universe with the standard theory of primordial nucleosynthesis and with upper limits on anisotropies in the cosmic microwave background⁴⁻⁶. The resulting model is consistent with the observed dynamics of galaxy clustering only if galaxy formation is biased towards high-density regions^{7,8}. We have shown that such a biased model successfully matches the distribution of galaxies on megaparsec (Mpc) scales⁹. If it is to be viable, it must also account for the structure of individual galaxies and their haloes. Here we describe a simulation of a flat CDM universe which can resolve structures of comparable scale to the luminous parts of galaxies. We find that such a universe produces objects with the abundance and characteristic properties inferred for galaxy haloes. Our results imply that merging plays an important part in galaxy formation and suggest a possible explanation for the Hubble sequence.





Balatonfured: East meets West



Yakob Zel'dovich (1914 – 1987)

(15-19) / June / 1987

INTERNATIONAL ASTRONOMICAL UNION
SYMPOSIUM No. 130

LARGE SCALE STRUCTURES OF THE UNIVERSE

Edited by
JEAN AUDOUZE, MARIE-CHRISTINE PELLETAN and ALEX SZALAY

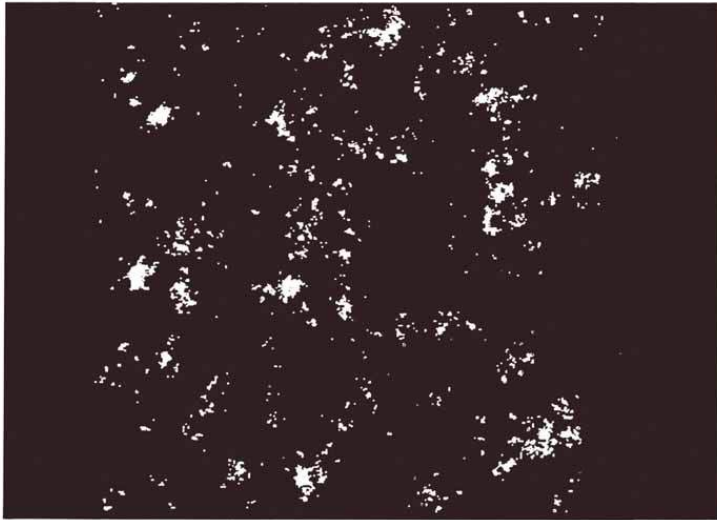


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† deceased on 12/2/87

APPENDIX 2 :
THE BALATONFÜRED ALPHABET OF COSMOLOGY

by Vera Rich

Firstly, Aaronson let us recall,
For his death was a blow to us all,
But his papers, J. Mould,
His colleague of old,
Will present in due time, in the Hall.

With B, let us contemplate Bubbles,
Which have brought to our theory some troubles ;
Distance now must be counted,
So turn we, undaunted,
To red shift, and that constant of Hubble's.

Contrariwise, we've C for
Where galaxies closely do
Both richly and poorly,
Observing them, surely,
Will bring the keen schola

In the microwave, Dipoles
Which we plot, ΔT upon
Then, to keep the score le
Kofman draws us the Dev
And a haloed, hirsute Dei

With E, Einstein comes ir
Whose theories once brou
Now we think, with respect,
He was not quite correct ;
But who, out of hundreds, is right ?

With F, we pursue the Fifth Force,
Of many a question the source ;
Profound explanations
Of its implications
Fujii will report in due course.

G for Galaxies, spiral, elliptic,

Or lens-shaped, of origin cryptic ;
And what is this factor
Called the Great Attractor,
Sited southerly from the ecliptic ?

H, of course, our Hungarian Hosts ;
To Sandor and György drink we toasts,
And to the SZOT hotel some !
They made us so welcome,
Down here on Lake Balaton's coasts,

Inflation and the Infrared
Are topics where much may be said,
The data from IRAS
Are sure to inspire us,
[I will argue no more on that head !

**N-bodied is Frenk's simulation
Presentig dark halo formation,
But he gave it so fast
We were quite lost at last,
Though we noted his good correlation !**

May prove a delusion
And lead to confusion
And provoke us to anger irrational

Here at M let controversists chatter,
Looking far where the galaxies scatter :
"In this vast universe
Is a substance perverse :
Is it cold ? Is it Dark ? Does it Matter ?"

**N-bodied is Frenk's simulation
Presentig dark halo formation,
But he gave it so fast
We were quite lost at last,
Though we noted his good correlation !**

The picture builds up over days.

W — and arrived at this junction,
The brain shows a marked lack of gumption :
But to counter a void,
What else should be deployed
But its complement, viz : the Wall function ?

And now X—ray background (alas !)
Does it emanate from dispersed gas
Abundant in heat ?
Or from sources discrete
Of baryons, heavy in mass ?

[wh]Y is the questioning particle,
A most indispensable article !

For did they not ask,
sk
speaking, unstartable !
t ! So, ere I go (which
let you know which
the best :
em with zest :
Audouze to Zel'dovich !

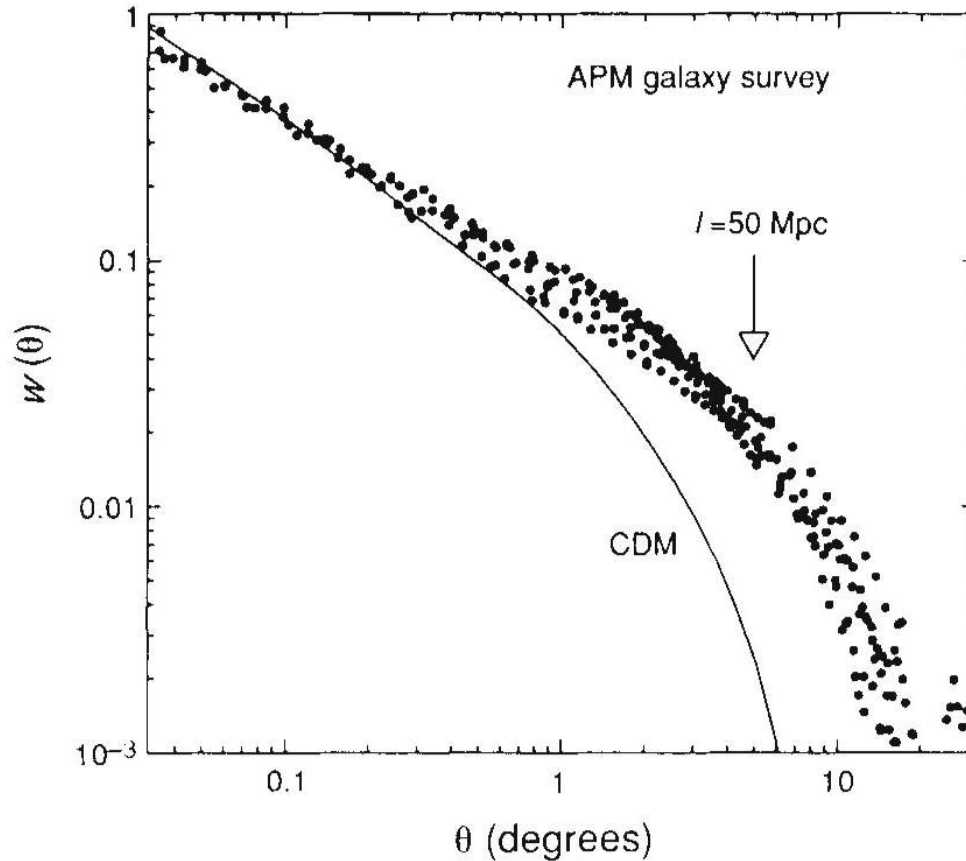
CDM rules

1987



$\Omega = 1$ CDM under strain

Angular 2-pt correlation function



Maddox, Efstathiou, Sutherland & Loveday '90

Nature 1992

REVIEW ARTICLE

The end of cold dark matter?

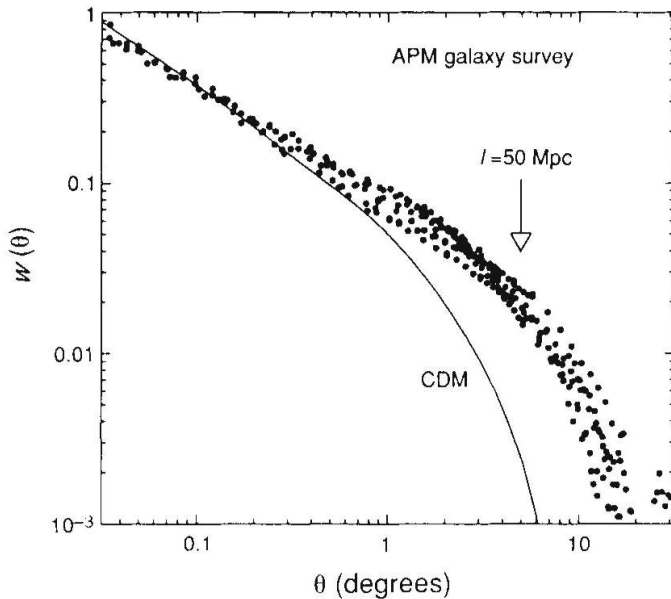
M. Davis, G. Efstathiou, C. S. Frenk & S. D. M. White

The successful cold dark matter (CDM) theory for the formation of structure in the Universe has suffered recent setbacks from observational evidence suggesting that there is more large-scale structure than it can explain. This may force a fundamental revision or even abandonment of the theory, or may simply reflect a modulation of the galaxy distribution by processes associated with galaxy formation. Better understanding of galaxy formation is needed before the demise of CDM is declared.

How did structure in the Universe form? This question has puzzled mankind for centuries, but in the past decade some cosmologists have felt that they were close to providing an answer. What has become known as the cold dark matter (CDM) theory is an elegant construct which links many aspects of the structure we see today to physical processes which took place when the Universe was only 10^{-35} s old. Recently, observations have been reported that seem to conflict with this model (see.

tion could have originated from quantum fluctuations that were inflated to macroscopic scale. Except in circumstances that appear contrived, the fluctuations would indeed contain no characteristic scales; in technical terms, irregularities in the spatial curvature are predicted to be a gaussian random field with a scale-invariant spectrum⁹⁻¹². For the first time cosmologists had a set of initial conditions stemming directly from fundamental, even if speculative, physics.

Angular 2-pt correlation function



end of the range allowed by observation⁵⁵, lowering the Hubble constant still further seems an implausible way of obtaining more large-scale structure. Lowering Ω is another possibility, but without an additional ingredient such models are inconsistent both with a spatially flat universe and with present upper limits on fluctuations in the microwave background^{56,57}. These problems can be avoided by appealing to a cosmological constant, because a low-density universe is spatially flat if the cosmological constant takes the value⁵⁸ $\Lambda = 3H_0^2(1 - \Omega)$. With such carefully chosen parameters it is possible to construct a CDM universe that explains large-scale structure⁵⁹, is compatible with inflation and with microwave-background experiments, and is old enough to contain the oldest observed star clusters even for a present expansion rate as high as $H_0 = 80 \text{ km s}^{-1} \text{ Mpc}^{-1}$, the value preferred by some recent measurements^{60,61}. From the point of view of a particle physicist, the value of Λ needed to work these miracles is extraordinarily small, 10^{120} times smaller than its 'natural' value⁶². Such fine tuning seems sufficiently unattractive that most cosmologists regard this solution as a long shot, preferring to think that some unknown symmetry principle requires the cosmological constant to be exactly zero.

Other possible fixes for the CDM model involve decaying particles or departures from the scale-invariant seed fluctuations predicted by simple inflationary models. For example, the pre-

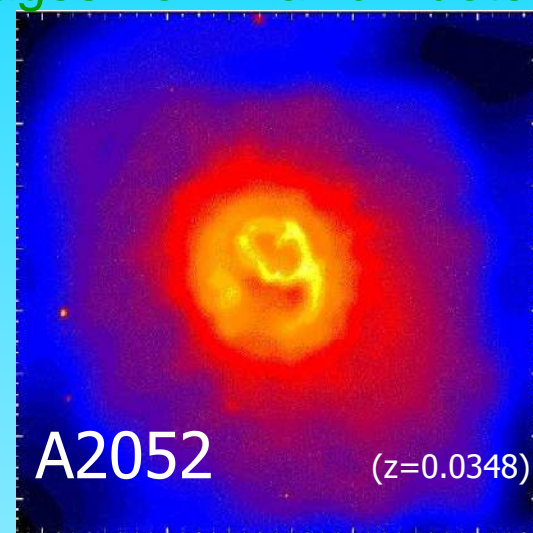
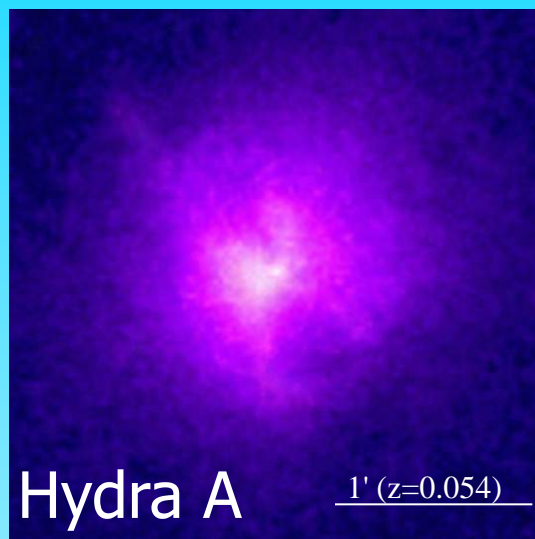
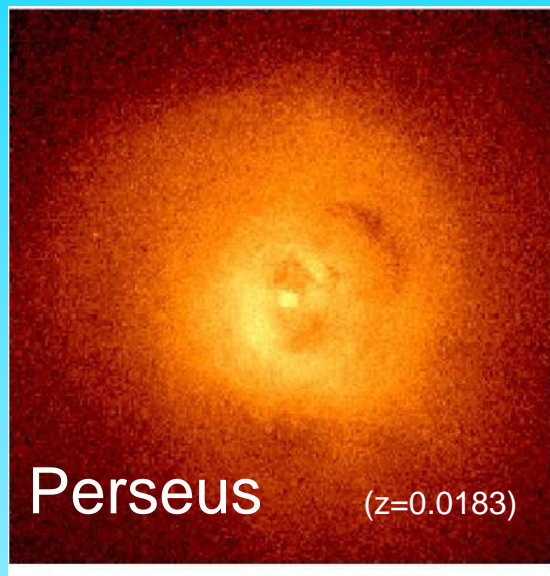


The end of standard ($\Omega_{\text{matter}}=1$) CDM
... or why Ω_{matter} cannot be 1

Galaxy clusters

X-ray emission from hot plasma in clusters

Images from David Buote



About 90% of baryons in clusters are in hot gas

X-rays \Rightarrow gas mass

Photometry \Rightarrow stellar mass

Gas in hydrostatic equilibrium so X-rays

(or lensing) \Rightarrow total gravitating mass

\Rightarrow Baryon fraction, f_b

Ω from the baryon fraction in clusters

baryon fraction in clusters \approx baryon fraction of universe

$$f_b = \frac{M_b}{M_{tot}} = \gamma \frac{\Omega_b}{\Omega_m}$$

White, Navarro,
Evrard & Frenk
Nature 1993

where $\gamma=1$ if f_b has the universal value

simulations $\rightarrow \gamma = 0.9 \pm 10\%$

X-rays+lensing $\rightarrow f_b = (0.060h^{-3/2} + 0.009) \pm 10\%$

BBNS, CMB $\rightarrow \Omega_b h^2 = 0.019 \pm 20\%$

HST $\rightarrow h = 0.7 \pm 10\%$

$$\longrightarrow \Omega_m = \frac{\Omega_b \gamma}{f_b} = 0.31 \pm 0.12$$

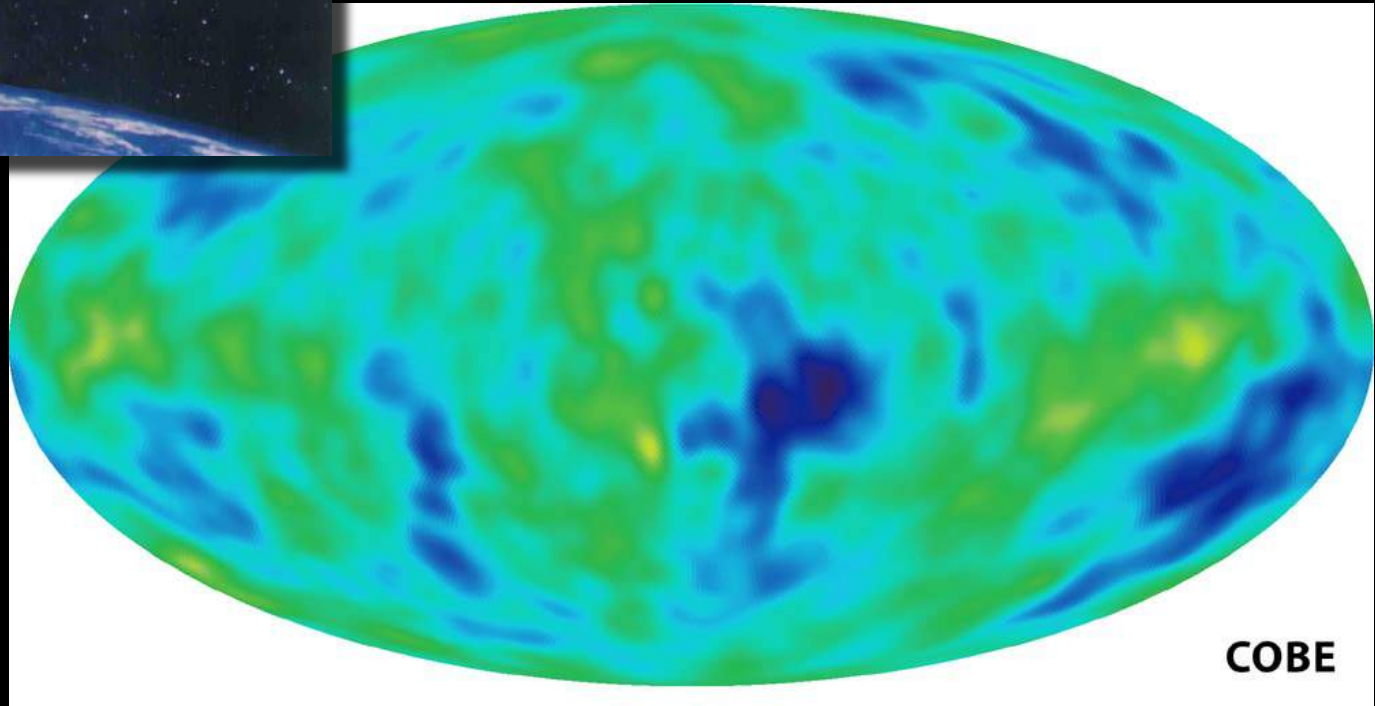
White, Navarro,
Evrard & Frenk '93
Allen et al '04

\rightarrow Flat geometry (inflation) requires $\Lambda=0.7$

The CMB



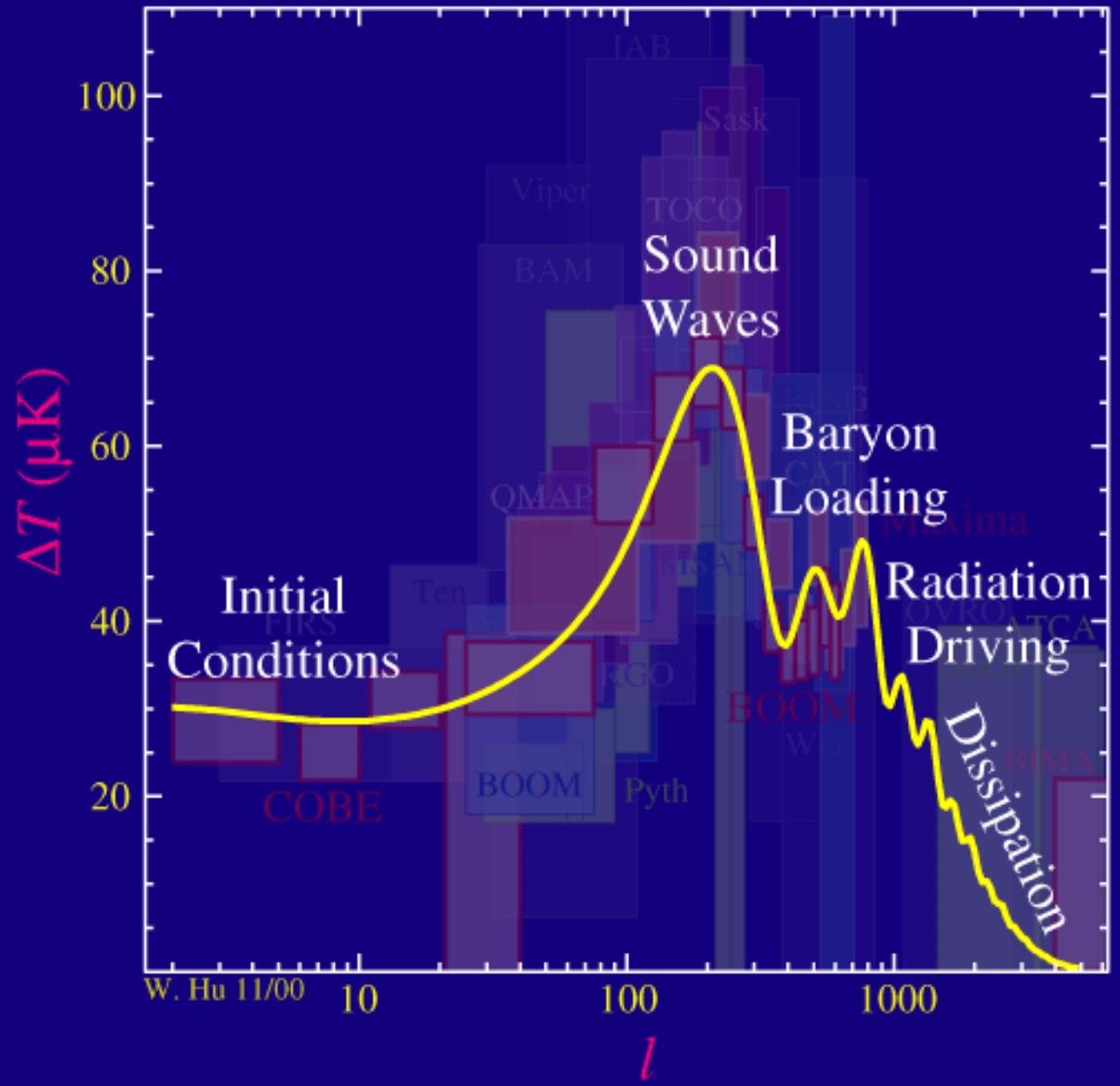
1992





Evidence for a flat universe

1993

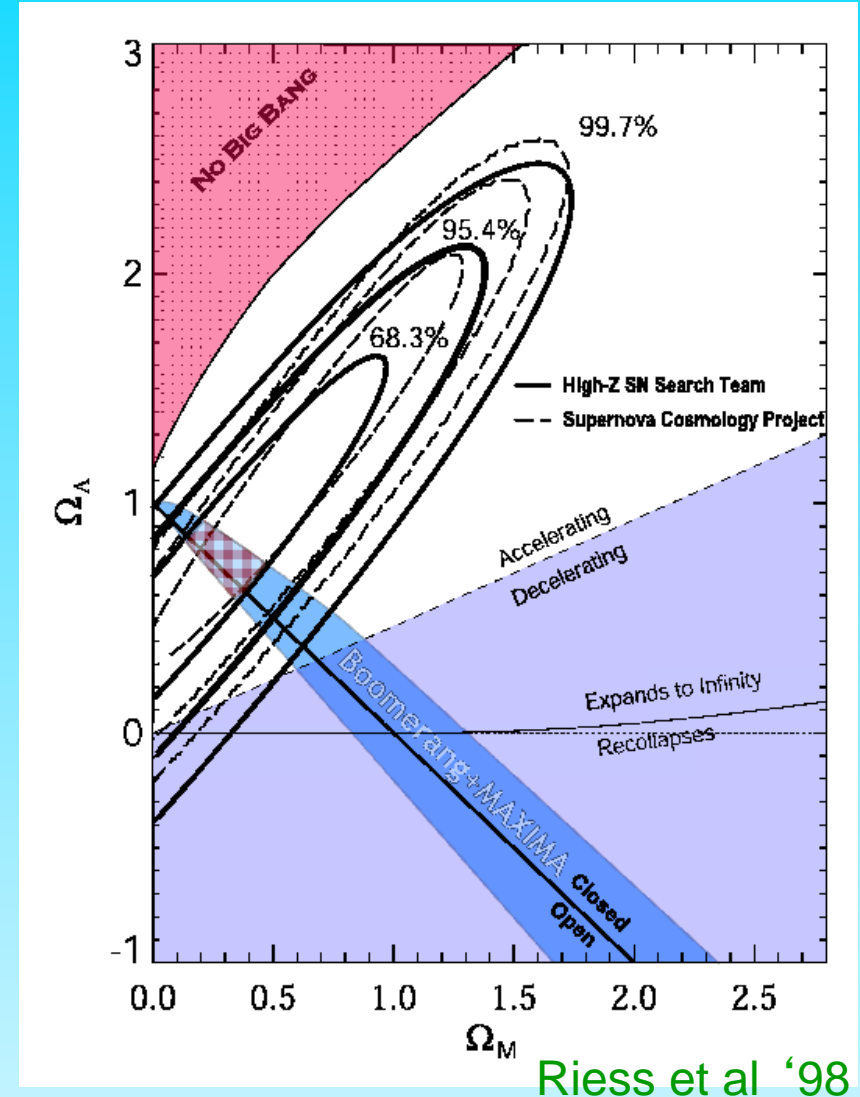
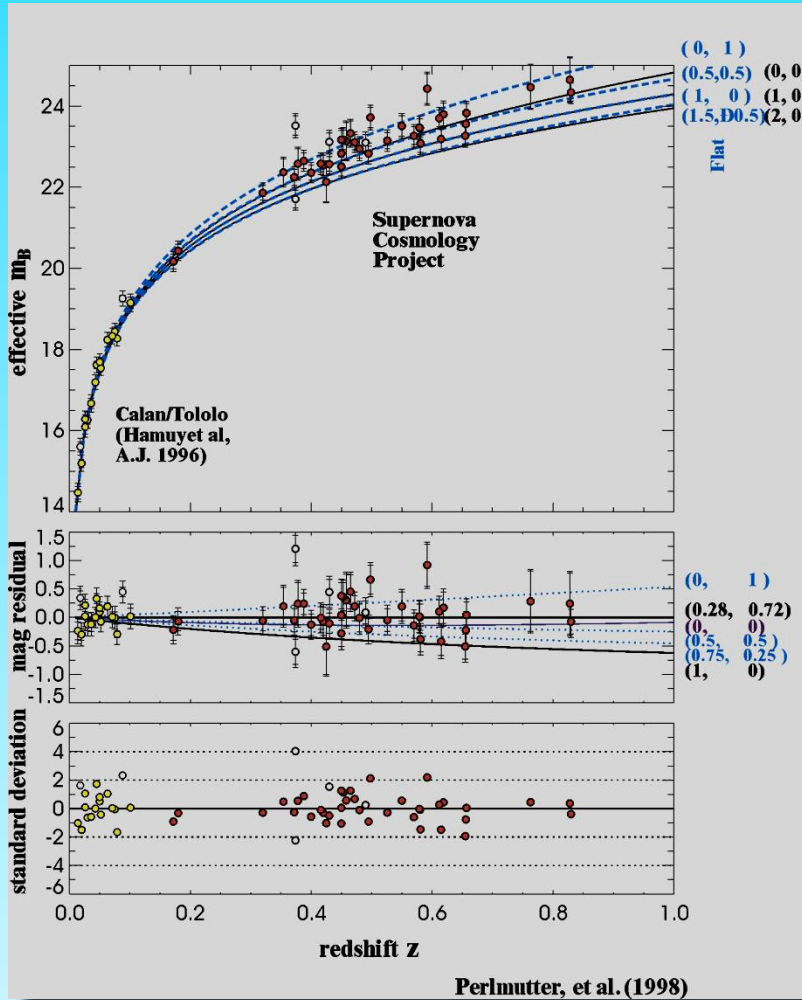




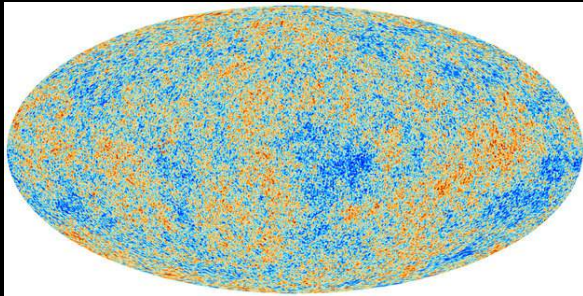
(Some) evidence for dark energy

Evidence for Λ from high-z supernovae

Distant SN are fainter than expected if expansion were decelerating

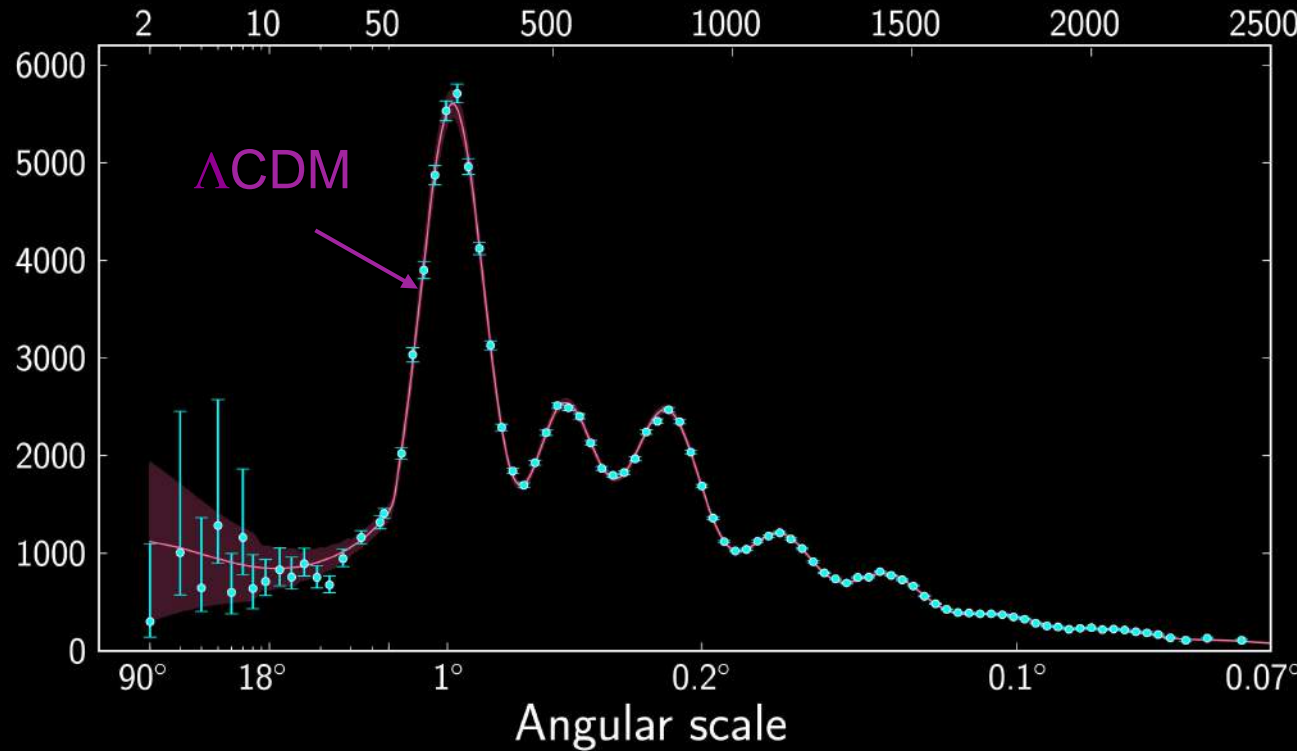


Riess et al '98



Amplitude of fluctuations at $z \sim 1000$

Multipole moment, ℓ



Temperature fluctuations [μK^2]

The data confirm
the theoretical
predictions
(linear theory)

Peebles '82; Bond &
Efstathiou '80s

Planck collaboration '13



Cosmological parameters from CMB data

Parameter	<i>Planck</i> +WP		<i>Planck</i> +WP+highL		<i>Planck</i> +lensing+WP+highL	
	Best fit	68% limits	Best fit	68% limits	Best fit	68% limits
$\Omega_b h^2$	0.022032	0.02205 ± 0.00028	0.022069	0.02207 ± 0.00027	0.022199	0.02218 ± 0.00026
$\Omega_c h^2$	0.12038	0.1199 ± 0.0027	0.12025	0.1198 ± 0.0026	0.11847	0.1186 ± 0.0022
$100\theta_{MC}$	1.04119	1.04131 ± 0.00063	1.04130	1.04132 ± 0.00063	1.04146	1.04144 ± 0.00061
τ	0.0925	$0.089^{+0.012}_{-0.014}$	0.0927	$0.091^{+0.013}_{-0.014}$	0.0943	$0.090^{+0.013}_{-0.014}$
n_s	0.9619	0.9603 ± 0.0073	0.9582	0.9585 ± 0.0070	0.9624	0.9614 ± 0.0063
$\ln(10^{10} A_s)$	3.0980	$3.089^{+0.024}_{-0.027}$	3.0959	3.090 ± 0.025	3.0947	3.087 ± 0.024
Ω_Λ	0.6817	$0.685^{+0.018}_{-0.016}$	0.6830	$0.685^{+0.017}_{-0.016}$	0.6939	0.693 ± 0.013
σ_8	0.8347	0.829 ± 0.012	0.8322	0.828 ± 0.012	0.8271	0.8233 ± 0.0097
z_{re}	11.37	11.1 ± 1.1	11.38	11.1 ± 1.1	11.42	11.1 ± 1.1
H_0	67.04	67.3 ± 1.2	67.15	67.3 ± 1.2	67.94	67.9 ± 1.0
Age/Gyr	13.8242	13.817 ± 0.048	13.8170	13.813 ± 0.047	13.7914	13.794 ± 0.044
$100\theta_*$	1.04136	1.04147 ± 0.00062	1.04146	1.04148 ± 0.00062	1.04161	1.04159 ± 0.00060
r_{drag}	147.36	147.49 ± 0.59	147.35	147.47 ± 0.59	147.68	147.67 ± 0.50

The 2dF Galaxy Redshift Survey

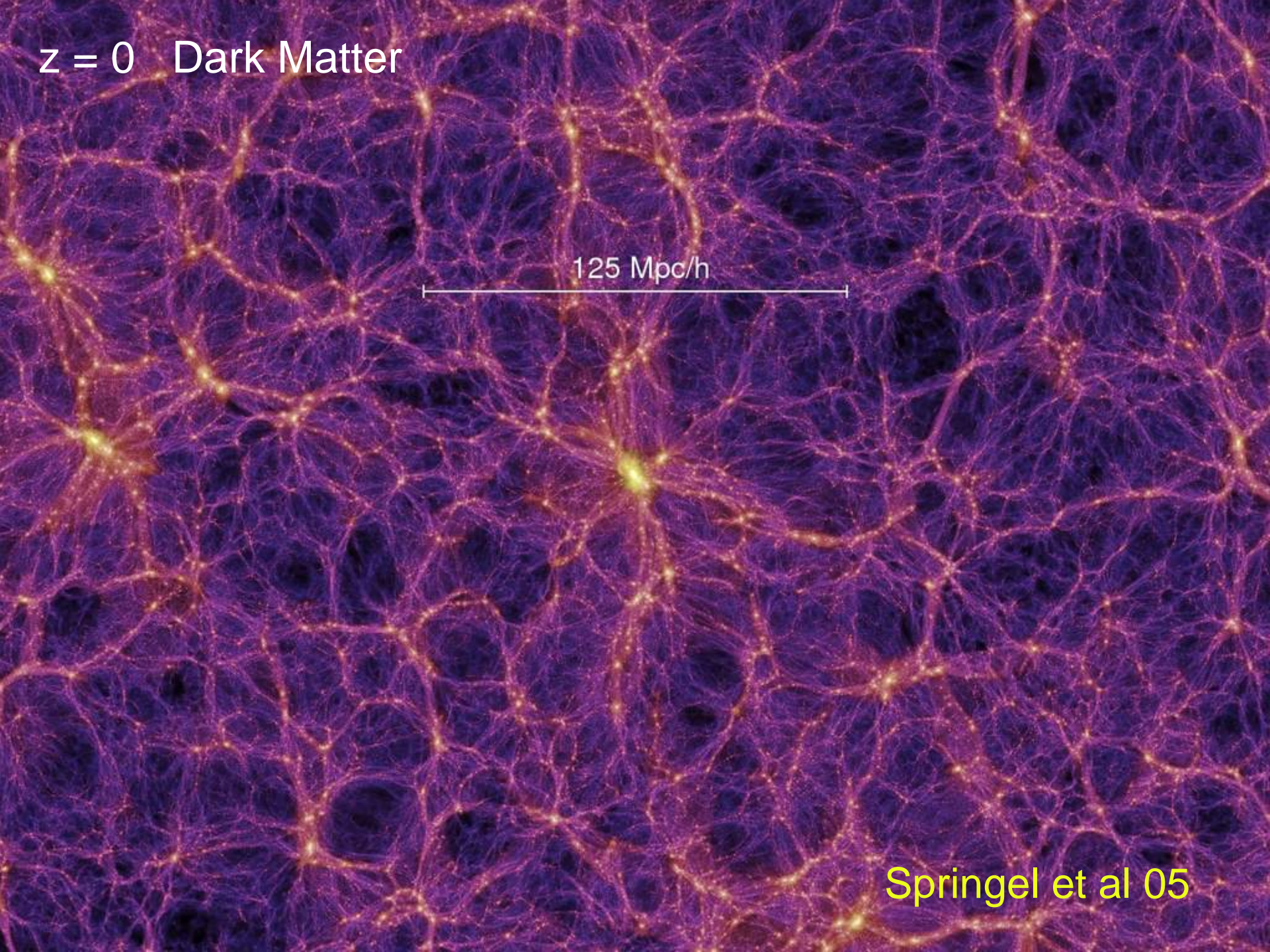
221,000 redshifts

$z \sim 0$



2005

$z = 0$ Dark Matter

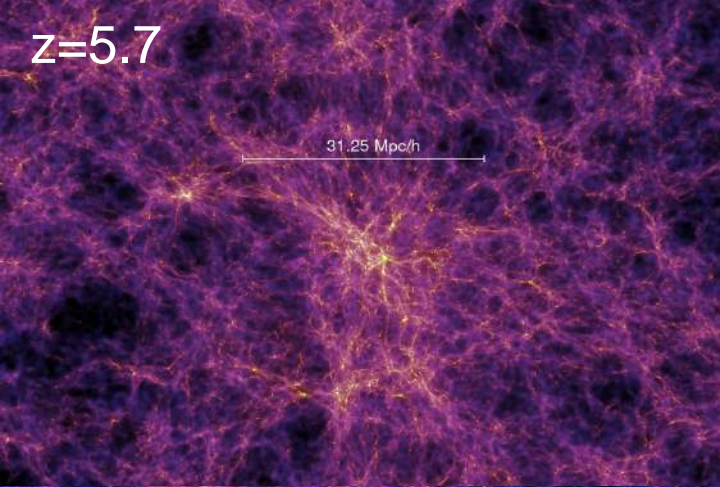


125 Mpc/h

Springel et al 05

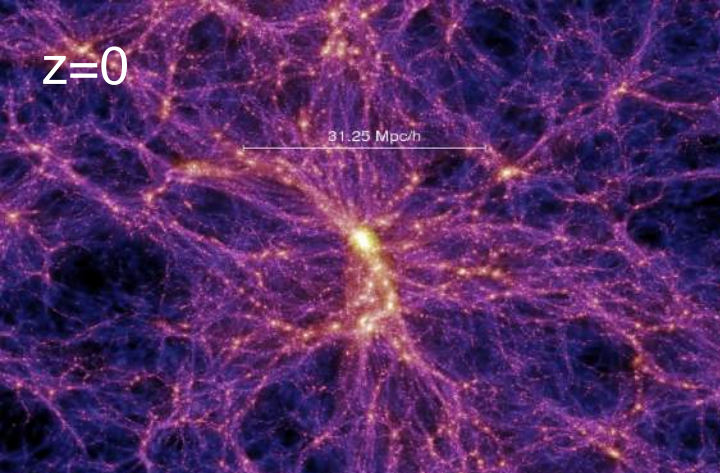
$z=5.7$

31.25 Mpc/h

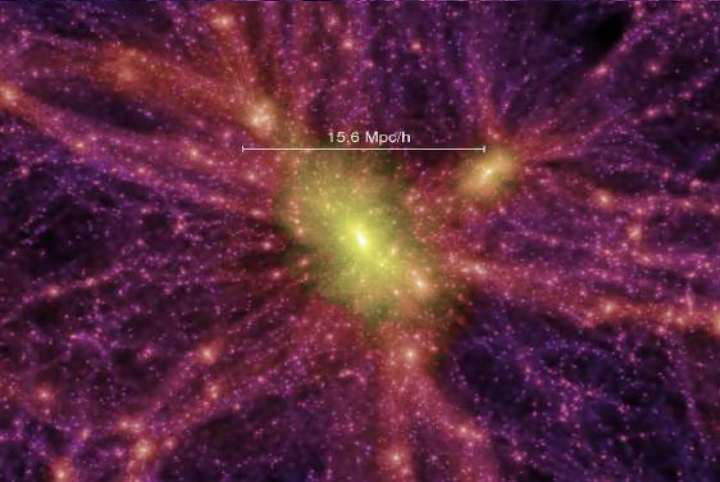


$z=0$

31.25 Mpc/h



15.6 Mpc/h



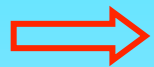
Galaxy formation theory

To compare simulations vs observations, need to know where the galaxies form

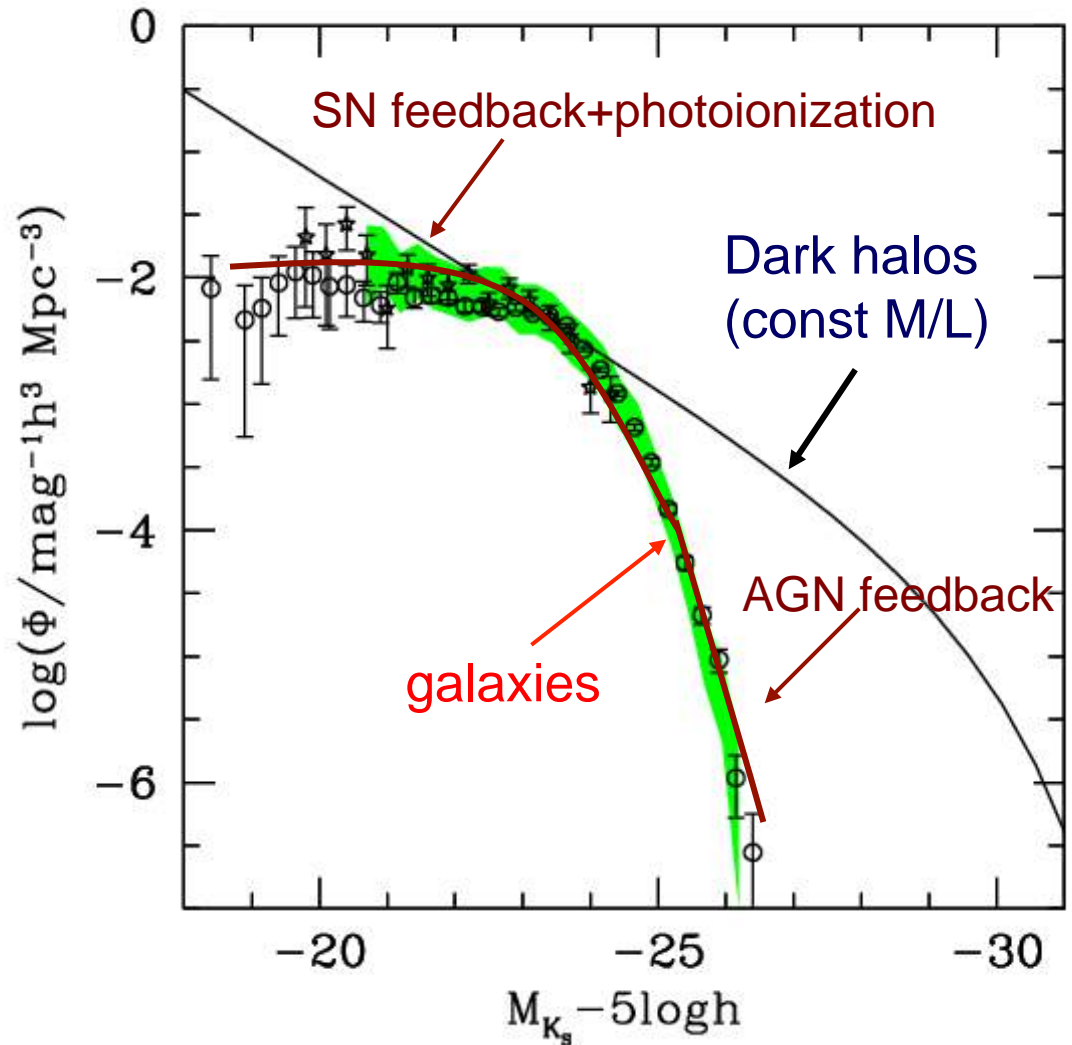
Galaxy formation theory:
a physics-based model for the formation and evolution of galaxies

The galaxy luminosity function

The halo mass function and the galaxy luminosity function have different shapes



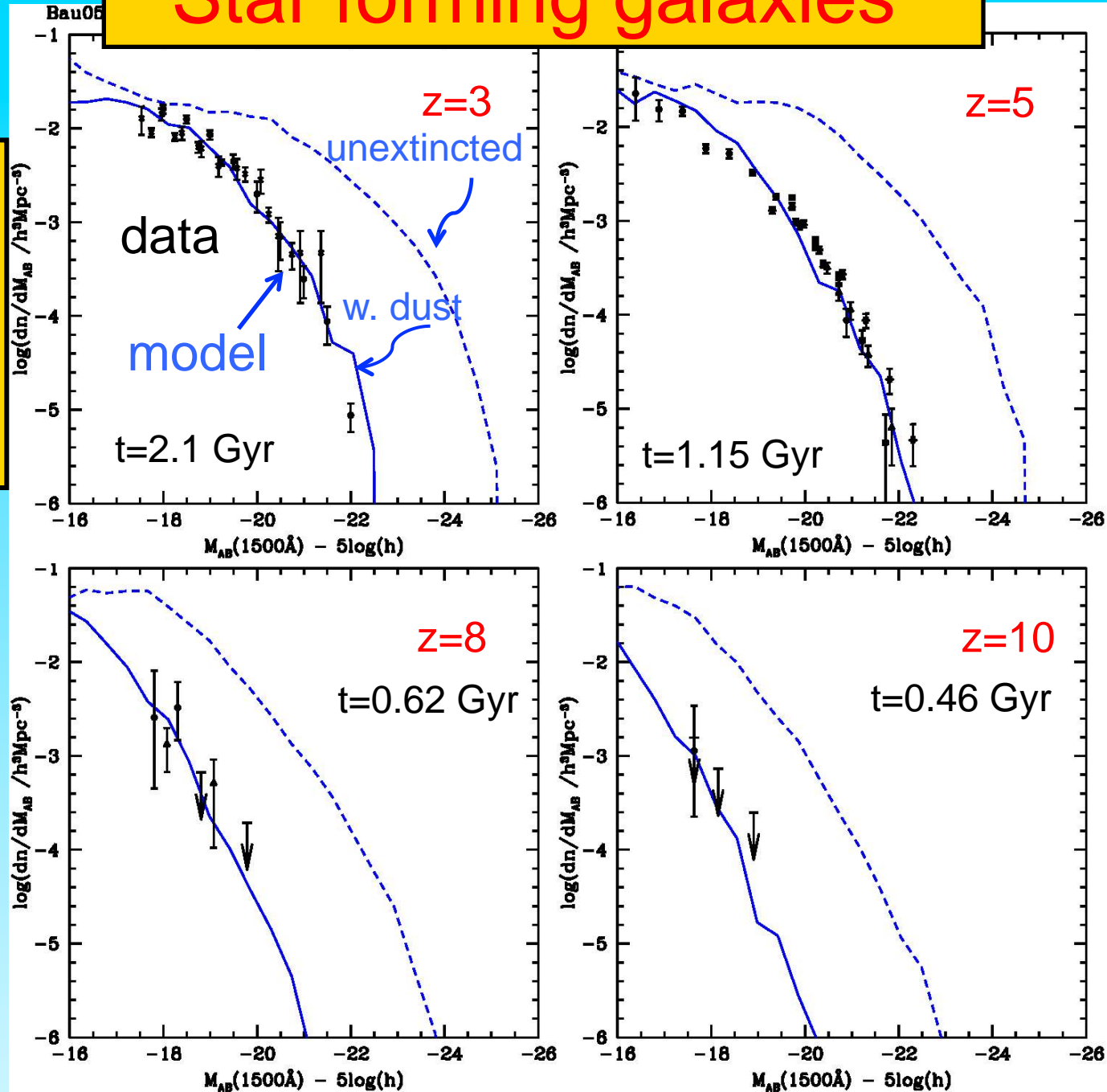
Complicated variation of M/L with halo mass



White & Frenk '91; Kauffmann et al '93; Benson et al '03; Croton et al '05; Bower et al. '06

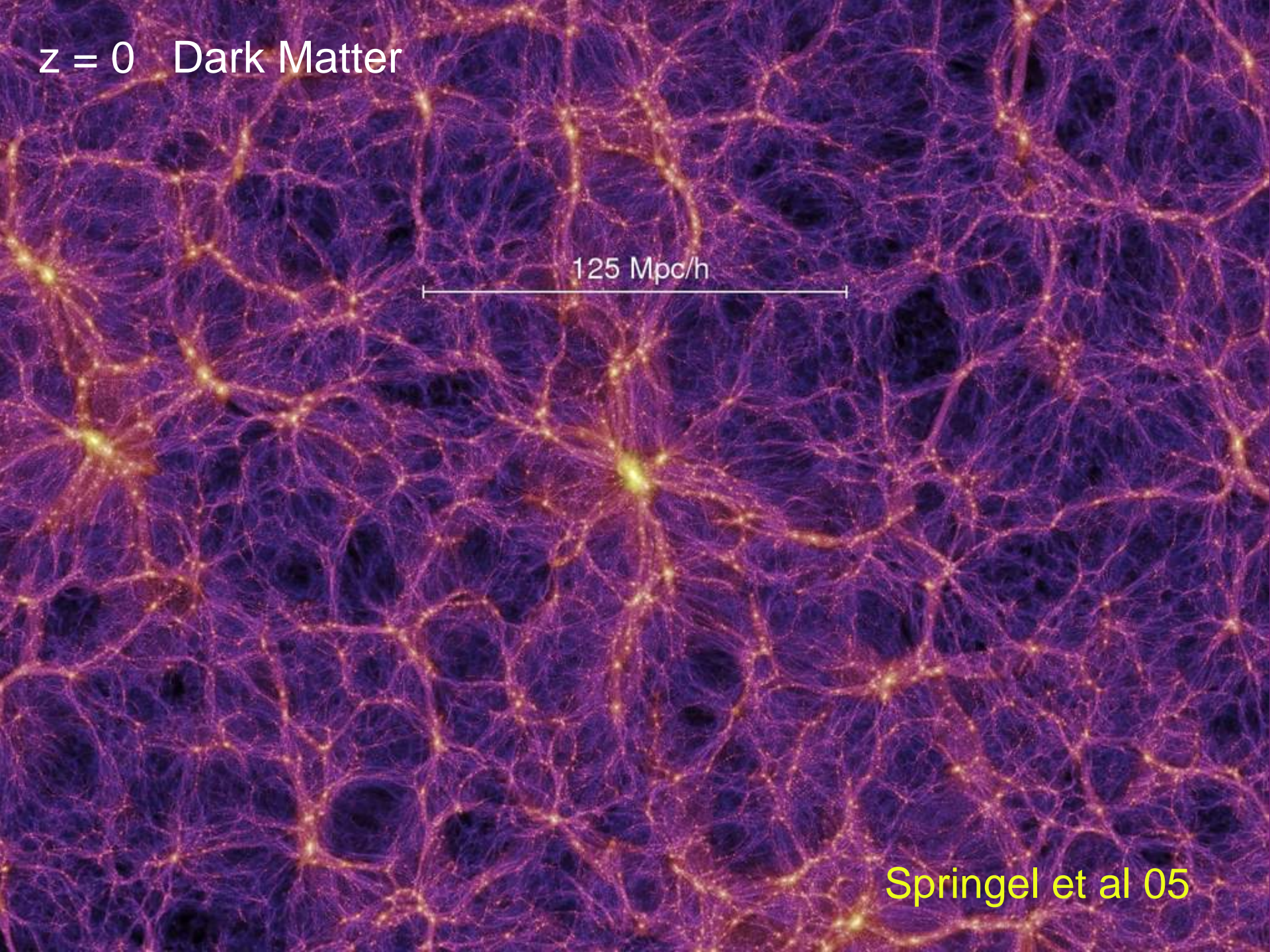
Star forming galaxies

Evolution of Lyman-break galaxy lum. function



Lacey, Baugh, Frenk, Benson '12

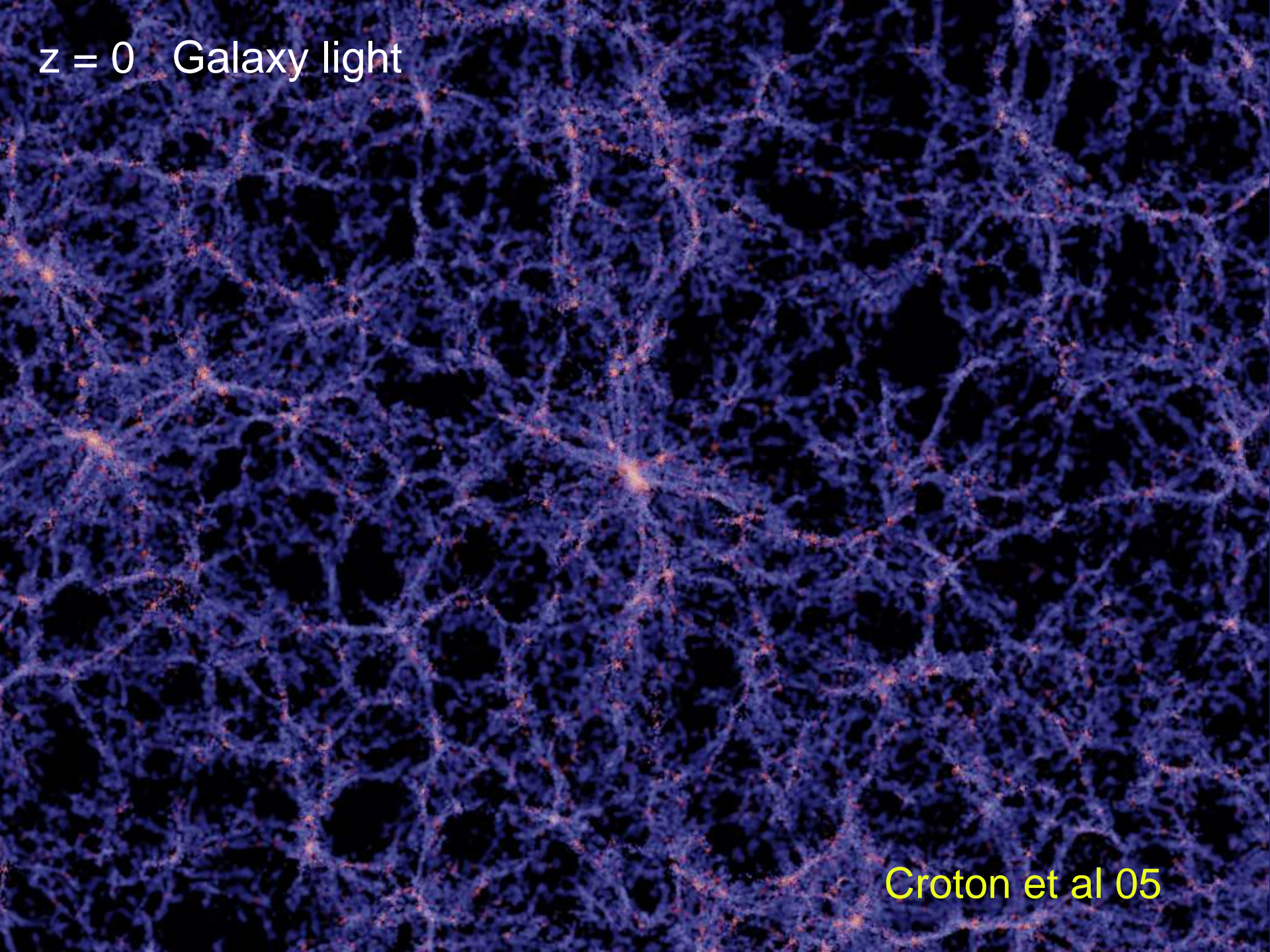
$z = 0$ Dark Matter



125 Mpc/h

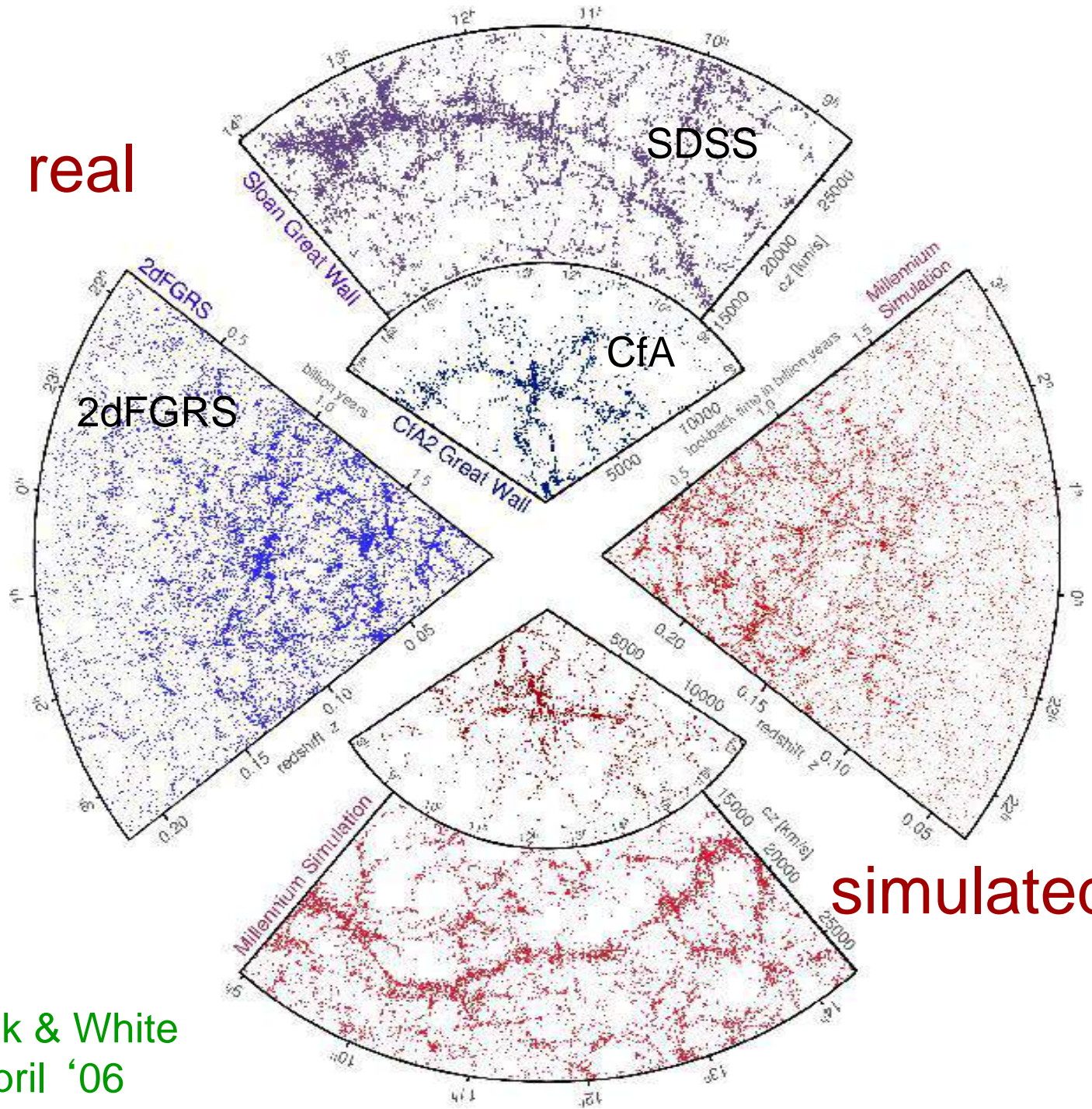
Springel et al 05

$z = 0$ Galaxy light



Croton et al 05

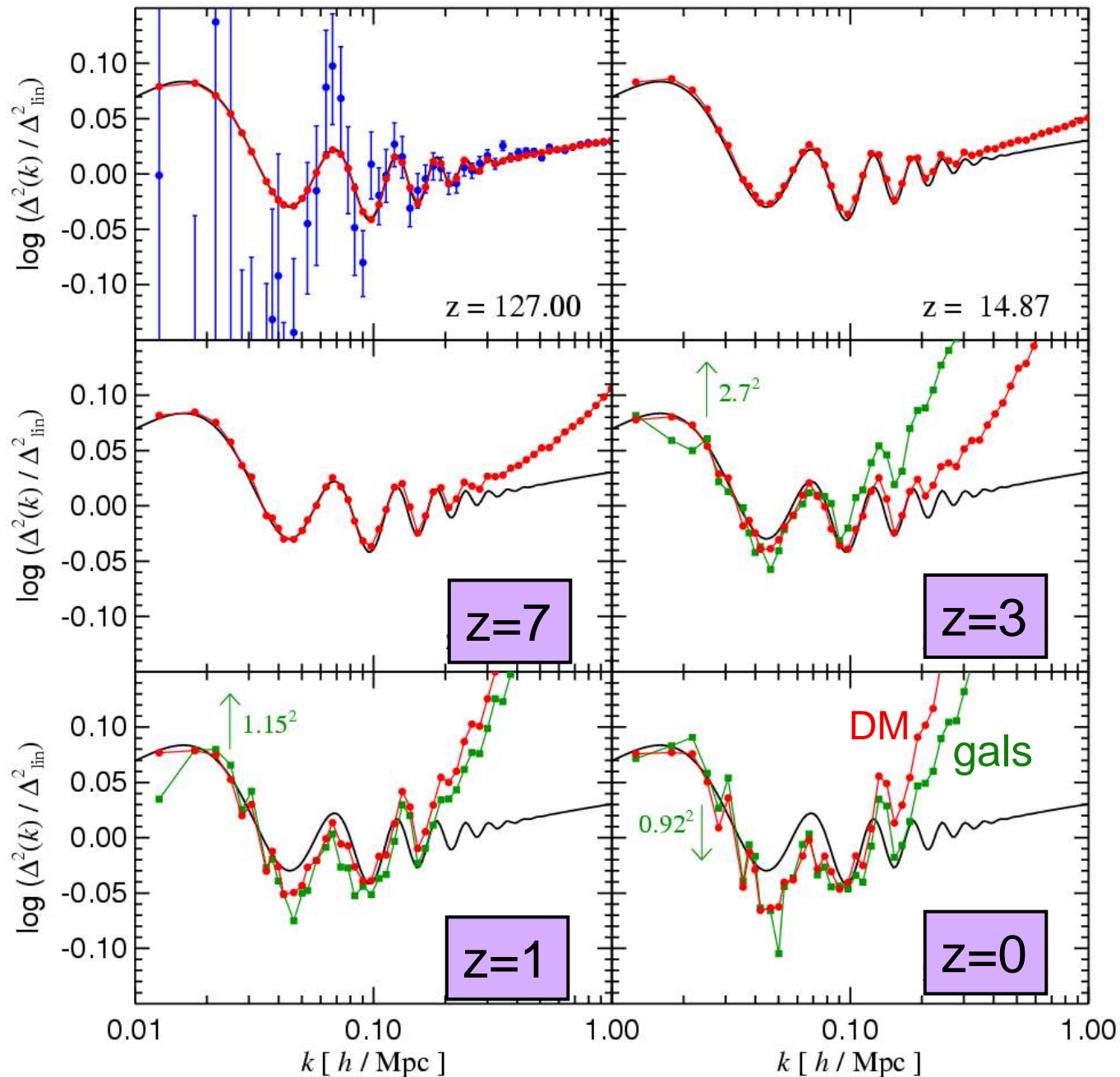
real



simulated

Springel, Frenk & White
Nature, April '06

Millennium simulation



Baryon wiggles in the galaxy distribution

Power spectrum from MS divided by a baryon-free Λ CDM spectrum

Galaxy samples matched to plausible large observational surveys at given z

Springel et al 2005



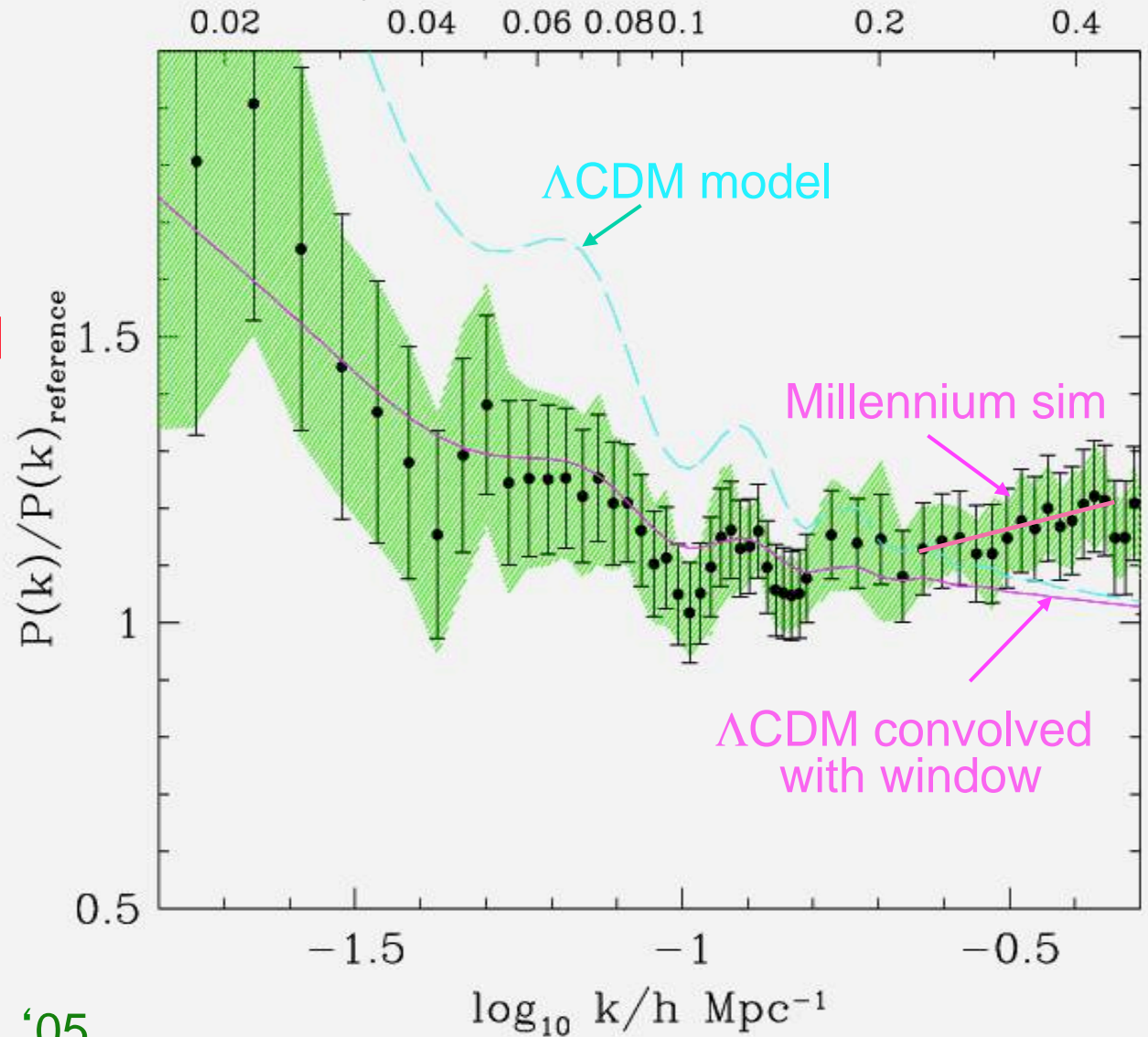
University of Durham

Baryon acoustic oscillations in 2dFGRS

$$P(k) / P_{\text{ref}}(\Omega_{\text{baryon}}=0) \text{ k/h Mpc}^{-1}$$

220,000 redshifts

Baryon oscillations conclusively detected in 2dFGRS!!!



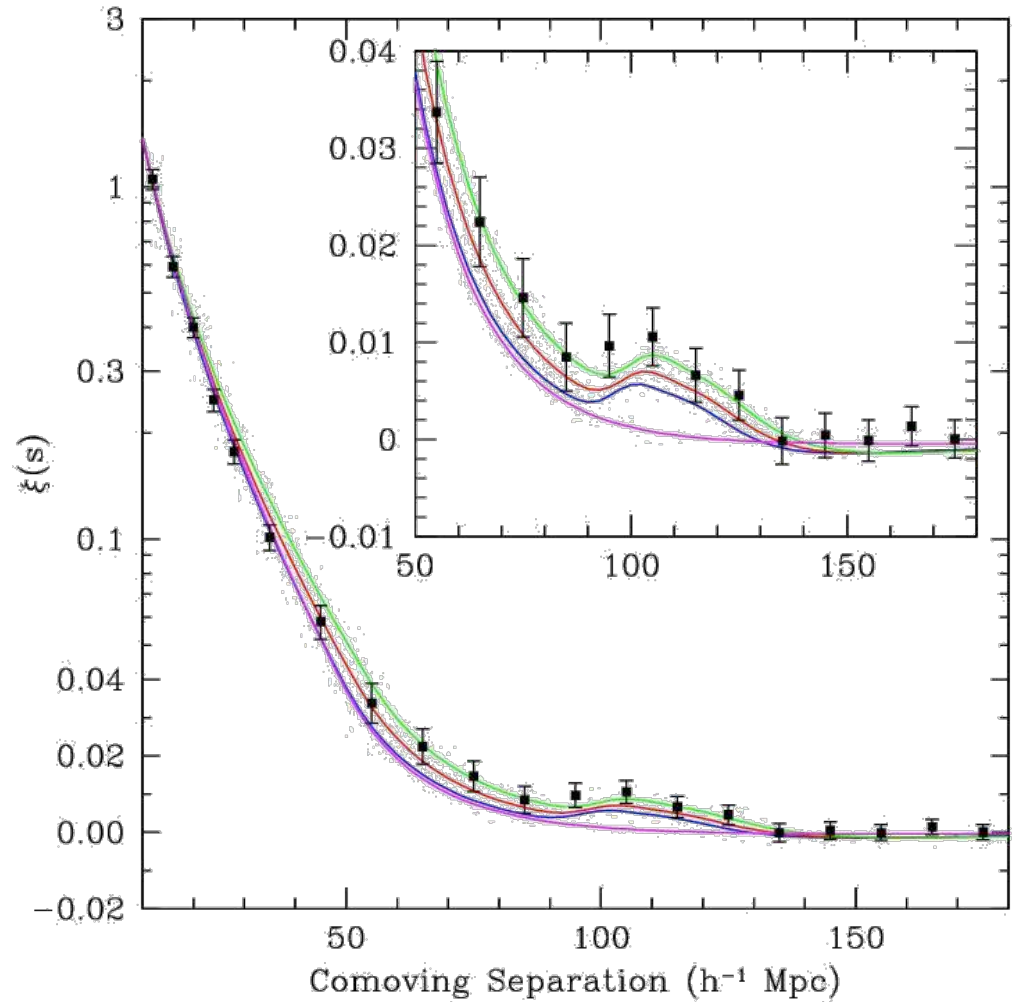
Cole, Percival, Peacock, Baugh, Frenk + 2dFGRS '05

- 47,000 SDSS LRGs
- 0.72 cubic Gpc
- Constraint on spherically averaged BAO scale
- Constrain distance parameter:

$$D_V(z) = \left[D_M(z)^2 \frac{cz}{H(z)} \right]^{1/3}$$

Angular diameter distance

Hubble parameter



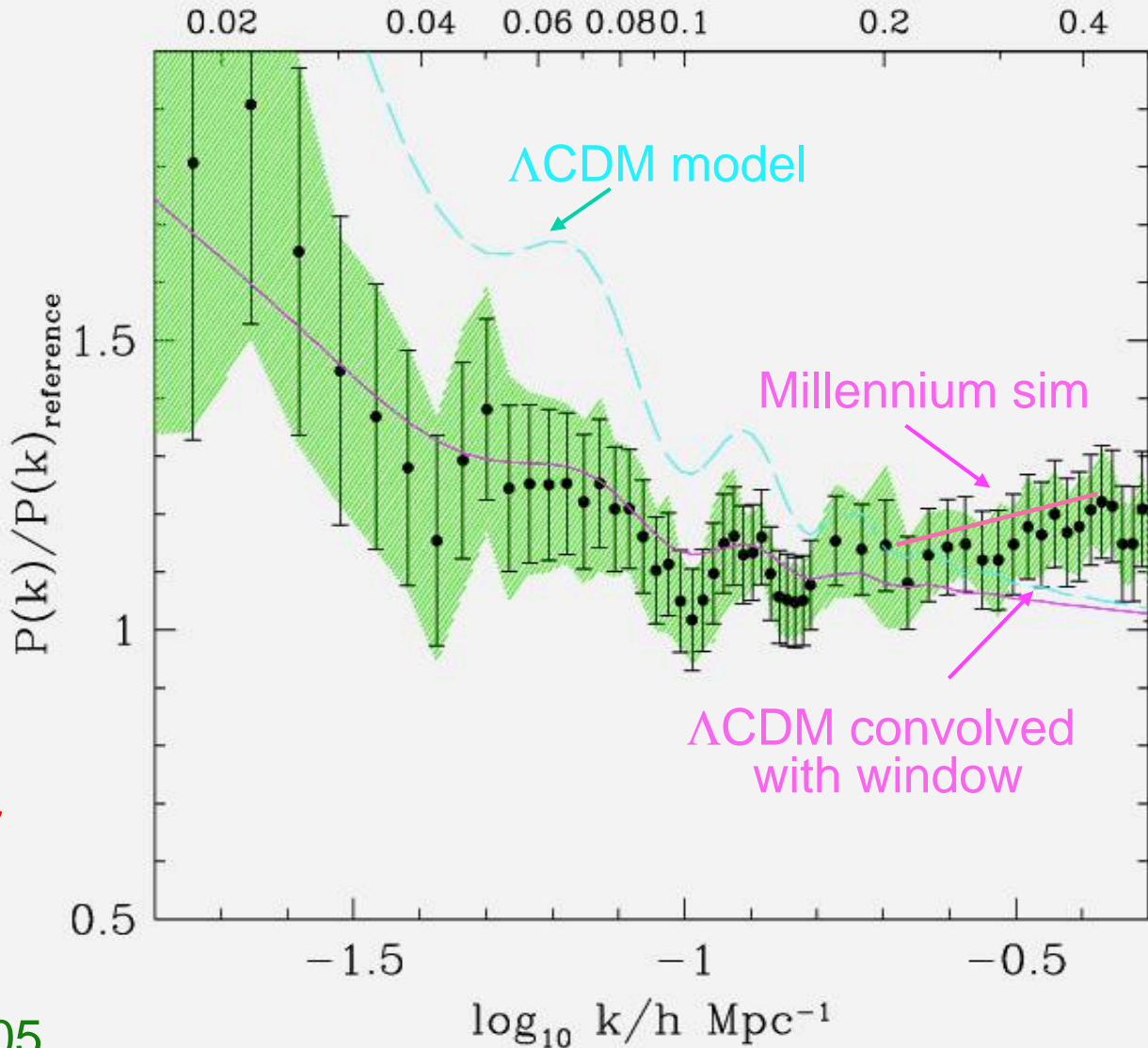
Eisenstein et al '05

Baryon acoustic oscillations in 2dFGRS

$$P(k) / P_{\text{ref}}(\Omega_{\text{baryon}}=0) \quad k/h \text{ Mpc}^{-1}$$

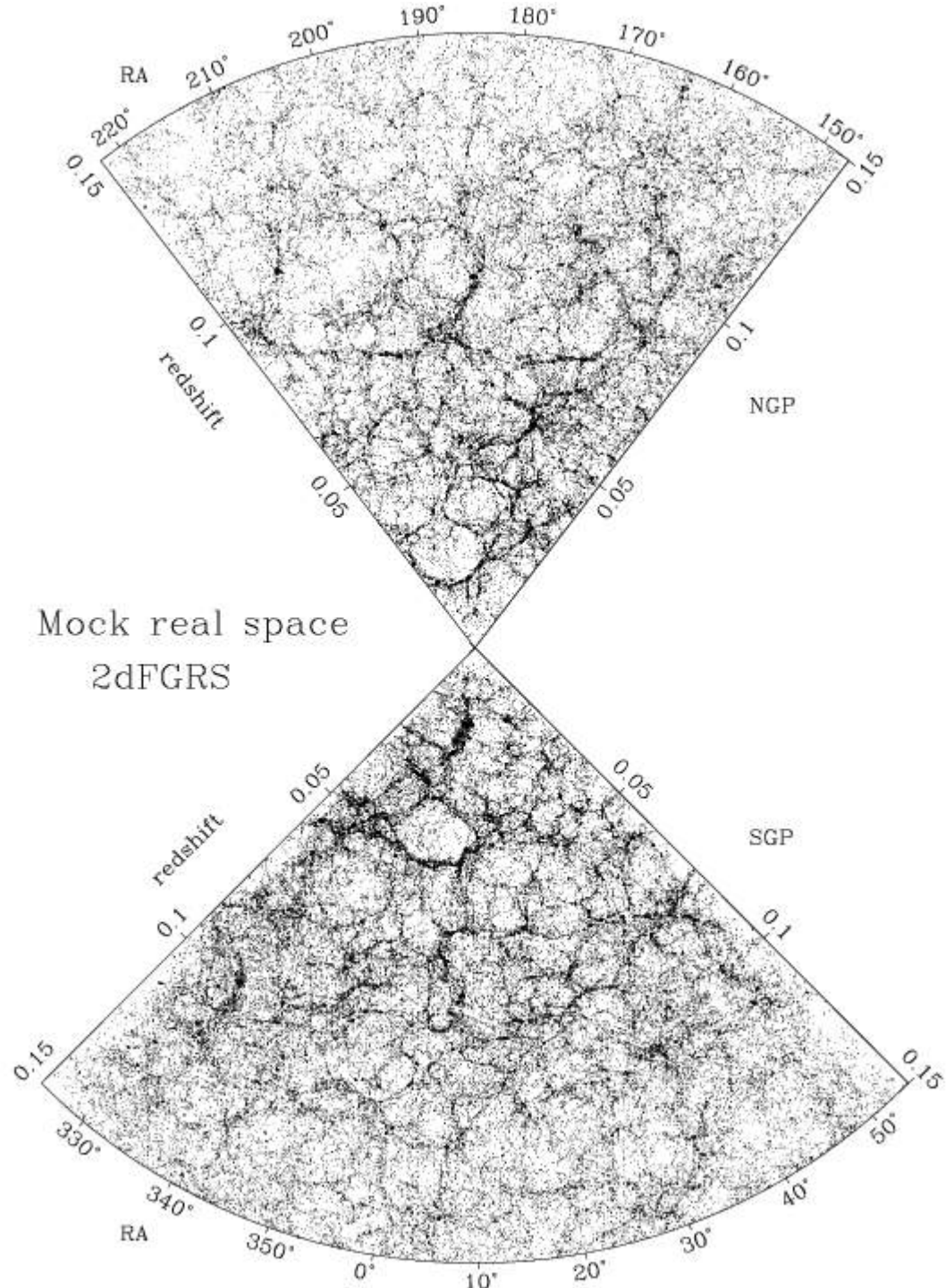
Baryon oscillations in 2dFGRS →

- Consistency with **structure growth** by gravitational instability in a Λ CDM universe
- Since size of acoustic horizon at t_{rec} known, **BAO** are **standard ruler**



Mock 2dFGRS from Hubble vol sim

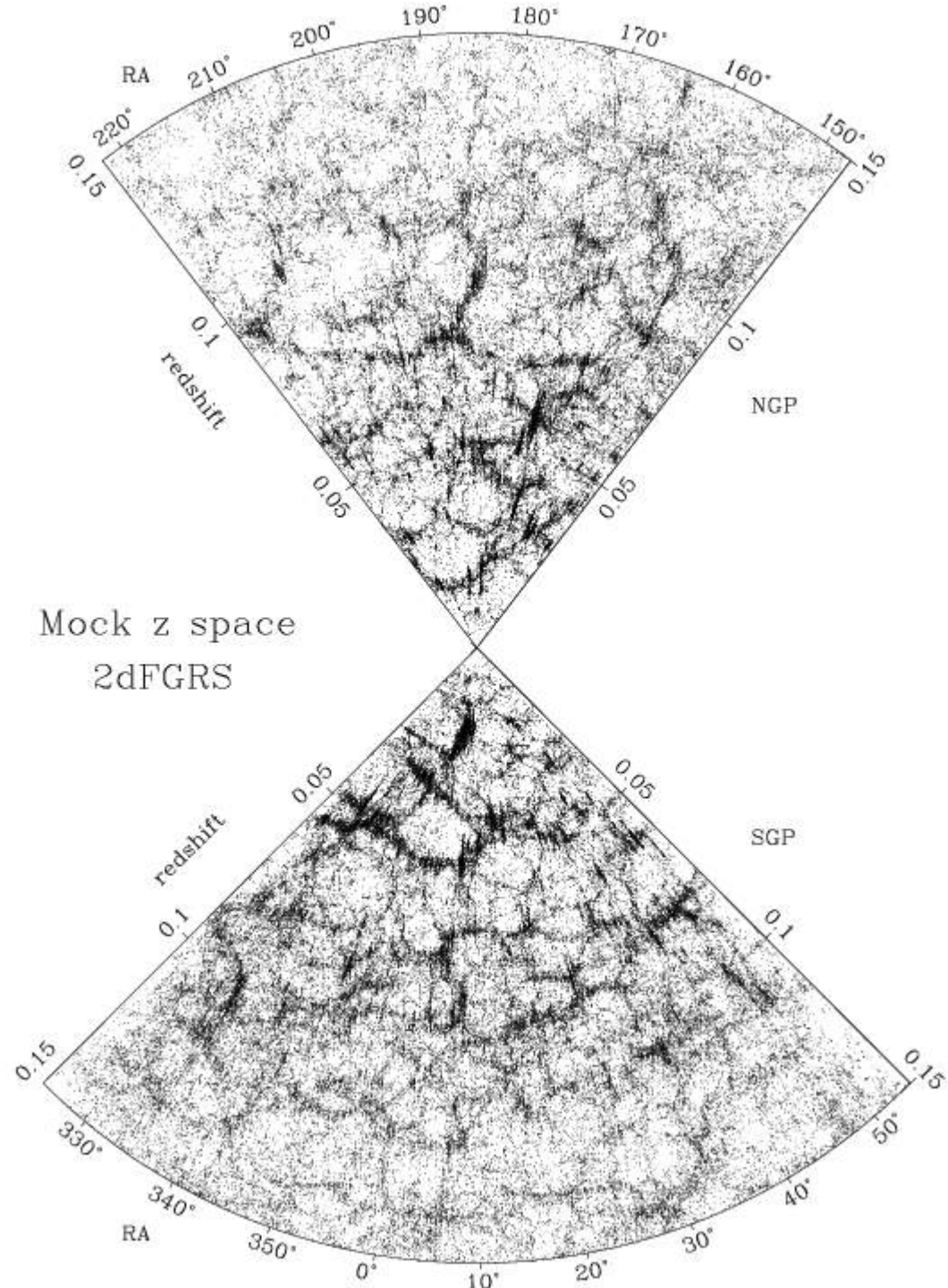
real space



Eke, Frenk, Cole, Baugh +
2dFGRS 2003

Mock 2dFGRS from Hubble vol sim

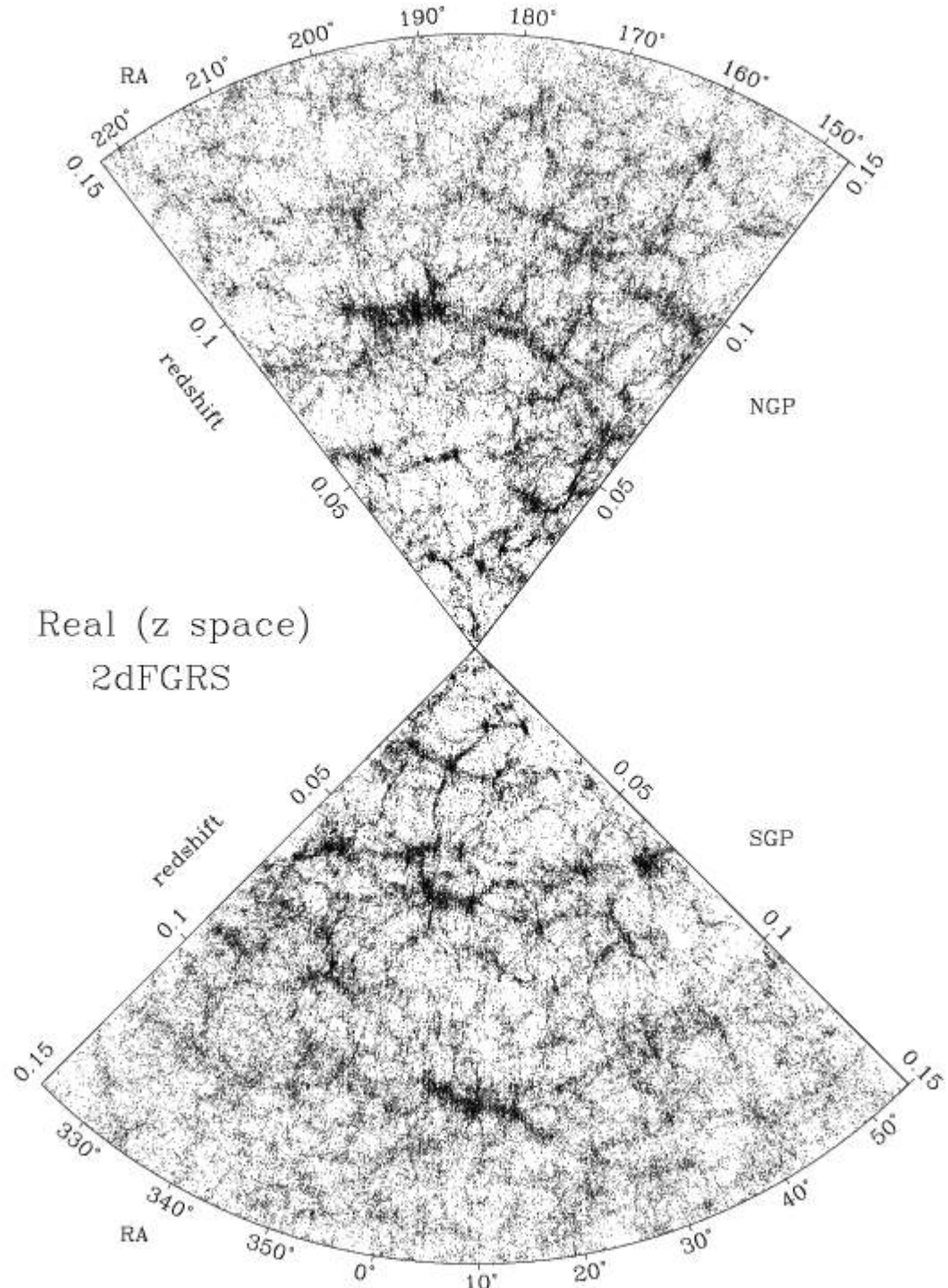
z-space



Eke, Frenk, Cole, Baugh +
2dFGRS 2003

Real 2dFGRS

z-space



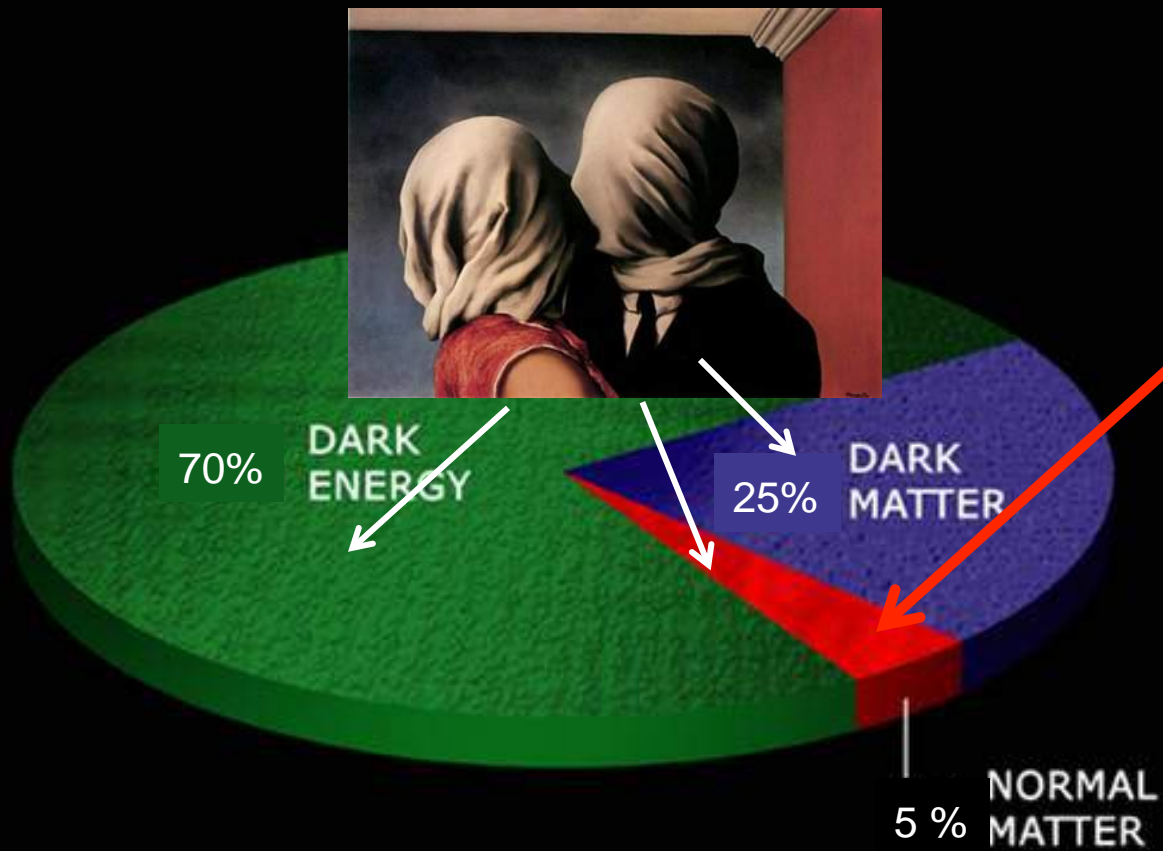


Open problems cosmology best
tackled with simulations



ICC

The content of our universe



- The dark energy problem:
 - Alternatives to Λ CDM: modified gravity, quintessence, etc
- The dark matter problem
 - Warm dark matter, self-interacting dark matter
- The baryon problem
 - How do galaxies form and how do baryons affect the evolution of DM?

The cosmic power spectrum: from the CMB to the 2dFGRS

Free streaming \rightarrow

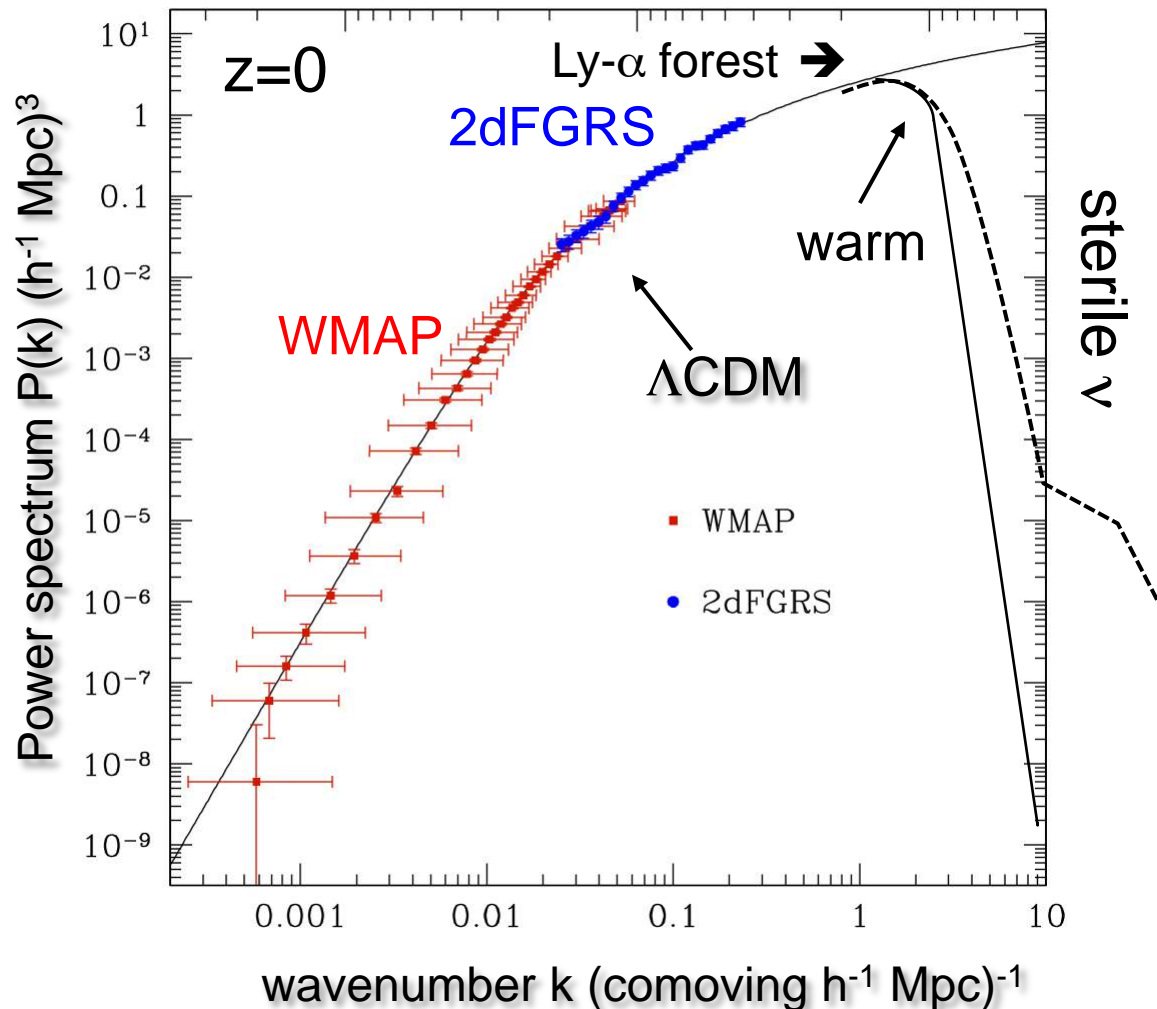
$$\lambda_{\text{cut}} \propto m_x^{-1}$$

for thermal relic

$m_{\text{CDM}} \sim 100 \text{ GeV}$
 susy; $M_{\text{cut}} \sim 10^{-6} M_{\odot}$

$m_{\text{WDM}} \sim \text{few keV}$
 sterile ν ; $M_{\text{cut}} \sim 10^9 M_{\odot}$

Log $k^3 P(k)$ wavelength k^{-1} (comoving $h^{-1} \text{ Mpc}$)





Gold Dark Matter

Warm Dark Matter

13.4 billion years ago

cold dark matter



warm dark matter

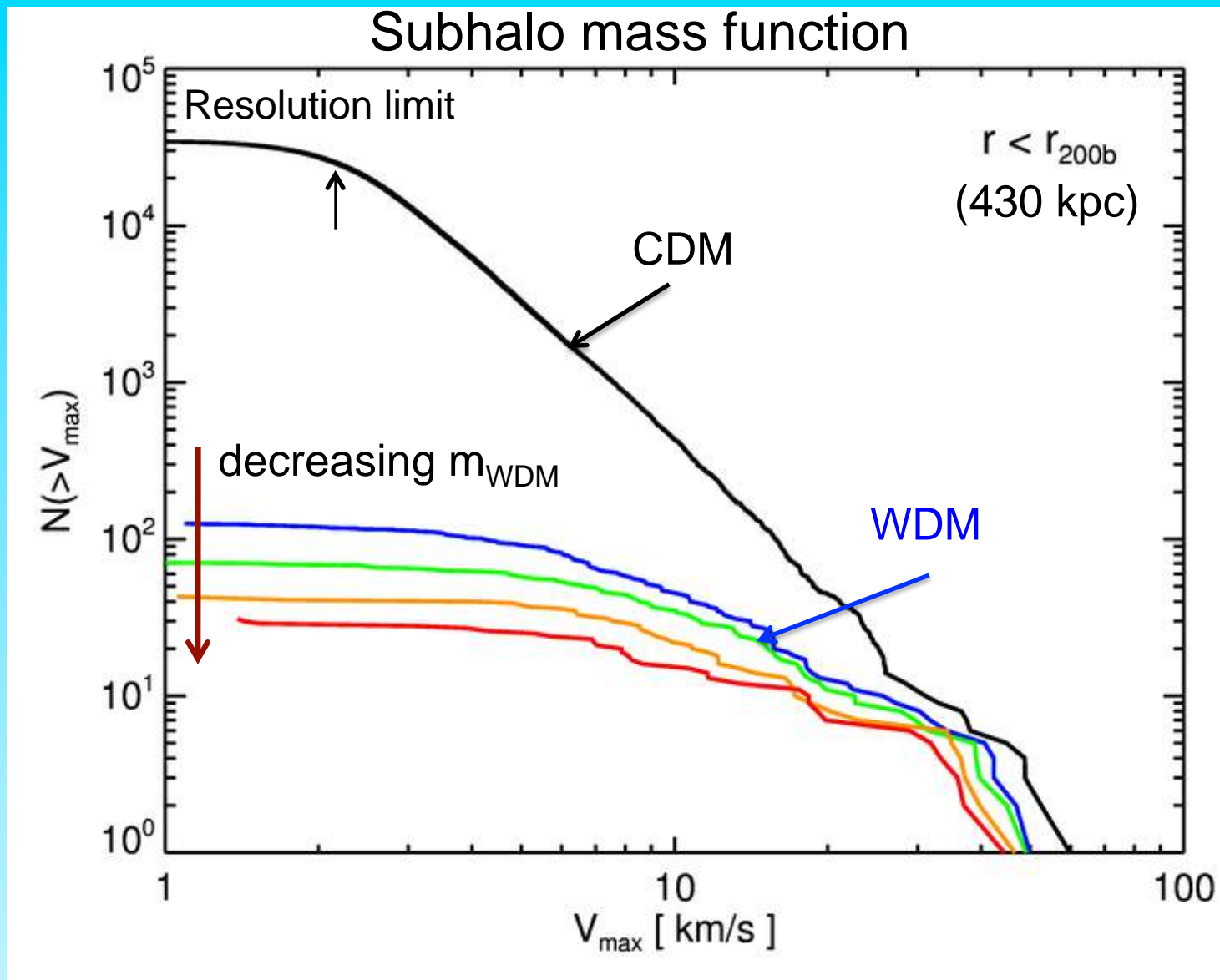


Lovell, Eke, Frenk, Gao, Jenkins, Wang, White, Theuns,
Boyarski & Ruchayskiy '13

The mass function of substructures

- WDM
- 2.3 keV
- 2.0 keV
- 1.6 keV
- 1.4 keV

No of suhalos
 ↗ with m_{WDM}





Subhalo abundance

cold dark matter

warm dark matter



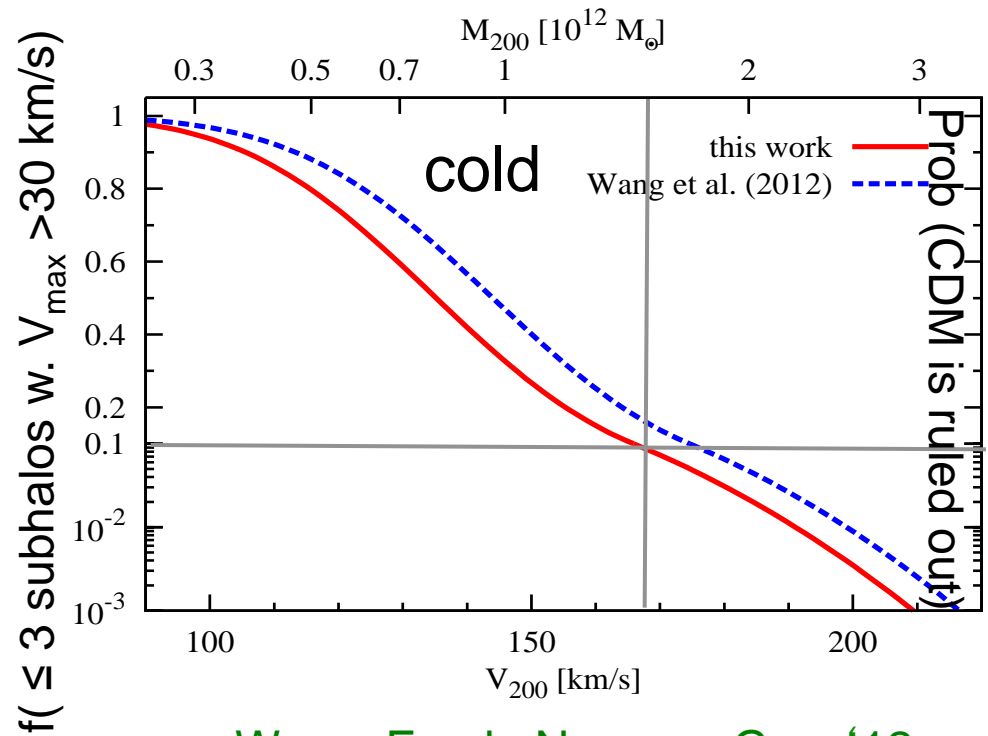
Too big-to-fail?



Too small-to-succeed?

Lovell, Frenk, Eke, Gao, Jenkins, Theuns '12, '13

The nature of the DM and M_{halo}



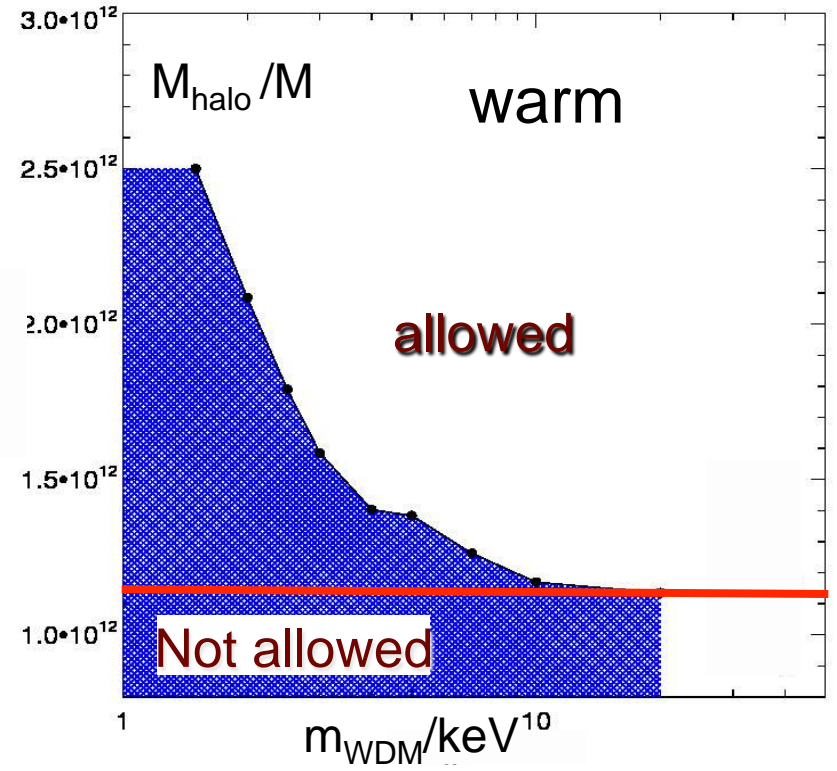
Wang, Frenk, Navarro, Gao '12

Cautun, Frenk, van den Weygaert, Hellwing '14

CDM requires

$$M_{\text{halo}} < 1.5 \times 10^{12} M_{\odot}$$

(95% confidence)



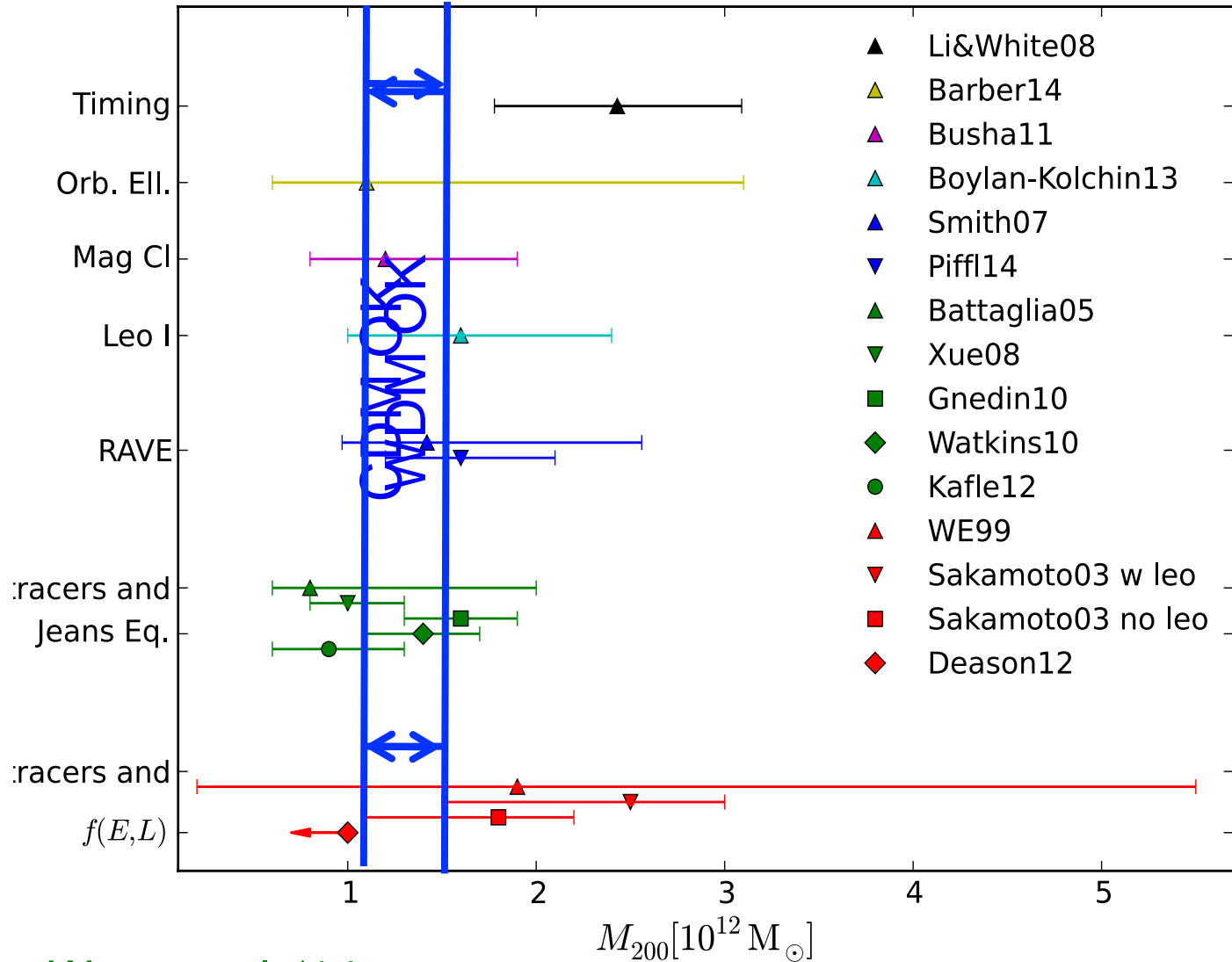
Kennedy, Cole Frenk, '14

WDM requires

$$M_{\text{halo}} > 1.1 \times 10^{12} M_{\odot}$$

(95% confidence)

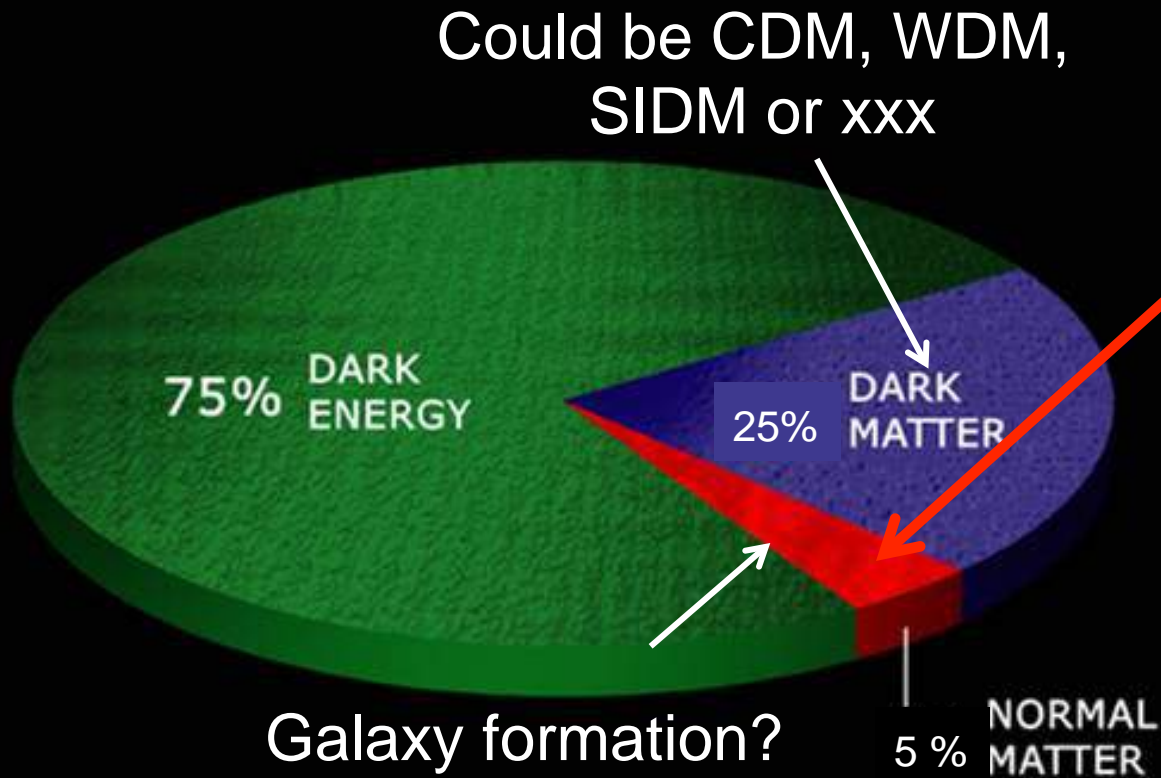
Estimates of the MW halo mass



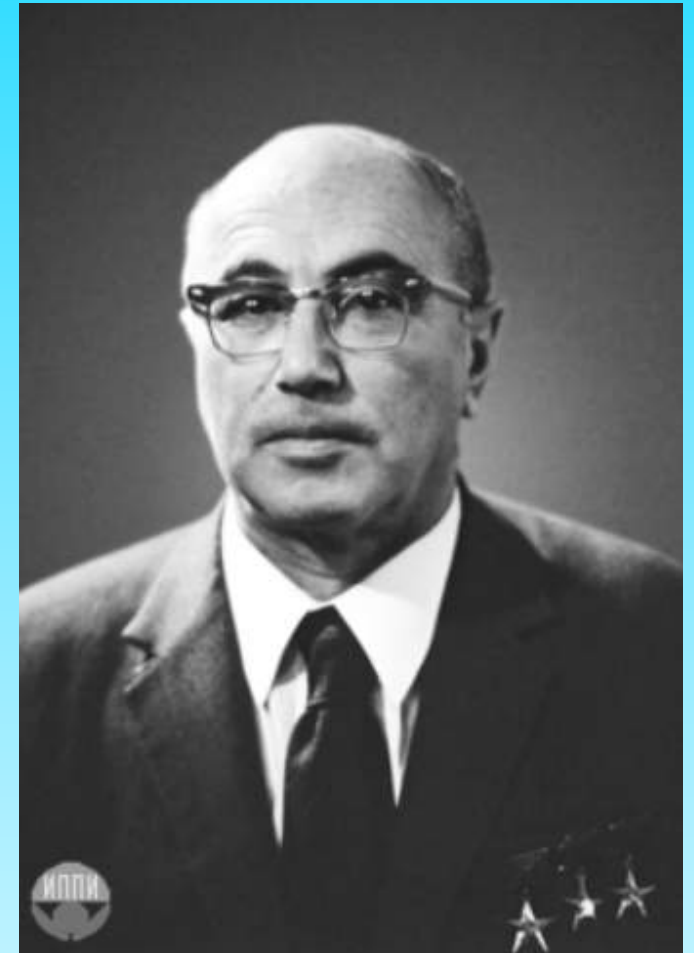
Wenting Wang et al. '14



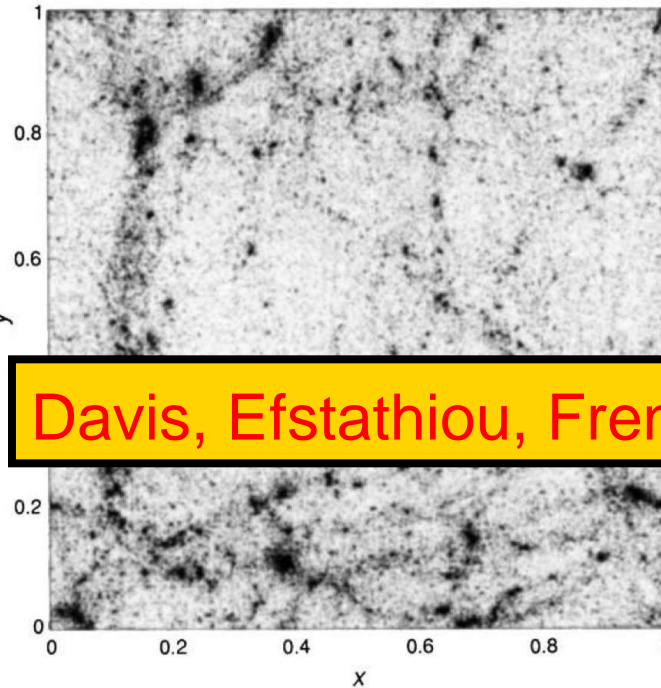
The content of our universe



Extrapolating from Krakow through Tallinn to the next symposium somewhere in the early eighties one can be pretty sure that the question of the formation of galaxies and clusters will be solved in the next few years.



$z=3$



Davis, Efstathiou, Frenk & White '92

5 Mpc

Many details of the CDM model, particularly those associated with galaxy formation, remain to be worked out, but the prospects seem promising. The next generation of sky surveys at optical, infrared and X-ray wavelengths, in combination with the measurement of redshifts for hundreds of thousands of galaxies, will produce a qualitative improvement in our knowledge of the large-scale galaxy distribution. If CDM is right, the 8-10-m apertures of the new generation of optical telescopes will enable us to see forming galaxies, to measure the evolution of galaxy clustering and to use absorption lines in the spectra of background quasars to study the gaseous component of protogalaxies. These observations will allow us to quantify many structure and to explore the evolution of the latest 90% of its history. Together with the rapidly improving technology for searches of variations in the brightness of the microwave background, they provide our best chance of testing the essential elements of the CDM picture for structure formation.

of the candidates. The attempt to identify the substance that apparently constitutes more than 90% of the mass of the Universe is surely one of the greatest challenges in contemporary physics. There are good reasons to hope that the mystery will be solved during this decade. □



Illustris Simulation

Vogelsberger, Genel, Springel, Torrey, Sijacki, Xu, Snyder, Bird, Nelson, Hernquist

Simulating the Universe

The EAGLE simulation project

Durham: Richard Bower, Michelle Furlong, Carlos Frenk, Matthieu Schaller, James Trayford, Yelti Rosas-Guevara, Tom Theuns, Yan Qu, John Helly, Adrian Jenkins.

Leiden: Rob Crain, Joop Schaye.

Other: Claudio Dalla Vecchia, Ian McCarthy, Craig Booth...

+ **Virgo Consortium**
NAM 2014



VIRG

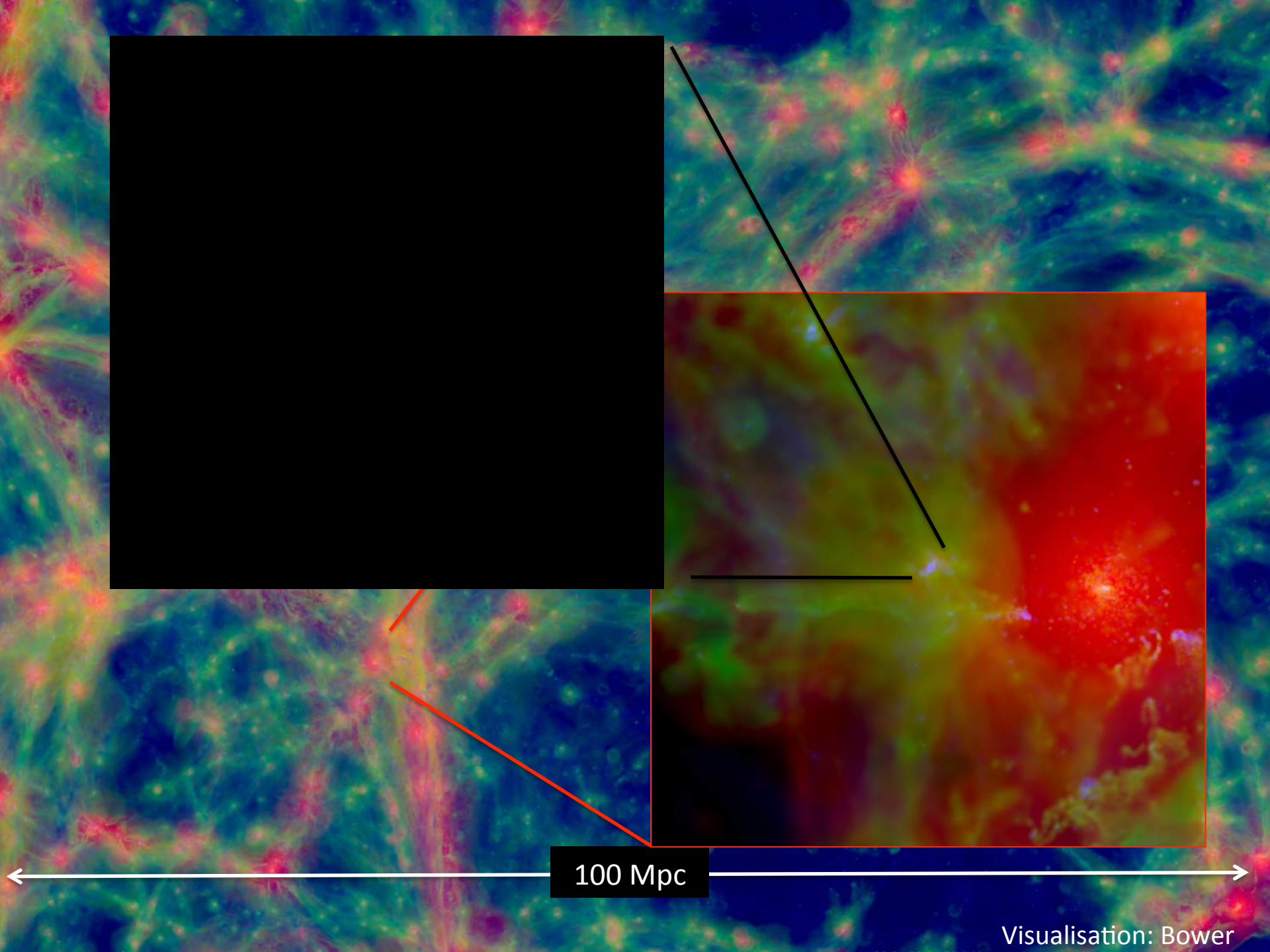


EAGLE: Evolution and Assembly of GaLaxies and their Environments

- Anarchy-SPH (Gadget-3) + Planck Cosmology
- Resolution 10^6 solar masses
- 25, 50 and 100 Mpc boxes
- Subgrid physics
 - Star formation
 - Cooling
 - Chemical evolution
 - Stellar feedback -> thermal
 - AGN feedback -> ang. mom.
- Evolution to $z=0$

← 20 Mpc →

This is only 1/8000 of the total volume



100 Mpc

Visualisation: Bower

The Eagle Simulations

EVOLUTION AND ASSEMBLY OF GALAXIES AND THEIR ENVIRONMENTS

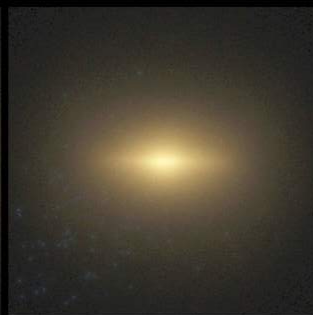
The Hubble Sequence realised in cosmological simulations

SB

E0

E7

S0

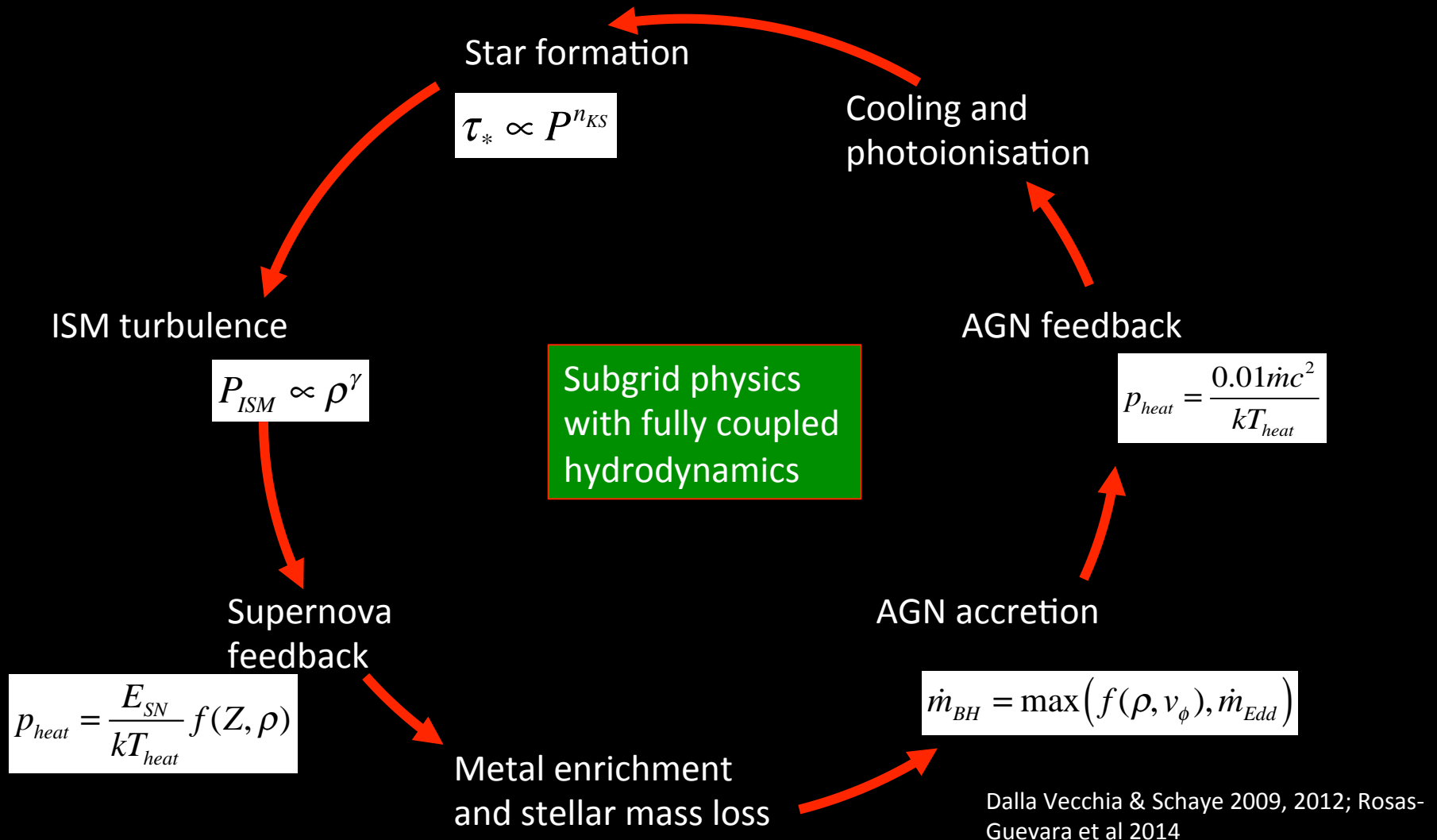


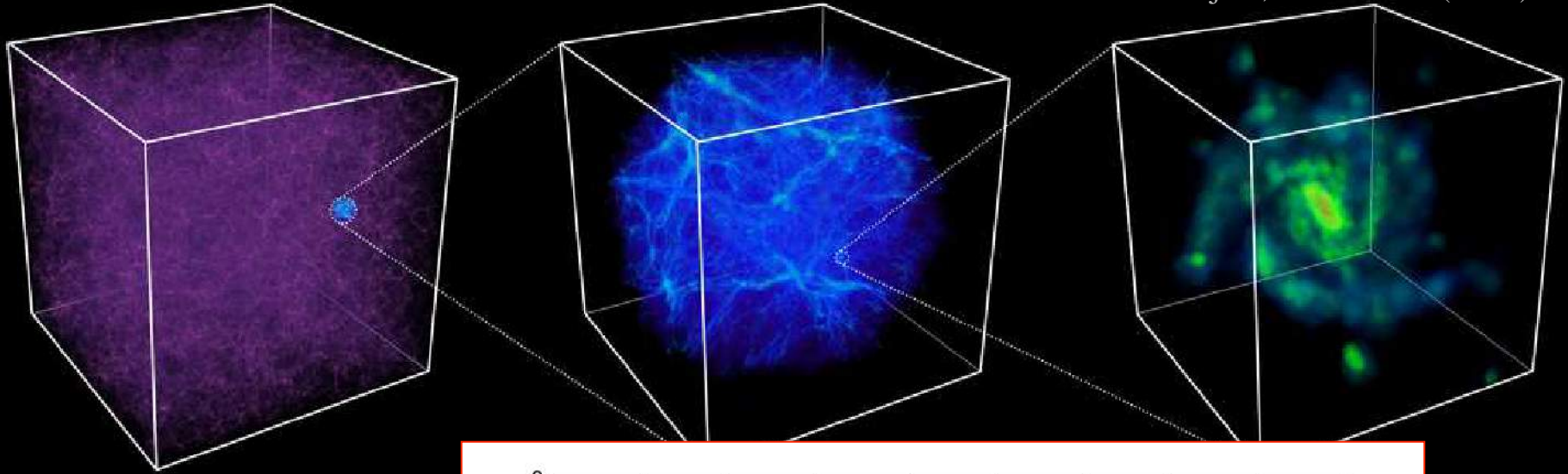
Irr

S

Trayford/Baes

Sub-grid schemes in EAGLE

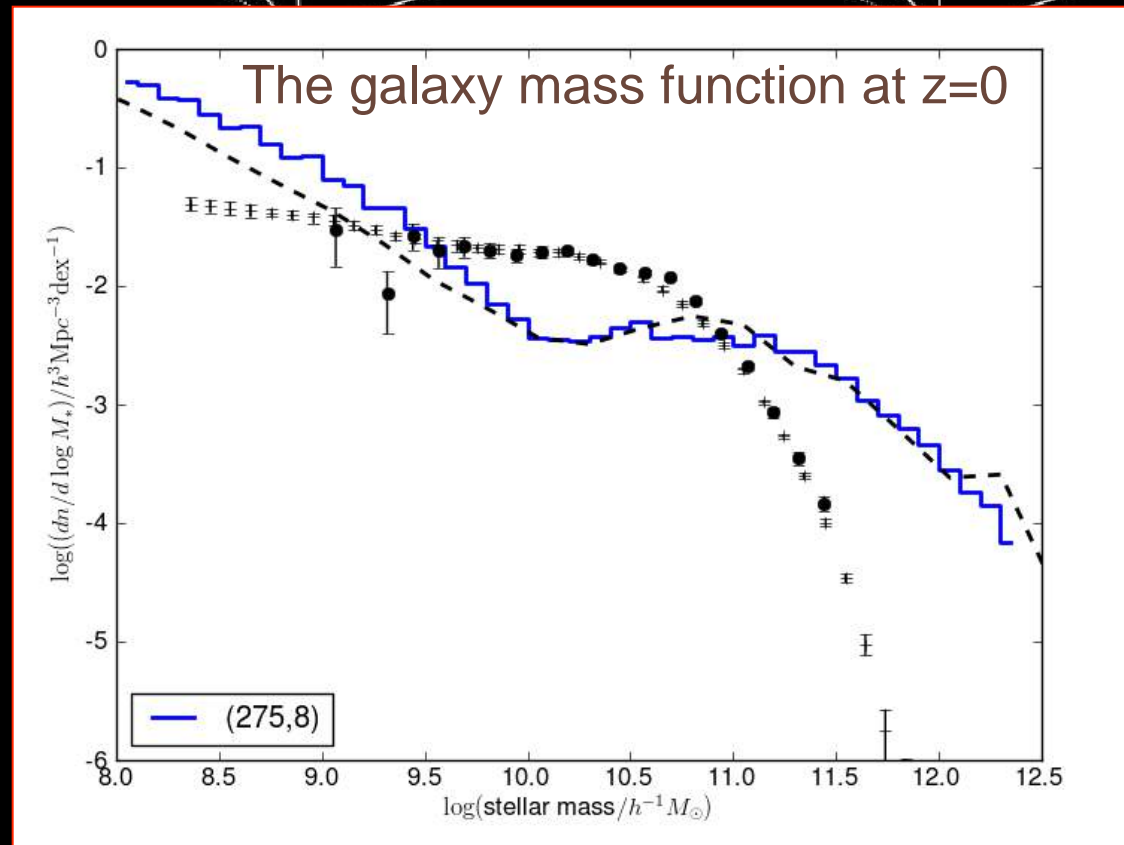




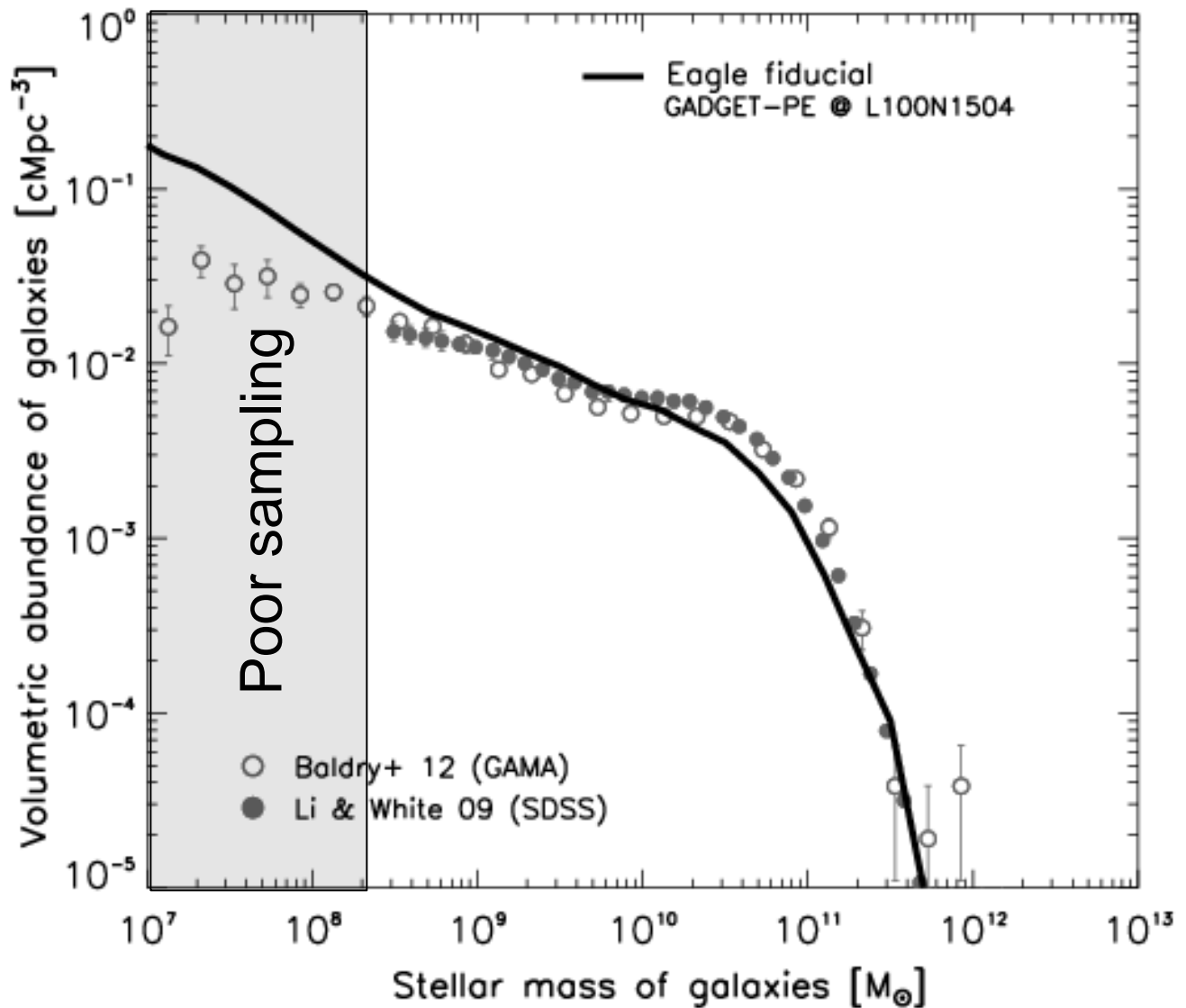
GIMIC

Previous generation
of cosmological
hydrodynamical
simulations

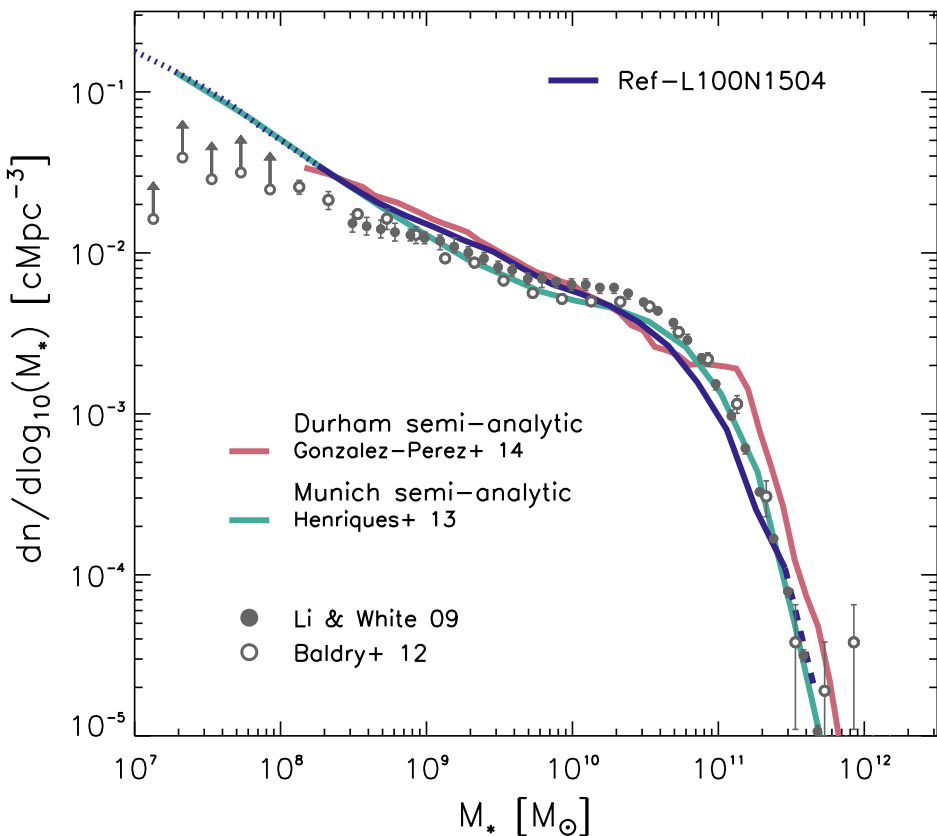
(Crain et al '08)



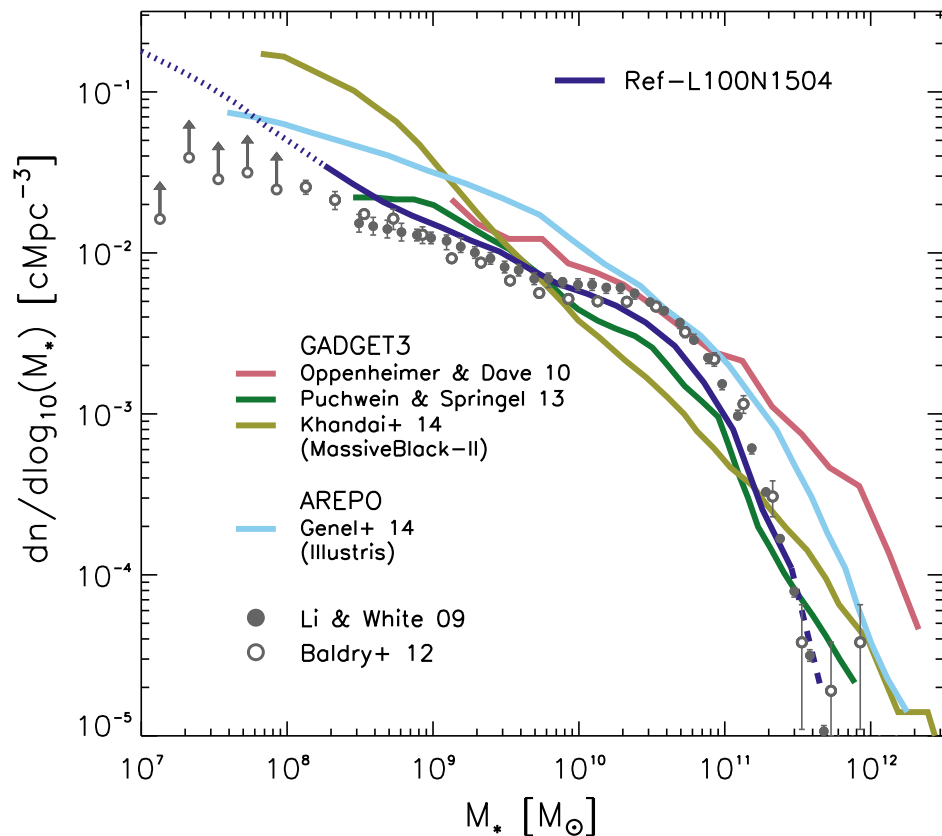
The galaxy mass function at $z=0$



EAGLE compared to other models



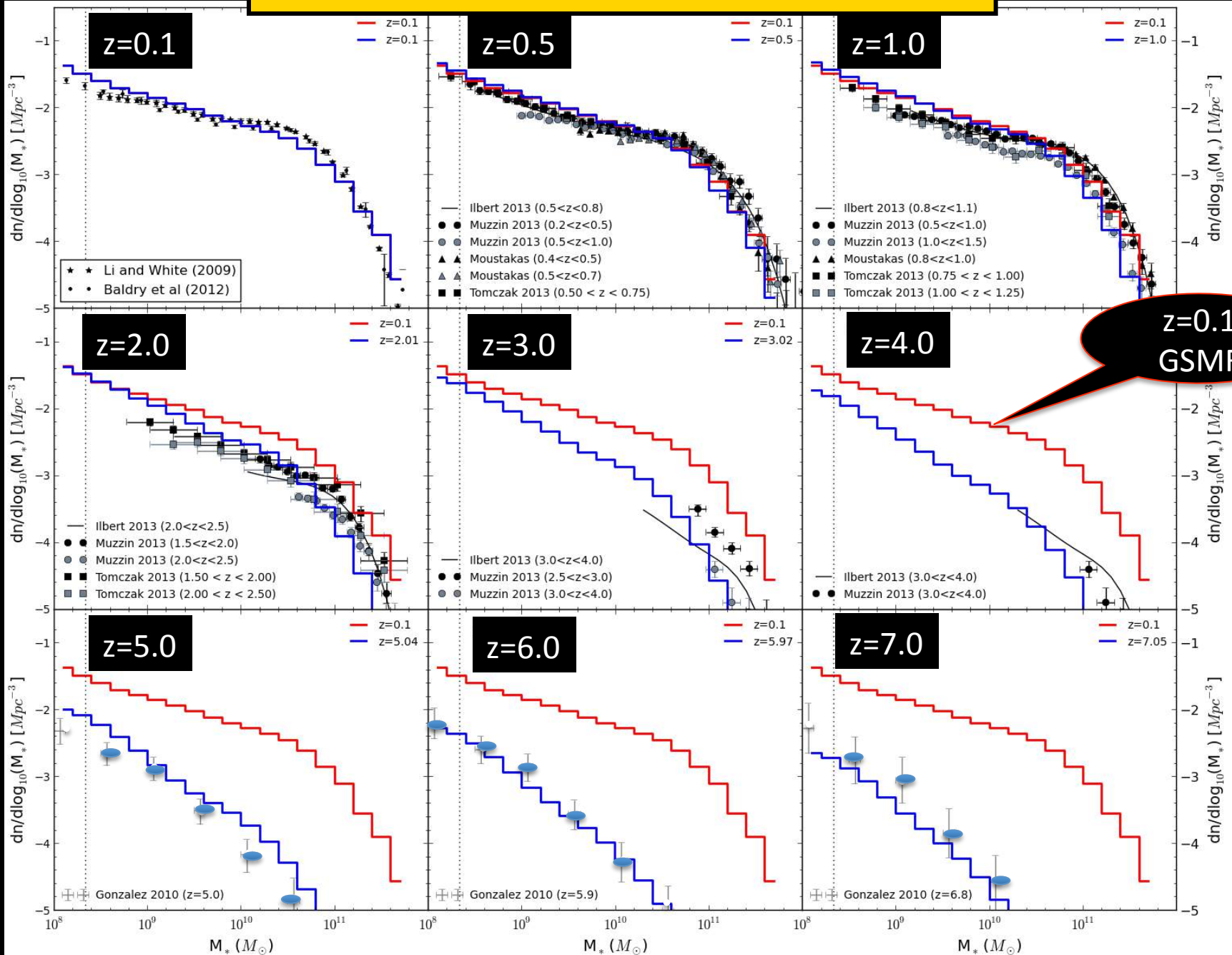
Semi-analytic models



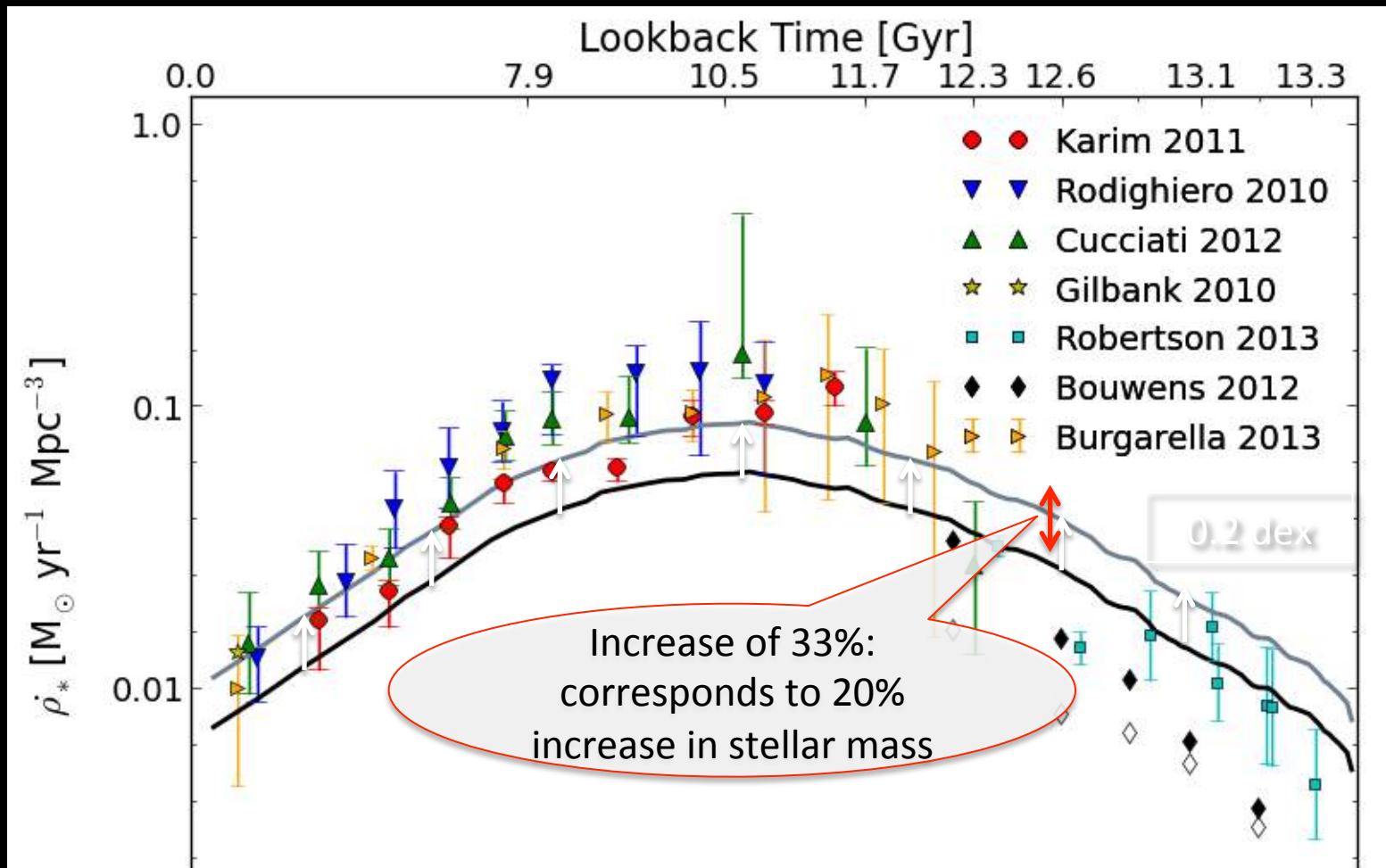
Hydrodynamic simulations

Evolution of the mass function

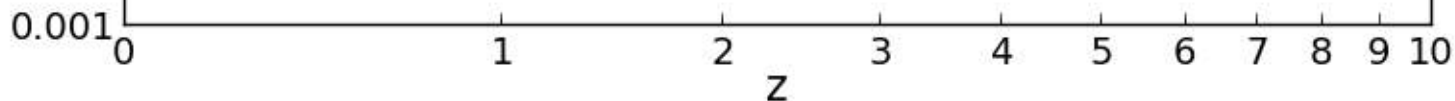
Galaxy Stellar Mass Function



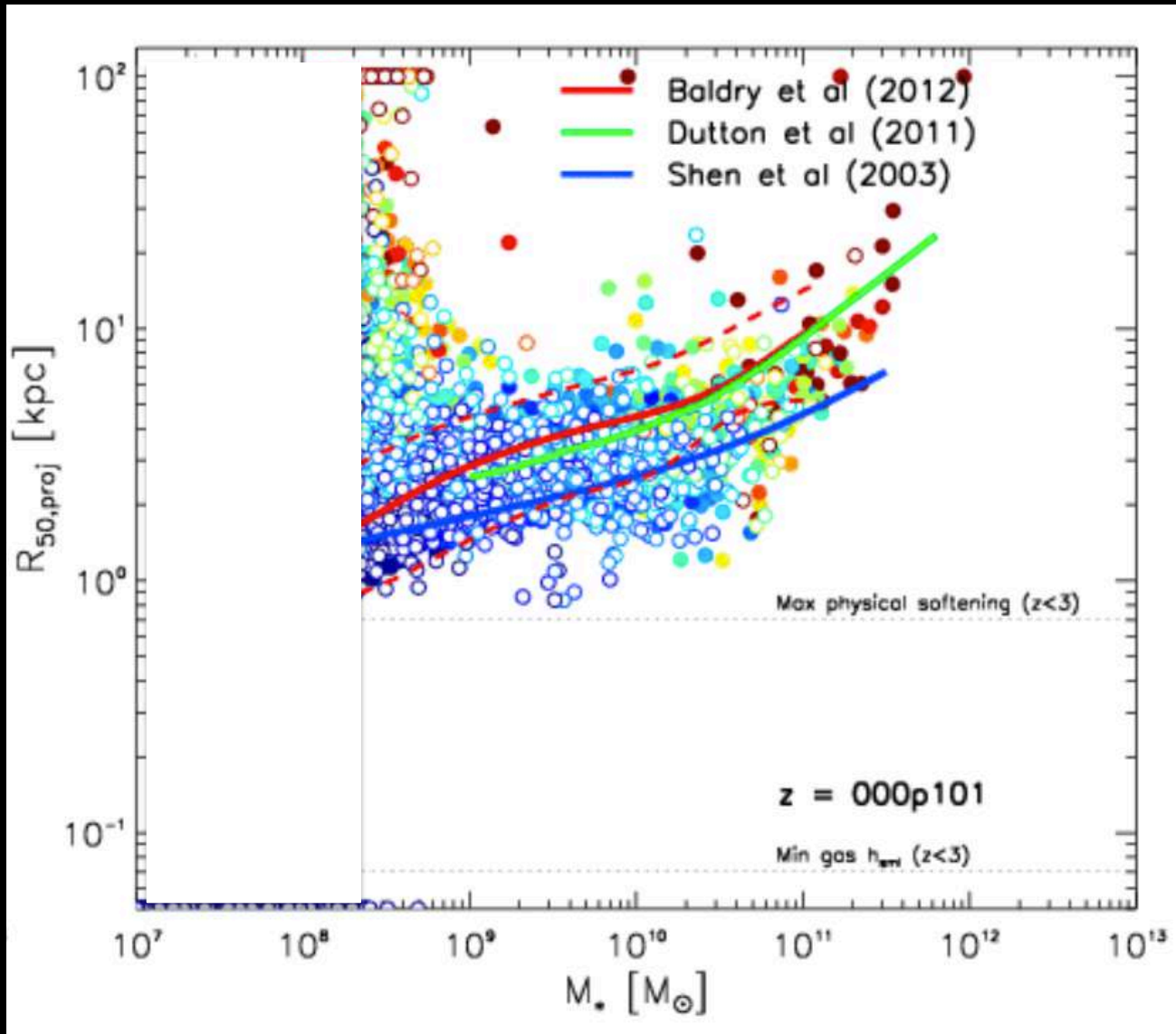
Evolution of the SFR density



Model recovers shape of the star formation history well, small offset in normalisation

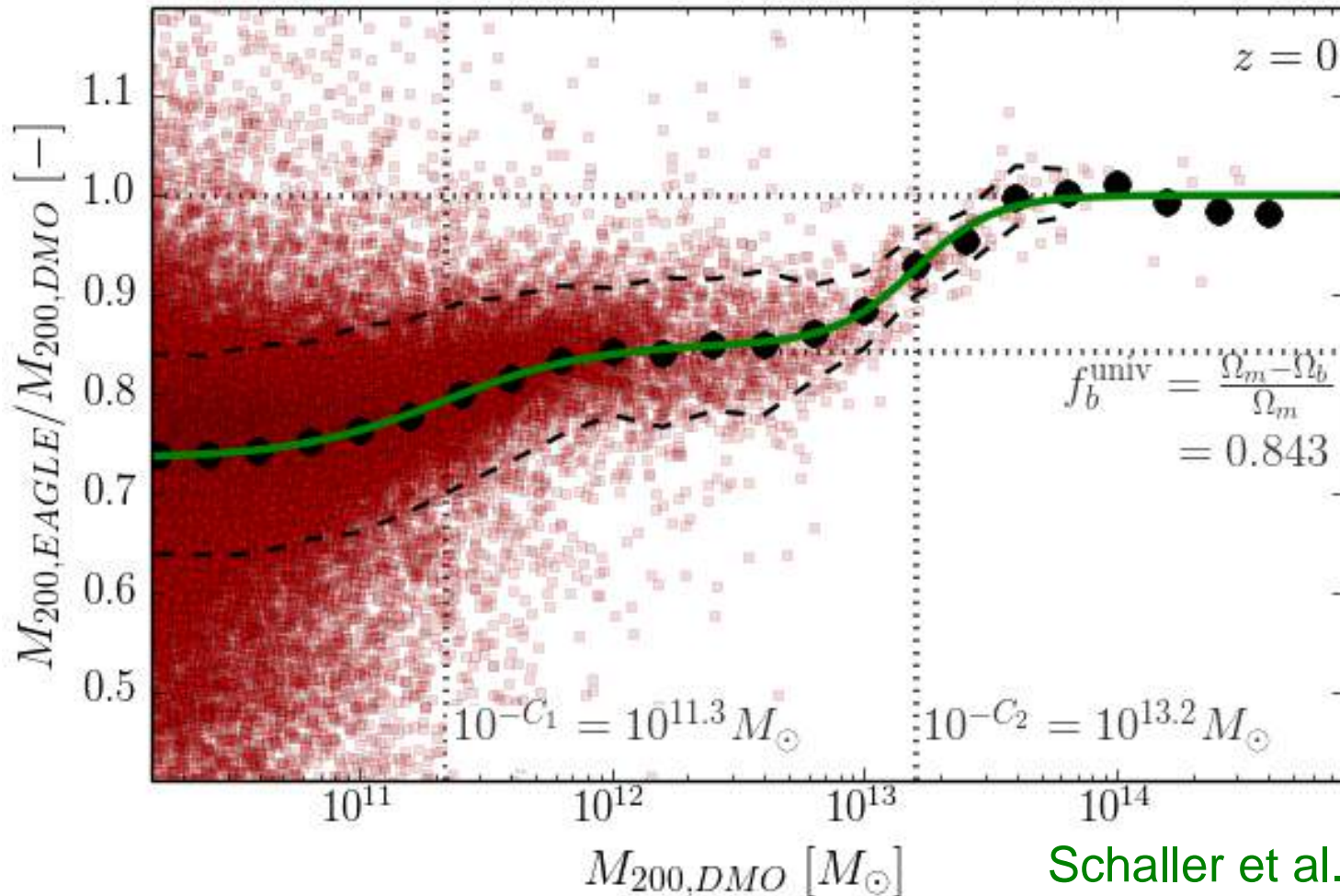


Galaxy sizes



Baryon effects: halo masses

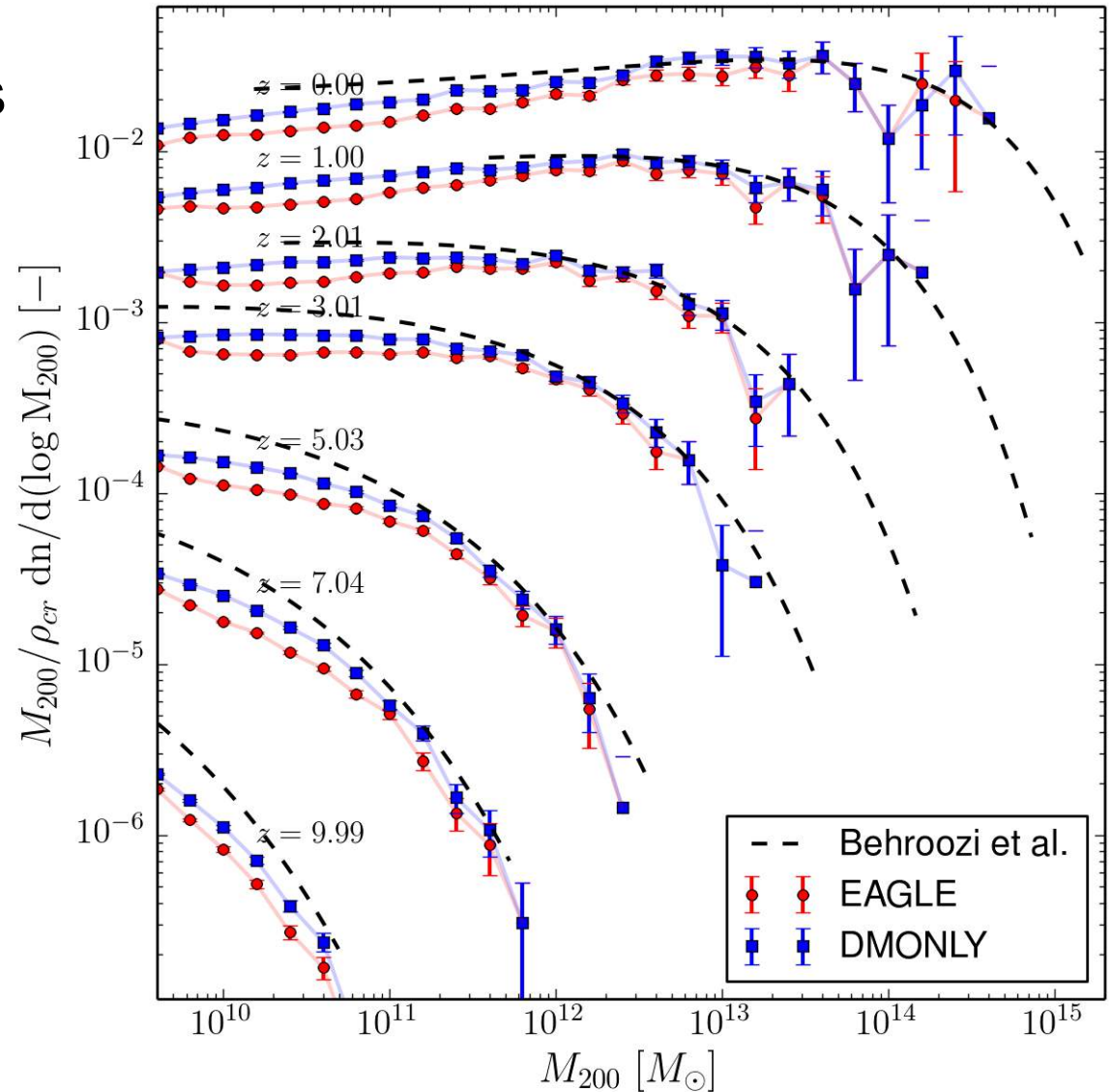
Average modification of halo masses as a function of mass

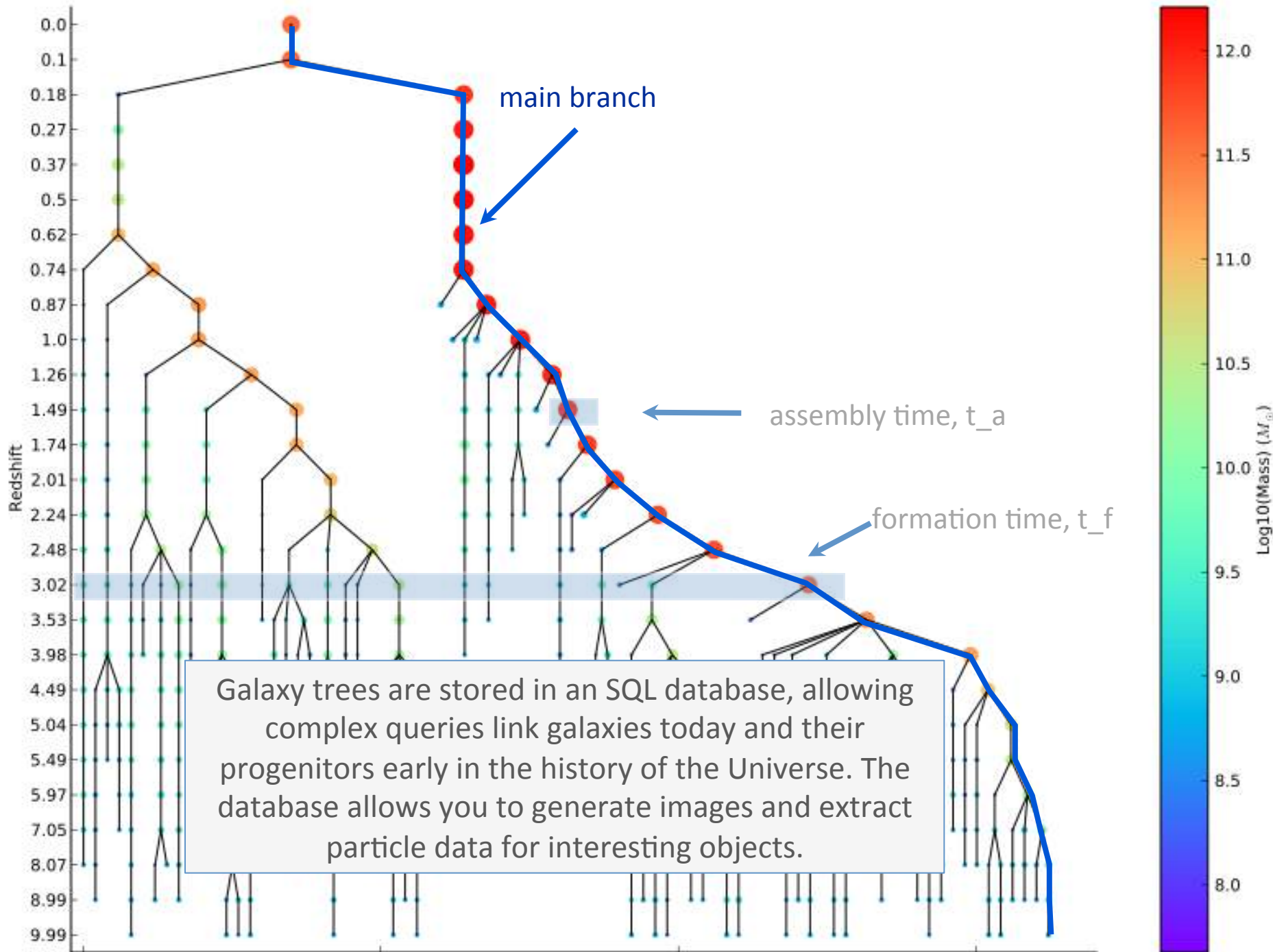


Schaller et al. '14

See also Sawala et al. '12, '14

Halo mass function as a function of z





Conclusions

- Modern cosmology began in ~1980 with two theoretical proposals
 - Inflation
 - non-baryonic DM
- Simulations of the cosmic web played the key role in developing the Λ CDM model, now validated by CMB and LSS data
- We don't know if the DM is CDM, but whatever it is, it must look like CDM on super-Galactic scales
- No too-big-to fail if M_h is small; WDM requires M_h to be large
- New frontiers
 - Dark energy
 - DM on sub-Galactic scales
 - Galaxy formation + environmental effects